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# **Design of Dual-Band FPD with High Selectivity**

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**ABSTRACT:** In this brief, a dual-band filtering power divider (FPD) with high selectivity and independently controllable passbands is designed. The proposed FPD consists of asymmetric folded F-type resonators (AFFRs) and quarter-wavelength three parallel-coupled lines (TPCLs). The center frequencies of the dual bands can be determined by adjusting the physical lengths of AFFRs. Meanwhile, TPCLs can increase the transmission paths and introduce multiple transmission zeros (TZs) to achieve high selectivity. For demonstration, the proposed FPD is designed, fabricated, and measured. The center frequencies are 2.59/3.63 GHz with the 3-dB fractional bandwidths (FBWs) of 12.95% and 7.88%, and the isolation between port 2 and port 3 is better than 12.56/21.03 dB. The minimum insertion losses are better than 0.54/0.32 dB in each passband. The simulated results are compared with measured ones, and good agreement is realized.

### **1. INTRODUCTION**

 $\mathbf{F}^{\text{ilters}}$  and power dividers are widely applied in microwave wireless communication systems. In order to achieve multifunction and miniaturization, filters and power dividers are integrated. T Filtering power divider (FPD) not only realizes the frequency selection, but also achieves signals division. In [1], a dual-band FPD was proposed by using three parallel-coupled lines (TPCLs), transmission lines, and a pair of short-ended parallel coupled lines. Unfortunately, only three transmission zeros (TZs) are generated, and the selectivity of passbands can be further enhanced. In [2-4], filters and FPD were composed of TPCLs, and multiple transmission zeros (TZs) have been generated, due to the horizontal transmission interference of the resonator and the new coupling path. In [5-9], two pairs of dual-resonance resonators (DRRs), two in-parallel transmission lines or shortended stepped-impedance resonators (SESIRs) were employed to design dual-band FPDs. Three TZs were generated by employing mixed electric and magnetic couplings, so two passbands selectivity was enhanced. In [10-12], Kron-Branin modeling and two-stage passive NGD cells have been proposed, providing new ideas for the diversity of modeling. In [13], a novel port-to-port isolation was proposed to design an FPD with good isolation, and the minimum insertion loss can be enhanced further. However, two TZs were realized by multiple-mode resonators, and the size of FPD has been increased.

In this brief, a dual-band FPD based on asymmetric folded Ftype resonators (AFFRs) is investigated. The two output ports are connected in parallel by a quarter-wavelength transmission line and the shunt connection through one resistor, aiming to realize high isolation between output ports. Meanwhile, the half-wavelength resonator is used to realize the passband working at 2.56 GHz and an open-stub loaded at the middle position working at 3.61 GHz. The two center frequencies and fractional bandwidths (FBWs) of the dual bands can be controlled independently by changing the parameters of AFFRs and the coupling gaps between TPCLs and AFFRs, respectively. The traditional method to improve FPD selectivity is employing more transmission paths. However, the size of the designed FPD will increase. In this brief, interdigital coupling lines are used to introduce extra transmission paths while keeping the FPD size unchanged. The simulated and measured results are in good agreement.

#### 2. DUAL-BAND FPD

#### 2.1. Asymmetric Short Stub-Loaded Resonator

The traditional center stub-loaded resonator (CSLR) consists of a half-wavelength uniform impedance resonator (UIR) and an open-stub loaded at the middle position shown in Fig. 1(a), where  $Y_1$ ,  $Y_2$ ,  $L_{r1}$ , and  $L_{r2}$  denote the characteristic admittances, length of the open-stub, and the folded resonator, respectively. The even-odd mode equivalent circuits are shown in Figs. 1(b) and (c). In order to simplify the calculation,  $Y_2 = 2Y_1$  is set, and the input impedances  $Z_{in,odd}$  and  $Z_{in,even}$ can be expressed as [14]:

$$Z_{in,odd} = -\frac{\tan\left(\theta_1\right)}{jY_1} \tag{1}$$

$$Z_{in,even} = \frac{2Y_1 - Y_2 \tan(\theta_1) \tan(\theta_2)}{jY_1 (Y_1 \tan(\theta_1) + Y_2 \tan(\theta_2))}$$
(2)

Therefore, the even-odd mode resonant frequencies are calculated as:

$$f_1 = f_{odd} = \frac{c}{2L_{r2}\sqrt{\varepsilon_{eff}}} \tag{3}$$

$$f_2 = f_{even} = \frac{c}{(L_{r2} + 2L_{r1})\sqrt{\varepsilon_{eff}}}$$
(4)

where c expresses the light speed in free space, and  $\varepsilon_{eff}$  is the effective dielectric constant of the substrate. Based on formu-



FIGURE 1. (a) CSLR, (b) even-mode and (c) odd-mode equivalent circuit of CSLR, (d) asymmetric short stub-loaded resonator, (e) AFFR and (f) equivalent circuit of AFFR.

las (3) and (4), the even-mode determines the higher resonant frequency, and the odd-mode defines the lower one.

In Fig. 1(d),  $L_d$  is the displacement of the loaded resonator relative to the center open-stub. CSLR is folded to realize miniaturization, as shown in Fig. 1(e). The AFFR introduces an additional resonance mode because the position of openloaded stub is unlimited. In order to simplify the calculation, the same characteristic impedance of AFFR is designed and used for analysis. The equivalent circuit of AFFR is given in Fig. 1(f), where  $\theta_T$  ( $\theta_T = \theta_2 + \theta_3 + \theta_4 + \theta_5$ ) is the electrical length of UIR; the electrical length of the loaded stub is  $\theta_1$ ; and  $\theta_2 + \theta_3 \neq \theta_4 + \theta_5$ .  $\alpha$  and  $\beta$  are defined as follows:

$$\alpha = \frac{\theta_2 + \theta_3}{\theta_2 + \theta_3 + \theta_4 + \theta_5} = \frac{\theta_2 + \theta_3}{\theta_T}$$
(5)

$$\beta \frac{\theta_1}{\theta_2 + \theta_3 + \theta_4 + \theta_5} = \frac{\theta_1}{\theta_T} \tag{6}$$

where  $\alpha$  is the ratio of the shorter section to total length of UIR, and  $\beta$  is defined as the radio of the loaded stub to the total length of UIR.

#### 2.2. Dual-Band FPD Design

Figure 2(a) illustrates the configuration of the proposed dualband FPD, which consists of AFFRs, TCLRs, and an isolation resistor. The transmission-line equivalent circuit is shown in Fig. 2(b). For even-odd mode excitation, the equivalent circuits are given in Figs. 2(c) and (d), where  $\theta_i$  (i = 1, 2, 3) represents the electrical length, and  $Z_i$  (i = 1, 2, 3) is the impedance of the microstrip line.

The end-coupling and TPCL are exhibited in Figs. 3(a) and (b). TPCL is composed of interdigital coupling lines, which increases the transmission paths and achieves two TZs. Meanwhile, the out-of-band characteristics are improved without influencing the in-band characteristics. The novel TPCL generates  $TZ_2$  and  $TZ_3$  to enhance the selectivity in Fig. 3(c). It can be obtained that the out-of-band suppression is controlled by the different lengths of  $L_1$  (total length of the interdigital coupled line), as shown in Fig. 3(d).

For dual bands, the half-wavelength resonator realizes the lower frequency band ( $f_1$ , 2.59 GHz), and  $f_1$  is controlled by  $L_{r2}$  while the higher frequency band ( $f_2$ , 3.63 GHz) is achieved

by employing  $L_{r2}$  and  $L_5$ . In order to explain the effects of AFFR lengths on two center frequencies, simulation calculations are performed on each branch, and the results are shown in Fig. 4. As shown in Figs. 4(a) to (d),  $f_1$  and  $f_2$  decrease with the increase of  $L_r = L_4 + L_6$ ,  $L_3$ ,  $L_7$ ,  $L_8$ .  $f_2$  can be controlled independently by  $L_5(L_{r1} = L_5)$  as shown in Fig. 5. Based on formula (3), the lower resonant frequency  $f_{odd}$  for  $f_1$  is affected by the value of  $L_{r2}(L_r + L_3 + L_7)$ . Similarly,  $f_{even}$  for  $f_2$  is influenced by the dimensions of the open-stub loaded.

The FBWs are controlled by the coupling gaps  $S_1$  and  $S_3$ , because AFFRs are fed by TPCL. FBW<sub>1</sub> (fractional bandwidth of the first passband, the same as below) is determined independently by physical length  $S_1$ , as shown in Fig. 6(a). Meanwhile, FBW<sub>1</sub> and FBW<sub>2</sub> vary with the coupling gap  $S_3$ , and quasi-independent control of FBW<sub>1</sub> and FBW<sub>2</sub> can be realized by  $S_1$  and  $S_3$ .

Due to the symmetrical structure of the proposed dual-band FPD, to simplify the calculation, the three-port circuit can be simplified as its half-two-port bisection network for isolation analysis [13]. As given in Figs. 2(c) and (d),  $S_{22}$  and  $S_{23}$  are defined as

$$S_{22} = \frac{\Gamma_e + \Gamma_o}{2} \tag{7}$$

$$S_{32} = \frac{\Gamma_e - \Gamma_o}{2} \tag{8}$$

where  $\Gamma_e$  and  $\Gamma_o$  are the reflection coefficients of the even-odd mode circuit at port 2.  $\Gamma_e$  and  $\Gamma_o$  can be given by

$$\Gamma_e = \frac{Z_{ine} - Z_0}{Z_{ine} + Z_0} \tag{9}$$

$$\Gamma_o = \frac{Z_{ino} - Z_0}{Z_{ino} + Z_0} \tag{10}$$

where  $Z_0$  is the impedance of port.  $Z_{ine}$  is the input impedance of the even-mode circuit and can be calculated as

$$Z_{ine} = Z_4 \frac{Z_{ine}^1 + jZ_4 \tan \theta_{10}}{Z_4 + jZ_{ine}^1 \tan \theta_{10}}$$
(11)

where

$$Z_{ine}^{1} = -jZ_{a3}\cot\theta_{10} + \frac{Z_{b3}^{2}\csc^{2}\theta_{10}}{Z_{ine}^{2} - jZ_{a3}\cot\theta_{10}}$$
(12)



FIGURE 2. (a) Topology of the proposed dual-band FPD, (b) transmission-line equivalent circuit, (c) even-mode and (d) odd-mode equivalent circuit of the proposed FPD.



FIGURE 3. (a) End-coupling, (b) TPCL, comparison of selectivity with (c) different types of coupling and (d) sizes of the interdigital coupled line.

$$Z_{ine}^{2} = \frac{jZ_{1}Z_{ine}^{3}\cot\left(\sum_{i=2}^{8}\theta_{i}\right)}{jZ_{1}\cot\left(\sum_{i=2}^{8}\theta_{i}\right) - Z_{ine}^{3}}$$
(13)

$$Z_{ine}^{3} = -jZ_{a1}\cot\theta_{10} + \frac{Z_{b1}^{2}\csc^{2}\theta_{10}}{2Z_{0} - jZ_{a1}\cot\theta_{10}}$$
(14)



**FIGURE 4**. Variation of odd-mode resonance frequency of AFFR with parameters (a)  $L_r$ , (b)  $L_3$ , (c)  $L_7$  and (d)  $L_8$ .



**FIGURE 5**. Variation of even-mode resonance frequency of AFFR with different  $L_5$ .

$$\begin{cases} Z_{ai} = \frac{Z_{ei} + Z_{oi}}{2} \\ Z_{bi} = \frac{Z_{ei} - Z_{oi}}{2} \end{cases} (i = 1 \quad or \quad 3)$$
(15)

The input impedance  $Z_{ino}$  can be expressed as

$$Z_{ino} = \frac{Z_{ino}^{1}R}{R + 2Z_{ino}^{1}}$$
(16)

where

$$Z_{ine}^1 = j Z_4 \tan \theta_{10} \tag{17}$$

When  $f_0 = (f_1 + f_2)/2$ ,  $\theta = 90^\circ$  is defined.  $f_1$  and  $f_2$  are the center frequencies of the two passbands of the proposed FPD.  $S_{22} = 0$ , and  $S_{32} = 0$ , (11) and (16) can be derived as

$$Z_{ine} = Z_0 = \frac{Z_4^2 Z_{b1}^2}{2Z0Z_{b3}^2}$$
(18)

$$Z_{ino} = Z_0 = \frac{R}{2}$$
 (19)

If  $Z_{b1} = Z_{b3}$ , one can obtain that  $Z_4 = \sqrt{2}Z_0$  and  $R = 2Z_0$ . The in-band isolation increases from 5.01/5.93 dB to 12.56/21.03 dB in Fig. 7, respectively.

#### 3. SIMULATION AND MEASUREMENT RESULTS

In this brief, the proposed dual-band FPD is designed on an F4BM-2 substrate with a thickness of 0.8 mm and a dielectric constant of 2.2. The measurement of FPD is done by an Agilent Network Analyzer N5230A.

In Fig. 2(a), the cases of the dual-band FPD are:  $L_1 = 10.6 \text{ mm}, L_2 = 37.46 \text{ mm}, L_3 = 12 \text{ mm}, L_4 = 7.3 \text{ mm}, L_5 = 12.3 \text{ mm}, L_6 = 12.2 \text{ mm}, L_7 = 9.4 \text{ mm}, L_8 = 8.5 \text{ mm}, L_9 = 6.5 \text{ mm}, L_{10} = 8.2 \text{ mm}, W_1 = 1.24 \text{ mm}, W_2 = 0.3 \text{ mm}, W_3 = 0.3 \text{ mm}, W_4 = 2 \text{ mm}, W_5 = 1.36 \text{ mm}, S_1 = 0.1 \text{ mm}, S_2 = 0.17 \text{ mm}, S_3 = 0.6 \text{ mm}, S_4 = 0.6 \text{ mm}, R = 100 \Omega.$ Fig. 8(a) shows the fabricated dual-band FPD, and its overall size is 67.38 mm × 61.96 mm (0.79 $\lambda_g \times 0.73\lambda_g$ , where  $\lambda_g$  is the guide wavelength at 2.59 GHz). In Fig. 8(a), the





**FIGURE 6**. Variation of the two center frequencies with the parameters (a)  $S_1$  and (b)  $S_3$ .



FIGURE 7. Effect of resistor on isolation.



**FIGURE 8**. Simulated and measured results of the proposed dual-band FPD (a)  $|S_{11}|$  and  $|S_{21}|$ , (b)  $|S_{23}|$ , (c) amplitude imbalance and phase difference, and (d) photograph of the proposed FPD.

Ref.	$f_0$ (GHz)	IL (dB)	3-dB FBW (%)	Number of TZs	Isolation	Size $(\lambda g \times \lambda g)$
[1]	2.4/3.8	N/A	43.6/25.1	3	> 15.0	$0.49 \times 0.49$
[6]	4.11/6.56	0.8/1.8	N/A	0	17/26	0.133  imes 0.133
[7]	2.46/5.19	1.74/2.12	4.5/2.3	3	15.3/22.5	0.09  imes 0.09
[9]	5.5/8.3	0.9/1.5	N/A	0	> 20	$2.15 \times 0.89$
This work	2.59/3.63	0.54/0.32	12.95/7.88	4	12.56/21.03	0.79 × 0.73

TABLE 1. Comparisons with some reported dual-band FPDs.

FBW: fractional bandwidth. IL: insertion loss. TZs: transmission zeros.

measured two center frequencies are 2.59/3.63 GHz with 3-dB FBWs of 12.95/7.88%. The insertion losses in-band are less than 0.54/0.32 dB (excluding 3-dB power division), and the return losses are better than 12.8/21.8 dB. The isolation is better than 12.56 dB in Fig. 8(b). In addition, four TZs (2.11, 3.1, 3.31, and 4 GHz) are realized successfully at the edges of the passbands to achieve higher selectivity. The phase difference and magnitude imbalance within the passbands are less than  $1^{\circ}$  and 0.5 dB, respectively in Fig. 8(c). Table 1 summarizes the comparisons in the key performance parameters between the proposed FPD and other reported ones. The proposed one is featured by the low insertion losses and high selectivity.

### 4. CONCLUSION

In this letter, a dual-band FPD with good performance has been proposed. The physical size of AFFRs can independently control the center frequencies of the two passbands, and the 3-dB FBWs can be determined by the coupling gaps between AFFRs and TPCLs. The TPCLs can increase the transmission paths and introduce two TZs to effectively improve the selectivity. Due to the small insertion loss and good selectivity, the proposed dual-band FPD is widely used in the application of wireless communication systems.

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