# Ultra Compact Flexible Monopole Antennas for Tri-Band Applications

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Abstract—Two novel ultra-compact flexible tri-band antennas with coplanar waveguide (CPW) feed and asymmetric coplanar strip (ACS) feed arrangements are presented in this paper. These antennas are fabricated on an extremely thin substrate with dielectric constant ( $\varepsilon_r$ ) 3.5 and loss tangent (tan  $\delta$ ) 0.027. The folded geometry of the antennas contributes to the size reduction. While the CPW-fed tri-band antenna (19 mm × 19 mm) exhibits bandwidth of 130 MHz, 600 MHz, and 1550 MHz in the lower, middle, and upper frequency bands, the ACS-fed tri-band antenna (19.5 mm × 15 mm) exhibits 80 MHz, 600 MHz, and 2220 MHz bandwidth, respectively. Design equations are developed, and an appropriate circuit model is recommended. The performance of the antenna is investigated for various bending conditions. Simple geometry, compactness, flexibility, and stability under bending conditions over multiband make these incredibly thin antennas quite appealing for ISM 2.4/5.2 GHz, Wi-Fi 2.4/5 GHz, WLAN 2.4/5.2/5.8 GHz and WiMAX 3.5/5.5 GHz applications.

# 1. INTRODUCTION

Versatility and miniaturization are the key features of emerging electronic gadgets in the present world. Multiband antennas on flexible substrates are popular for such applications. Among multiband antennas, tri-band antennas are well known [1–9]. Tri-band antennas are designed to operate in three different frequency bands. The popular bands for these applications are DCS 1.89 GHz, LTE (1.96–2.22 GHz), 5G mid band (2.35–2.5 GHz/3.18–3.82 GHz/4.15–5.42 GHz), ISM (2.4–2.48 GHz/5.2–6 GHz), WLAN (2.4–2.484 GHz/5.15–5.35 GHz/5.725–5.825 GHz), and WiMAX (3.4–3.6 GHz/5.28–5.85 GHz) [4–8].

Compactness and flexibility are important attributes of antennas. The compactness of an antenna is mainly achieved by the proper selection of antenna geometry. A flexible substrate leads to the flexibility of any antenna. Different flexible materials for numerous applications have been reported, Rogers R04835T [1], polyamide [2], polyimide [3], Dupont [10, 11], kapton polyimide [12], polyethylene terephthalate (PET) [13], RT-5880 [14] to name a few. Octagonal patch [1], slotted patch [2, 9], triannular square ring [3], triangular monopole [4], and fractal geometry [5] are the different multiband antennas proposed on flexible substrates. Microstrip, coplanar waveguide (CPW) coaxial, aperture coupled, proximity coupled, and asymmetric coplanar strip (ACS) are the various feeding techniques employed for these antennas. The authors have reported compact CPW and ACS fed dual band antennas on flexible Dupont substrates [10, 11].

This paper presents two novel ultra-compact flexible tri-band antennas with CPW feed and ACS feed designed on extremely thin flexible substrates. Folded geometry is used in this work to reduce the overall antenna size. Easy fabrication process is one of the attractive features of the proposed antennas. Compactness and flexibility of the antennas make them suitable where bending situations

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are encountered. Therefore, detailed bending investigations are conducted. The proposed antennas are simulated, fabricated, and tested under experimental conditions to validate their performance.

# 2. ANTENNA STRUCTURE AND DESIGN

The design of compact coplanar waveguide (CPW) and asymmetric coplanar strip (ACS) fed tri-band flexible monopole antennas (TBFMAs) is explained in this section.

### 2.1. Compact CPW-Fed Tri-Band Flexible Monopole Antenna (TBFMA)

The proposed compact coplanar waveguide (CPW) fed tri-band flexible monopole antenna (TBFMA) comprises three resonant sections catering to the different application bands. Figs. 1(a)-(d) show the development phases of the proposed CPW-fed TBFMA. The corresponding reflection coefficient plot  $(S_{11} \text{ in dB})$  is shown in Fig. 1(e). The 19 mm  $\times$  19 mm antenna is designed on an extremely thin Dupont substrate with height (h) 130  $\mu$ m, dielectric constant ( $\varepsilon_r$ )3.5, and loss tangent (tan  $\delta$ )0.027. The simulations are done using Computer Simulation Technology (CST) software. Size miniaturization of monopole antennas at low frequencies is the main motivation of the proposed design. This is accomplished by folding a straight monopole to create a meandered antenna (P-1) formed by strip  $d_s$  and folded strips  $d_2 + d_3 + d_4 + d_5 + d_6$ , as shown in Fig. 1(a), obtaining a resonance at 2.72 GHz in the lower resonant band. In order to achieve the upper resonance in the 5.5 GHz application band, the strip  $d_1$  is attached to P-1, resulting in an inverted L formed by  $d_s$  and  $d_1$ . As a result, an additional resonance at 5.75 GHz is achieved; the developed antenna (P-2) is presented in Fig. 1(b). The strips  $d_7 + d_8 + d_9$  added to P-2, resulting in a C-shaped structure formed by  $d_m$  and  $d_7 + d_8 + d_9$ , produce a resonance in the middle band at 3.62 GHz. The modified geometry (P-3) is shown in Fig. 1(c). The narrow slit introduced in P-3 results in the final geometry (P-4), as shown in Fig. 1(d). This helps to tune out the unwanted resonance. In the course of evolution, a lower shift in resonances is observed as



**Figure 1.** (a)–(d) Development phases of the proposed CPW fed TBFMA ( $\varepsilon_r = 3.5$ ,  $h = 130 \,\mu\text{m}$ ,  $W = 19 \,\text{mm}$ ,  $L = 19 \,\text{mm}$ ,  $d_s = 6.2 \,\text{mm}$ ,  $d_m = 1.7 \,\text{mm}$ ,  $L_g = 2.8 \,\text{mm}$ ,  $W_g = 7.8 \,\text{mm}$ ,  $d_f = 9 \,\text{mm}$ ,  $W_f = 4 \,\text{mm}$ ,  $W_s = 1.5 \,\text{mm}$ ,  $d_1 = 7 \,\text{mm}$ ,  $d_2 = 4.2 \,\text{mm}$ ,  $d_3 = 4.5 \,\text{mm}$ ,  $d_4 = 13.7 \,\text{mm}$ ,  $d_5 = 4.5 \,\text{mm}$ ,  $d_6 = 15.2 \,\text{mm}$ ,  $d_7 = 6.5 \,\text{mm}$ ,  $d_8 = 14 \,\text{mm}$ ,  $d_9 = 2.5 \,\text{mm}$ ,  $g_p = 0.2 \,\text{mm}$ ,  $s_t = 0.3 \,\text{mm}$ ,  $a_1 = 1.5 \,\text{mm}$ ,  $a_2 = 1.5 \,\text{mm}$ ). (e) Reflection coefficient (dB) plot of antennas in the development phases.



**Figure 2.** (a) CPW fed TBFMA geometry. (b) Circuit model of the antenna developed using ADS. (c) Corresponding reflection coefficient plot.

strips are subsequently added to the folded antenna (P-1). The dimensions of the strips are optimized to obtain the resonances in the required bands. The developed antenna (Fig. 2(a)) operates in three frequency bands 2.4 to 2.48 GHz (80 MHz), 3.37–3.77 GHz (400 MHz), and 5.1– to 7.7 GHz (2600 MHz), resonating at 2.45 GHz, 3.57 GHz, and 5.59 GHz, respectively. The design equations are developed from parametric analysis as detailed below.

Figure 2(b) illustrates the circuit model for the proposed CPW-fed TBFMA. The 50  $\Omega$  CPW feed, folded monopole, inverted L-shaped and C-shaped structure contributing to various resonances are modelled in the proposed circuit. The elements  $R_S$  (50  $\Omega$ ),  $L_S$  (0.165 nH), and  $C_S$  (0.5 pF) represent the CPW feed. The T-shaped circuit elements  $L_1$  (1.5 nH) and  $C_1$  (0.61 pF), denoting the folded strip  $(d_S+d_2+d_3+d_4+d_5+d_6=0.58\lambda)$ , provide the lower resonance at 2.44 GHz ( $f_1$ ); the circuit elements  $C_2$  (0.115 pF) and  $L_2$  (18.5 nH), denoting the C-shaped open stub  $(d_m+d_7+d_8+d_9=0.28\lambda)$ , contribute to the middle resonance at 3.58 GHz ( $f_2$ ); and the circuit elements  $L_3$  (3.93 nH) and  $C_3$  (0.38 pF), denoting the inverted L-shaped open stub  $(d_S+d_1=0.242\lambda)$ , contribute to the upper resonance at 5.6 GHz ( $f_3$ ). Fig. 2(c) shows the reflection coefficient plot ( $S_{11}$  in dB) of the circuit simulated using Advanced Design System (ADS) software. The plot clearly indicates the three resonant bands.

The impact of antenna dimensions on different antenna characteristics has been studied by parametric analysis. It is found that the ground dimensions  $(L_g \text{ and } W_g)$  mainly affect the impedance. To achieve the intended performance,  $L_g \times W_g$  of the proposed CPW-fed TBFMA is optimized to  $2.8 \text{ mm} \times 7.8 \text{ mm}$ . The design equations are:

$$d_{t1} = -5.685f_1 - 0.126\varepsilon_r - 8.32h + 63; \tag{1}$$

here 
$$d_{t1} = d_S + d_2 + d_3 + d_4 + d_5 + d_6$$

$$d_{t2} = -5.93f_2 - 0.2\varepsilon_r - 11.708h + 48.2;$$
where  $d_{t2} = d_m + d_7 + d_8 + d_9$ 
(2)

$$d_{t3} = -3.18f_3 - 0.19\varepsilon_r - 9.31h + 32.9;$$
(3)

where 
$$d_{t3} = d_S + d_1$$

W

h is the height of substrate in mm, and  $\varepsilon_r$  is the dielectric constant of the material. The lengths of the

individual strips of the folded monopole which make up  $d_{t1}$  are limited by the dimensions of the gaps  $a_1, a_2$  defined by the following equations.

$$a_1 = -3.08h - 0.056\varepsilon_r - 2.334f_1 + 7.84 \tag{4}$$

$$a_2 = -4.15h - 0.069\varepsilon_r - 2.628f_1 + 8.72\tag{5}$$

Equations (1)–(5) are valid for  $h \leq 0.2 \text{ mm}$  and  $2.2 \leq \varepsilon_r \leq 4.4$ . The resonant length is calculated for various substrate heights (*h*), dielectric constant ( $\varepsilon_r$ ), and frequencies to validate the above equations. Table 1 shows the % error in resonant length of the proposed CPW-fed TBFMA. The observed error is less than 2%.

Substrate		Frequencies (GHz)			Resonant les Equation			ngth (mm) Simulation			Error (%)		
$\varepsilon_r$	h (mm)	$f_1$	$f_2$	$f_3$	$d_{t1}$	$d_{t2}$	$d_{t3}$	$d_{t1}$	$d_{t2}$	$d_{t3}$	$d_{t1}$	$d_{t2}$	$d_{t3}$
4.4	0.025	2.6	3.6	5.5	47.36	25.4	14.3	48.3	25.7	14.2	1.9	1.2	0.7
2.2	0.05	2.7	3.7	6.3	46.86	25.2	12	47.3	24.7	12.2	0.93	1.9	1.63
Proposed CPW fed TBFMA													
3.5	0.13	2.45	3.57	5.59	47.54	24.8	13.3	48.3	24.7	13.2	1.57	0.4	0.05

Table 1. Error in resonant length of proposed CPW fed TBFMA.

# 2.2. Compact ACS Fed Tri-Band Flexible Monopole Antenna (TBFMA)

Asymmetric coplanar strip (ACS) feeding is another technique used in compact planar antenna design. The asymmetrical nature of the structure contributes to size miniaturization. Figs. 3(a)-(c) show the development phases of the proposed ACS-fed TBFMA. The corresponding reflection coefficient plot is



**Figure 3.** (a)–(c) Development phases of the proposed ACS-fed TBFMA ( $\varepsilon r = 3.5$ ,  $h = 50 \,\mu\text{m}$ ,  $W = 19.5 \,\text{mm}$ ,  $L = 15 \,\text{mm}$ ,  $d_s = 2 \,\text{mm}$ ,  $L_g = 5 \,\text{mm}$ ,  $W_g = 5.5 \,\text{mm}$ ,  $d_f = 7 \,\text{mm}$ ,  $W_f = 4 \,\text{mm}$ ,  $d_1 = 12.5 \,\text{mm}$ ,  $d_2 = 1.3 \,\text{mm}$ ,  $d_3 = 4.8 \,\text{mm}$ ,  $d_4 = 16.3 \,\text{mm}$ ,  $d_5 = 4.85 \,\text{mm}$ ,  $d_6 = 17 \,\text{mm}$ ,  $d_7 = 13.9 \,\text{mm}$ ,  $d_8 = 8.7 \,\text{mm}$ ,  $g_p = 0.3 \,\text{mm}$ ,  $d_m = 0.5 \,\text{mm}$ ,  $p = 0.5 \,\text{mm}$ ,  $a_1 = 2 \,\text{mm}$ ,  $a_2 = 2.3 \,\text{mm}$ ). (d) reflection coefficient plot (dB) plot of antennas in the development phases.

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shown in Fig. 3(d). The 19.5 mm × 15 mm antenna is designed on an extremely thin Dupont substrate with height (h) 50 µm, dielectric constant ( $\varepsilon_r$ ) of 3.5, and loss tangent (tan  $\delta$ ) of 0.027. To miniaturize the monopole antennas, the straight monopole is folded to create a meandered geometry (P-1) formed by strip  $d_s$  and folded strips  $d_2 + d_3 + d_4 + d_5 + d_6$ , as presented in Fig. 3(a), and a resonance is obtained at 2.64 GHz in the lower resonant band. In order to achieve the upper resonance in the 5 GHz application band, strip  $d_1$  is attached to P-1, resulting in an inverted L formed by  $d_s$  and  $d_1$ . Thus an additional resonance at 5.26 GHz is achieved, and the modified structure (P-2) is shown in Fig. 3(b). The strips  $d_7 + d_8$  added to P-2, resulting in a L-shaped structure formed by  $d_m$  and  $d_7 + d_8$ , produce an additional resonance in the middle band at 3.5 GHz. The final geometry (p-3) is shown in Fig. 3(c). In the course of evolution, a shift in resonances is observed as strips are subsequently added to the folded antenna (P-1). The dimensions of the strips are optimized to obtain the resonances in the required bands. The asymmetric ground and folded geometry are responsible for the compactness. The developed antenna (Fig. 4(a)) operates in three frequency bands 2.38–2.43 GHz (50 MHz), 3.3–3.65 GHz (350 MHz), and 4.76–7.4 GHz (2640 MHz), resonating at 2.4 GHz, 3.5 GHz, and 5.3 GHz, respectively. The design equations are developed from parametric analysis as detailed below.



**Figure 4.** (a) ACS-fed TBFMA geometry. (b) Circuit model of the proposed antenna developed using ADS. (c) Corresponding reflection coefficient plot.

Figure 4(b) depicts the circuit model for the proposed ACS-fed TBFMA. The 50  $\Omega$  ACS feed, folded monopole, L-shaped and inverted L-shaped structure contributing to various resonances are modelled in the proposed circuit. The elements  $R_S$  (50  $\Omega$ ),  $L_S$  (0.165 nH), and  $C_S$  (0.5 pF) represent the ACS feed. The T-shaped circuit elements  $L_1$  (1.51 nH) and  $C_1$  (0.62 pF), denoting the folded strip  $(d_S + d_2 + d_3 + d_4 + d_5 + d_6 = 0.55\lambda)$ , provide the lower resonance at 2.4 GHz ( $f_1$ ); the circuit elements  $C_2$  (0.118 pF) and  $L_2$  (18.5 nH), denoting the L-shaped open stub  $(d_m + d_7 + d_8 = 0.269\lambda)$ , provide middle resonance at 3.5 GHz ( $f_2$ ); and the circuit elements  $L_3$  (4.5 nH) and  $C_3$  (0.38 pF), denoting the inverted L-shaped open stub  $(d_S + d_1 = 0.28\lambda)$ , contribute to the upper resonance at 5.38 GHz ( $f_3$ ). Fig. 4(c) displays the reflection coefficient plot ( $S_{11}$  in dB) of the circuit simulated using ADS software. The plot clearly indicates the three resonant bands.

The impact of antenna dimensions on the different antenna characteristics has been studied by parametric analysis. To achieve the intended performance,  $L_g$  and  $W_g$  of the proposed ACS-fed TBFMA

are optimized to 5.5 mm and 5 mm. The design equations are:

W

$$d_{t1} = -12.5f_1 - 0.496\varepsilon_r - 27.15h + 79.6; \tag{6}$$

here 
$$d_{t1} = d_S + d_2 + d_3 + d_4 + d_5 + d_6$$
  
 $d_{t2} = -9.34f_2 - 0.43\varepsilon_r - 19.43h + 58.3;$ 
(7)

where 
$$d_{t2} = d_m + d_7 + d_8$$

$$d_{t3} = -1.062f_3 - 0.027\varepsilon_r - 1.107h + 20.29;$$
(8)
where  $d_{t3} = d_S + d_1$ 

*h* is the height of substrate in mm, and  $\varepsilon_r$  is the dielectric constant of the substrate material. The lengths of the individual strips of the folded monopole which make up  $d_{t1}$  are limited by the dimensions of the gaps  $a_1$ ,  $a_2$  defined by the following equations.

$$a_1 = -5.6h - 0.111\varepsilon_r - 2.787f_1 + 9.384 \tag{9}$$

$$a_2 = -4.037h - 0.08\varepsilon_r - 2.04f_1 + 7.676 \tag{10}$$

Equations (6)–(10) are valid for  $h \leq 0.2 \text{ mm}$  and  $2.2 \leq \varepsilon_r \leq 4.4$ . The resonant length is calculated for various substrate heights (*h*), dielectric constant ( $\varepsilon_r$ ), and frequencies to validate the above equations. The % error in resonant length of the ACS-fed TBFMA is presented in Table 2. The observed error is less than 2%.

Substrate		Frequencies		Resonant length (mm)					$\mathbf{Frror}(\%)$				
		(GHz)			Equation			Simulation					
$\varepsilon_r$	h (mm)	$f_1$	$f_2$	$f_3$	$d_{t1}$	$d_{t2}$	$d_{t3}$	$d_{t1}$	$d_{t2}$	$d_{t3}$	$d_{t1}$	$d_{t2}$	$d_{t3}$
4.4	0.025	2.49	3.6	5.25	45.67	21.83	14.56	45.25	22.1	14.6	0.9	1.22	0.27
2.2	0.13	2.37	3.54	5.4	45.35	21.76	14.39	45.25	22.1	14.4	0.22	1.53	0.69
Proposed ACS fed TBFMA													
3.5	0.05	2.4	3.5	5.3	46.6	23.15	14.52	46.25	23.1	14.5	0.75	0.22	0.14

Table 2. % Error in resonant length of ACS-fed TBFMA.

### 3. RESULTS AND DISCUSSION

The parameters described in the previous section are used to build the antennas on a flexible DuPont substrate. Fabricated prototypes of the CPW-fed and ACS-fed TBFMAs are shown in Figs. 5(a) and 5(c). Experiments were done using Antritzu MS46122B Vector Network Analyzer (VNA). Figs. 5(b) and 5(d) show the reflection coefficient plots of the proposed CPW- and ACS-fed TBFMAs. The measured bandwidth of the CPW-fed TBFMA is 130 MHz (2.35 to 2.48 GHz) in the lower band, 600 MHz (3.1 to 3.7 GHz) in the middle band, and 1550 MHz (5.5 to 7.05 GHz) in the upper band. The measured bandwidth of the ACS-fed TBFMA is 80 MHz (2.39 to 2.47 GHz) in the lower band, 600 MHz (3 to 3.6 GHz) in the middle band, and 2220 MHz (4.78 to 7 GHz) in the upper band. These results reasonably agree with the simulated results presented in Figs. 1(e) and 3(d). ISM (2.4–2.48 GHz/5.2–6 GHz), WLAN (2.4–2.484 GHz/5.15–5.35 GHz/5.725–5.825 GHz) and WiMAX (3.4–3.6 GHz/5.28–5.85 GHz) communication bands are covered by the lower, middle, and upper bands.

Figures 6(a)-(c) show the surface current plots of CPW-fed TBFMA at 2.45 GHz, 3.5 GHz, and 5.5 GHz. The resonance at 2.45 GHz shown in Fig. 6(a) is mainly due to the Z-shaped monopole of length  $d_{t1}$  ( $d_S+d_2+d_3+d_4+d_5+d_6$ ). However, it is observed that the current through the C-shaped path



**Figure 5.** (a) Prototype of CPW-fed TBFMA (b) reflection coefficient plot of CPW-fed TBFMA (c) prototype of ACS-fed TBFMA (d) reflection coefficient plot of ACS-fed TBFMA.

length  $d_{t2}(d_m + d_7 + d_8 + d_9)$  also contributes to this. The effective resonance length  $(d_{t1})$  at 2.45 GHz is  $0.47\lambda_{d1}$ , and  $d_{t2}$  is  $0.24\lambda_{d1}$ , where  $\lambda_{d1}$  is the effective wavelength at  $f_1$ , calculated as follows [15, 16];

$$\lambda_d = \frac{c}{f\sqrt{\varepsilon_{efft \cdot r}}} \tag{11}$$

$$\varepsilon_{efft \cdot r} = \varepsilon_{efft} - \frac{\varepsilon_{efft} - 1}{\frac{(m-n)/2}{0.7r} \cdot \frac{K(k)}{K'(k)} + 1}$$
(12)

$$\varepsilon_{efft} = 1 + \frac{\varepsilon_r - 1}{2} \cdot \frac{K(k')K(k_p)}{K(k)K(k'_p)}$$
(13)

$$k_p = \frac{\sinh\left(\frac{\pi n_r}{4h}\right)}{\sinh\left(\frac{\pi m_r}{4h}\right)} \tag{14}$$

$$n_r = n + \frac{1.25r}{\pi} \left[ 1 + \ln\left(\frac{4\pi n}{r}\right) \right] \tag{15}$$

$$m_r = m - \frac{1.25r}{\pi} \left[ 1 + \ln\left(\frac{4\pi n}{r}\right) \right] \tag{16}$$

where n is the feed width, r the conductor thickness,  $\varepsilon_{efft}$  the effective dielectric constant,  $m = n + 2g_p$ 

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Figure 6. Surface current plots of the CPW-fed TBFMA at (a) 2.45 GHz, (b) 3.57 GHz, (c) 5.5 GHz, and the ACS-fed TBFMA at (d) 2.4 GHz, (e) 3.5 GHz, (f) 5.3 GHz.

and  $k = \frac{n}{m}$ .

As seen in Fig. 6(b), the resonance at 3.57 GHz is due to the current path  $d_m$ ,  $d_7$ ,  $d_8$ , and  $d_9$  in the C-shaped strip. The effective resonance length  $(d_{t2})$  is  $0.35\lambda_{d2}$ . The inverted L strip makes up most of the contribution at 5.5 GHz. The current path  $d_s$  and  $d_1$  is shown in Fig. 6(c), and corresponding length  $(d_{t3})$  is  $0.29\lambda_{d3}$ .

Figures 6(d)–(f) show the surface current plots of ACS-fed TBFMA at 2.4 GHz, 3.5 GHz, and 5.3 GHz. The resonance at 2.4 GHz shown in Fig. 6(d) is mainly due to the Z-shaped monopole of length  $d_{t1}$  ( $d_S + d_2 + d_3 + d_4 + d_5 + d_6$ ). However, it is observed that the current through the L-shaped path length  $d_{t2}$  ( $d_m + d_7 + d_8$ ) also contributes to this. The effective resonance length ( $d_{t1}$ ) at 2.4 GHz is 0.407 $\lambda_{d1}$ , and  $d_{t2}$  is  $0.2\lambda_{d1}$ , where  $\lambda_{d1}$  is the effective wavelength at  $f_1$ , calculated as follows [15, 16];

$$\lambda_d = \frac{c}{f\sqrt{\varepsilon_{efft}}} \tag{17}$$

$$\varepsilon_{efft} = 1 + t(\varepsilon_r - 1) \tag{18}$$

$$t = \frac{K(k_r)}{K'(k_r)} \frac{K'(k_q)}{K(k_q)} \tag{19}$$

$$k_r = \sqrt{\frac{\sinh(\pi n/2h)e^{-\pi g_p/2h}}{\sinh(\pi (n+g_p)/2h)}}$$
(20)

$$k_q = \sqrt{\frac{n}{n+g_p}} \tag{21}$$

where n is the feed width, and  $\varepsilon_{efft}$  is the effective dielectric constant. As seen in Fig. 6(e), the resonance at 3.5 GHz is due to the current path  $d_m$ ,  $d_7$ , and  $d_8$  in the L-shaped strip. The effective resonance length  $(d_{t2})$  is  $0.296\lambda_{d2}$ . The inverted L strip  $d_s$  and  $d_1$  makes up most of the contribution at 5.3 GHz. The current path is shown in Fig. 6(f), and corresponding length  $(d_{t3})$  is  $0.28\lambda_{d3}$ .

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The measured E(YZ) and H(XZ) plane 2D patterns of the proposed CPW-fed TBFMA and ACS-fed TBFMAs are shown in Figs. 7(a)–(c) and 7(d)–(f). The 3D patterns of the proposed CPW-fed and ACS-fed TBFMAs shown in Fig. 8 were measured using EMSCAN — RFXpert. Measured average gains of the proposed CPW-fed TBFMA in lower, middle, and upper frequency bands are 0.5 dBi, 1.1 dBi, and 2.5 dBi. The corresponding average gains of the ACS-fed TBFMA are 0.9 dBi, 1.8 dBi, and 5 dBi.



**Figure 7.** Measured E(YZ) and H(XZ) plane 2D patterns of the CPW-fed TBFMA at (a) 2.45 GHz, (b) 3.5 GHz, (c) 5.5 GHz, and the ACS-fed TBFMA at (d) 2.4 GHz, (e) 3.5 GHz, (f) 5.3 GHz.



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**Figure 8.** Measured 3D patterns of the CPW-fed TBFMA in XZ plane at (a) 2.45 GHz, (b) 3.5 GHz, (c) 5.5 GHz, and the ACS-fed TBFMA in XZ plane at (d) 2.4 GHz, (e) 3.5 GHz, (f) 5.3 GHz, (g) 3D pattern measurement set up.

# 4. FLEXIBILITY STUDIES

The flexibility of the substrate permits the TBFMA to be incorporated into numerous smart devices in a bent condition. The performance of the proposed antennas is investigated in various bending scenarios by bending the TBFMA on air cylindrical tubes with different radii. Figs. 9(a)–(b) show the simulated  $S_{11}$  (dB) of the CPW-fed TBFMA (XZ plane) under inward and outward bending on different radii cylinders. Figs. 9(c)–(d) show the simulated  $S_{11}$  (dB) of the ACS-fed TBFMA (XZ plane) under inward and outward bending on different radii cylinders. The results demonstrate that the ACS-fed TBFMA is less susceptible to bending than the CPW-fed TBFMA, as a result of its uniplanar nature

<b>Table 3.</b> Comparison of various multi-band antenna	Table 3.	Comparison	of various	multi-band	antennas
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Ref./year	Dielectric	Operating Bands (GHz)	Overall dimension (mm <sup>2</sup> )	Flexibility					
[1]/2020	ROGERS RO4835T ( $\varepsilon_r = 3.52$ , tan $\delta = 0.003$ )	2.35-2.5/3.18-3.82/4.15-5.42	$25 \times 32$	Yes					
[2]/2020	Flexible Polyamide ( $\varepsilon_r = 4.3$ , $\tan \delta = 0.004$ )	2.33-2.47/3.68-3.92/5.38-5.75	$24 \times 19$	Yes					
[3]/2021	Polyimide film ( $\varepsilon_r = 3.5$ , tan $\delta = 0.004$ )	2.28-2.51/5.2-6/5-4	$30 \times 30$	Yes					
[5]/2021	Fr4 $(\varepsilon_r = 4.4, \tan \delta = 0.02)$	1.96-2.22/3.51-3.91/4.78-5.26	$37 \times 28$	No					
[4]/2022	Fr4 $(\varepsilon_r = 4.4, \tan \delta = 0.02)$	2.37-2.51/3.34-3.71/4.6-6.4	$20 \times 15$	No					
Proposed TBFMA									
CPW fed	$\overline{ egin{array}{c}  ext{Dupont} \ (arepsilon_{ ext{r}}=3.5, ext{tan}\delta=\!0.027) \end{array} }$	2.35 – 2.48 / 3.1 – 3.7 / 5.5 – 7.05	19  imes 19	Yes					
ACS fed	$egin{array}{c}  ext{Dupont} \ (arepsilon_{ ext{r}}=3.5, ext{tan}\delta$ =0.027)	2.39 - 2.47/3 - 3.6/4.78 - 7	19.5 imes15	Yes					



**Figure 9.** Flexibility studies: simulated  $S_{11}$  (dB) of the CPW fed TBFMA (XZ plane) under (a) inward bending, (b) outward bending, and the ACS fed TBFMA under (c) inward bending, (d) outward bending.



**Figure 10.** Flexibility studies: measured  $S_{11}$  (dB) of the TBFMA bending on cylindrical tubes (radius: R and  $\varepsilon_r$ : 4). (a) CPW fed TBFMA. (b) ACS fed TBFMA.

and asymmetrical design. Fig. 10 shows the measured  $S_{11}$  (dB) plot of the proposed TBFMA bending on cylindrical tubes with radius R and dielectric constant ( $\varepsilon_r$ ) : 4. The findings prove that the antennas retain their tri-band characteristics regardless of the radius of the bend.

Table 3 compares the proposed TBFMA with existing multi-band antennas. The compactness of the proposed antennas is evident from the table.

## 5. CONCLUSION

The tri-band flexible monopole antennas with coplanar waveguide (CPW) feed and asymmetric coplanar strip (ACS) feed presented in this paper are ultra compact. The extremely thin Dupont material ( $\varepsilon_r$  : 3.5 and tan  $\delta$  : 0.027) used as the substrate makes the antenna flexible. A simple geometry with folded structure enables easy fabrication of the antenna. The CPW-fed antenna (19 mm × 19 mm) exhibits bandwidths of 130 MHz, 600 MHz, and 1550 MHz in the lower, middle, and upper frequency bands. The ACS-fed antenna (19.5 mm × 15 mm) exhibits bandwidths of 80 MHz, 600 MHz, and 2220 MHz in the lower, middle, and upper frequency bands, catering to ISM 2.4/5.2 GHz, Wi-Fi 2.4/5 GHz, WLAN 2.4/5.2/5.8 GHz, and WiMAX 3.5/5.5 GHz. The circuit model and design equations presented in this paper give a good theoretical support for the performance evaluation of these proposed antennas. The antennas are found to maintain their performance under different bending conditions. Simple geometry, compactness, excellent flexibility, and stability under bending conditions over multiband make these extremely thin antennas quite attractive.

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