A Compact Coplanar Waveguide Spoof Surface Plasmon Polariton with Enhanced Field Confinements

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ABSTRACT: In this article, a spoof surface plasmon polariton (SSPP) based on coplanar waveguide (CPW) with flipper structures is proposed to improve field confinement. The analyses based on the developed equivalent circuit (E.C) reveal that the proposed unit exhibits flexibly controllable dispersion features and improved field confinements owing to the introduction of the flipper structures. Finally, the proposed SSPP TL is designed, fabricated, and tested to validate the design principles. The experiment results illustrate the theoretical analyses and validate that the proposed SSPP TL exhibits ultra-compact size occupation and enhanced field confinement.

1. INTRODUCTION

The concept of spoof surface plasmon polarization (SSPP) is developed to mimic natural SPPs at terahertz and microwave frequencies [1]. Different structures such as onedimensional arrays of grooves have been employed to construct SSPP transmission lines (TLs) [2–6]. However, if stronger field confinement in the millimeter or microwave band is expected, deeper grooves and hence a geometrical size are required which poses a crucial limitation for many real applications.

To break through this restriction, many compact SSPPs with strong field confinements are reported in recent years. In [7], a novel SSPP TL with zigzag grooves is proposed. By using such grooves, the SSPP TL can exhibit ultra strong field confinement with a limited strip width. Capacitive loading techniques are utilized in [8,9] to manipulate the dispersion characteristics and enhance field confinement. In [10], an onchip SSPP TL with reduced size and ultra-strong field confinement using 0.18 µm Complementary Metal Oxide Semiconductor (CMOS) technology is proposed. However, relatively complicated mode-conversion structures are still required to convert guided waves to SSPP wave [7-10], increasing transversal width largely. In [11–13], three advanced SSPPs with enhanced field confinement are reported. In [14], a new coplanar waveguide (CPW) SSPP with a simple and efficient modeconversion transition structure is proposed, exhibiting the advantages of lower cut-off frequency (8.9 GHz) and stronger field confinement than the conventional CPW SSPP. Based on the CPW SSPP in [15], we proposed another new SSPP with improved field confinement. However, field confinements of these SSPPs are still not strong enough.

In this work, a novel CPW SSPP TL with flipper structures is proposed. Dispersion analyses based on the equivalent circuit reveal the stronger confinement ability of this new TL than conventional unloaded one. Measured S-parameters and simulated electric field distributions indicate enhanced field confinement

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ability due to the introduced flipper structure. Finally, experimental example is designed and fabricated to validate our design principles. The experimental results are in accordance with the theoretical ones. The ultra-strong field confinement of the proposed spoof SPP TL can be utilized to suppress the crosstalk or reduce the area of some microwave devices.

2. THEORY AND DESIGN PRINCIPLE

In our previous work [15], we proposed a CPW SSPP TL with stepped groove structures. Based on that SSPP, we designed a new CPW SSPP unit by loading flipper structures as shown in Figure 1. The material of the substrate in Figure 1 and all the following examples in this paper is FR4 with a dielectric constant of 4.4, a loss tangent of 0.02, and a thickness of 0.8 mm.

As shown in Figure 1, The proposed unit consists of a central CPW line with the line width of w_m and coupled gap of w_p . The parameter p denotes the period of the unit cell. Each stepped groove structure is composed of one wider slot line with the width of w_{s1} and length of l_{s1} , and one narrower slot line with the width of w_{s2} and length of l_{s2} . The flipper structure consists of a metallic patch with the width of w_1 and length of l_1 on the bottom layer of the unit. The metallic patch is connected to the CPW ground on the top layer through a metallic via with the radius of d.

To further explain operating principle of the proposed SSPP TL unit cell, we developed an equivalent circuit (E.C) model in Figure 1 according to the coupled-mode theory [16]. In the E.C model, the two capacitors C represent the effect of the flipper structures. The two TL models (Z_s, θ_s) represent the two CPW lines with the width of w_s and length of p/2. The TL models (Z_1, θ_1) and (Z_2, θ_2) represent the wider and narrower slot lines in each stepped groove structure, respectively. The transformers represent the electromagnetic coupling between the etched groove structures and the CPW line. Obviously, the unloaded SSPP corresponds to the case that C = 0 [10].



FIGURE 1. The proposed SSPP TL unit cell and its equivalent circuit.

In the E.C model, voltage and current on both sides of N_{th} unit cell $(V_n, I_n, V_{n+1}, I_{n+1})$ can be connected by transfer matrix which is also called ABCD matrix as follows:

$$\begin{bmatrix} V_n \\ I_n \end{bmatrix} = \begin{bmatrix} A & B \\ C & D \end{bmatrix} \begin{bmatrix} V_{n+1} \\ -I_{n+1} \end{bmatrix}$$
(1)

where A, B, C, and D represent the parameters of the ABCD matrix. As a symmetric network (A = D), the propagation

 χ_1

constant β should be in conformity with the subsequent relation:

$$\cos\left(\beta p\right) = A\tag{2}$$

By considering and combining Equations (2) and (3), then we can obtain the following relationship.

$$\beta = \cos^{-1}(A) = \cos^{-1}(\chi_1 + \chi_2 + \chi_3)$$
(3)

where:

$$= \frac{C\omega Z_1 \sin\left(2\theta_s\right) \left(Z_1 \tan \theta_1 + Z_2 \tan \theta_2\right)}{4n^2 Z_s \left[Z_1 \left(Z_1 \tan \theta_1 + Z_2 \tan \theta_2\right) + C\omega \left(Z_1 - Z_2 \tan \theta_1 \tan \theta_2\right)\right]}$$
(4)

$$= \frac{-Z_1 \cos\left(2\theta_s\right) \left(Z_1 \tan \theta_1 + Z_2 \tan \theta_2\right)}{(5)}$$

$$C_{2} = Z_{1} \left(Z_{1} \tan \theta_{1} + Z_{2} \tan \theta_{2} \right) + C_{\omega} \left(Z_{1} - Z_{2} \tan \theta_{1} \tan \theta_{2} \right)$$

$$C_{\omega} \cos \left(2\theta_{e} \right) \left(Z_{2} \tan \theta_{1} \tan \theta_{2} - Z_{1} \right)$$
(5)

$$\chi_3 = \frac{1}{Z_1 (Z_1 \tan \theta_1 + Z_2 \tan \theta_2) + C\omega (Z_1 - Z_2 \tan \theta_1 \tan \theta_2)}$$
(6)

It can be observed from Equation (3) that the value of C brought by the flipper structures influences the dispersion feature of the proposed unit. To further investigate the relationship between the asymptotic frequency and the dimension of loaded flipper structures, Figures 2(a) and (b) plot the E.C computed and electromagnetic (EM) simulated dispersion curves of the proposed unit for various l_1 and w_1 , respectively. The dimension parameters in Figure 4 are set as follows: $w_{s1} = 2$, $w_{s2} = 0.15$, $l_{s1} = l_{s2} = 7$, $l_{s3} = 1.5$, $w_m = 2.45$, $w_p = 0.14$, d = 0.2, l = 40, and p = 10 (all dimensions are in mm).

As shown in Figure 2, the loaded unit cell exhibits typical SSPP response which remains near the air line at low frequencies but goes away at high frequencies. It can also be observed that the E.C computed results are in accordance with the EM results, which demonstrates the accuracy of the proposed E.C model. Figure 2(a) compares the dispersion curves when w_1 is fixed at 7 mm, but l_1 is different. It can be observed that the larger the value of l_1 is, the larger the capacitance introduced by the flipper structures is, and the lower the asymptotic frequency is. Also, Figure 2(b) discusses the dispersion features when l_1 is fixed at 8 mm, but w_1 is different. The larger value of w_1 achieves larger capacitance and thus results in lower asymptotic frequency.

In summary, since the difference between the loaded and unloaded unit is the introduction of extra flipper structures, the decrease in asymptotic frequency can be attributed to the capacitance brought by the extra flipper structures. Secondly, the larger the area of the metallic patch of the flipper structures $(l_1 \times w_1)$ is, the larger the capacitance introduced by the flipper structures is, the lower the asymptotic frequency of the unit is. Since the decrease of the asymptotic frequency leads to the tighter field confinement, the proposed SSPP has stronger field confinement than conventional unloaded one. Moreover, the field confinement can be flexibly controlled by changing the geometrical dimension of the flipper structure without requiring modifications of the transversal geometrical configurations.

3. DESIGN AND MEASUREMENT

The unloaded and loaded SSPP TL based on the proposed unit is shown in Figures 3(a) and (b), respectively. It can be observed that these SSPP TLs consist of three different kinds of parts marked as I, II, and III, respectively. Part I is CPW region at two terminals. The dimensions of CPW are chosen so as to obtain an impedance of 50Ω . Part II is the transition region working as a mode converter and an impedance transformer to







FIGURE 3. The layout of the (a) convention SSPP TL. (b) designed SSPP TL.

connect Part I and Part III. Part III is the SSPP transmission waveguide. The dimension parameters of the conventional and designed SSPP TLs are set as follows: $l_{s1} = l_{s2} = 7$, $w_{s1} = 2$, $w_{s2} = 0.15$, $w_m = 2.45$, $w_p = 0.14$, d = 0.2, $w_1 = 8$, $l_1 = 7$, L = 100, W = 60 (all dimensions are in mm).

To validate the lower asymptotic frequency of the proposed SSPP TL, Figure 4 compares the simulated *S*-parameters between the conventional and proposed SSPP TLs. It can be observed that the asymptotic frequencies of the conventional and proposed SSPP TL are 1.83 GHz and 0.94 GHz, which indicates that the designed SSPP TL exhibits stronger field confinements.

In order to visualize such strong field confinements, Figure 5 plots the normalized field distribution of the unloaded and loaded SSPP TL on the same cross section (x-z plane) at 1 GHz, respectively. It can be observed that the field is confined tighter near the designed SSPP TL than the conventional one. In addition, if the confinement region is defined as from the maximum electric field strength to 1/e, then the confinement region is reduced by about 37.82% from 3.94 mm to 2.45 mm, which indicates that the designed SSPP TL exhibits stronger field confinements.

We also fabricated the designed SSPP TL, and its top and bottom views are shown in Figures 6(a) and (b), respectively. Figure 7 depicts the measured and simulated S-parameters. It can be easily observed that the measured results are in accordance with the simulated ones, and the -3 dB asymptotic frequency is only 0.95 GHz, implying its ultra strong ability of field confinement. The fabrication tolerance and measurement environment are the main causes of the disparity.

It should also be noticed that the size of the proposed SSPP TL unit cell is only $10 \text{ mm} \times 20.93 \text{ mm}$, corresponding to $0.0021 \lambda_a^2 (0.032\lambda_a \times 0.066\lambda_a)$, where λ_a is the free space wavelength at the asymptotic frequency. For comparison, performances of the proposed SSPP TL and some previous SSPP TLs are listed

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FIGURE 4. The simulated S-parameters comparison between the conventional and proposed SSPP TLs.



FIGURE 5. The normalized electric field of conventional and proposed SSPP TL.



FIGURE 6. The view of the fabricated SSPP TL from (a) top view. (b) bottom view.



FIGURE 7. Simulated and measured S-parameters.

Ref.	f_a (GHz)	unit size (λ_a^2)	overall size (λ_a^2)
6	8.1	0.015~(0.14 imes 0.11)	$6.502 (5.40 \times 1.20)$
7	5.8	0.010~(0.10 imes 0.10)	N.A.
12	8.9	0.019~(0.12 imes 0.16)	0.418~(2.61 imes 0.16)
13	1.67	0.007~(0.06 imes 0.11)	0.042~(0.38 imes 0.11)
This work	0.95	0.002 (0.03×0.07)	0.022 (0.32×0.7)

TABLE 1. Size performance of previous works and this work.

 f_a : the asymptotic frequency, λ_a : the wavelength at f_a .

in Table 1 in terms of asymptotic frequency f_a , unit size, and overall size. It can be observed that the proposed SSPP TL exhibits more compact unit size and overall size.

4. CONCLUSION

In this article, a novel CPW SSPP TL is proposed. The analyses based on the E.C model reveal that the loaded SSPP exhibits a lower asymptotic frequency and tighter field confinement due to the capacitance brought by the extra flipper structures. It is also found that the field confinement of the loaded unit can be flexibly controlled. The experimental results and theoretical analyses agree well and validate that the loaded SSPP TL exhibits stronger filed confinements.

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