

# A Compact Negative Group Delay Circuit Topology Based on Asymmetric Coplanar Striplines and Double-Sided Parallel Striplines

Zhongbao Wang\*, Yu Bai, Yuwei Meng, Shaojun Fang, and Hongmei Liu

**Abstract**—An innovative negative group delay (NGD) circuit topology based on asymmetric coplanar striplines (ACPSs) and double-sided parallel striplines (DSPSs) is proposed. The original NGD circuit topology consists of two sections of ACPS, one section of open-circuited DSPS, a connecting hole, and a group of grounding holes. The NGD characteristic is achieved by the open-circuited DSPSs combined with the connecting hole. To verify the proposed NGD circuit topology, a prototype is designed, fabricated, and measured. From the measured results, an NGD time of  $-2.42$  ns at the center frequency of  $1.577$  GHz is obtained with an NGD bandwidth of  $36$  MHz ( $1.561$ – $1.597$  GHz). The insertion loss is less than  $4.75$  dB with the return loss larger than  $11.7$  dB in the NGD band.

## 1. INTRODUCTION

Group delay (GD) distortion is one of the challenging issues in a circuit or system, which may cause the inter-symbol interference of wideband communication systems and the pseudo-range error of global navigation satellite systems (GNSSs). To address these issues, negative group delay circuit (NGDC) has been applied to compensate the GD distortion [1], enhance the bandwidth of analog feedback amplifier [2], increase the efficiency of feed-forward linearization amplifier [3], minimize the beam-squint in phased array antenna [4], realize linear-phase bandpass filter [5], and design wideband phase shifter [6].

Traditional NGDCs are realized by RLC resonators or transmission lines loaded with resistors [7–9]. However, they always have large insertion loss (IL) and require lumped components. Usually, these lumped components only have some standard values, which limit the flexibility of design. To solve this problem, several novel low-loss NGDCs without lumped components have been proposed [10–15]. In [10], a coupled line coupler-based NGDC without requiring resistors was proposed by using the isolated and coupled-accesses connected in a feedback loop through a lossy interconnect line. After that, an NGDC based on a coupling matrix with finite unloaded quality factor resonators was proposed in [11]. Recently, an NGDC was designed by using one section of coupled lines with open- and stub-loaded terminations [12]. In [13], a turtle-shaped NGDC was proposed, which comprised two different-length transmission lines interconnecting two identical coupled lines. In [14], a low-loss NGDC consisted of two identical coupled-lines and three identical transmission lines. In [15], a diakoptics modeling of flying bird-shaped NGDC was developed. However, the use of the coupled-lines made the theoretical analysis of these NGDCs complicated.

In this paper, a compact NGDC topology based on asymmetric coplanar striplines (ACPSs) and double-sided parallel striplines (DSPSs) is proposed. The proposed NGDC is composed of two sections of ACPS, an open-circuited DSPS, a connecting hole, and a group of grounding holes. The negative group delay (NGD) characteristic is achieved by the open-circuited DSPS combined with the connecting hole. The analysis and results of the proposed NGDC are given and discussed.

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## 2. DESIGN OF THE PROPOSED NGDC

Figure 1 shows the proposed NGDC topology, which consists of two ACPSs, an open-circuited DSPS, a connecting hole, and a group of grounding via holes. Two ACPSs connected with input and output ports are printed on the top and bottom sides of a substrate, respectively. The ground planes of ACPSs are connected by a group of via holes. The top and bottom strips of the open-circuited DSPS are connected to the top and bottom ACPSs, respectively. Furthermore, a connecting hole is also connected to the top and bottom strips of the open-circuited DSPS, as shown in Fig. 1. The NGD characteristic of the proposed NGDC is generated by the open-circuited DSPS combined with the connecting hole, which is equivalent to a parallel  $RLC$  resonator in series with input and output ACPSs. Therefore, the NGD time and operation frequency are mainly controlled by changing the length and width of the open-circuited DSPS (i.e., the capacitance and resistance of the parallel  $RLC$  resonator) and the diameter of the connecting hole (i.e., the inductance of the parallel  $RLC$  resonator).

Figure 2 gives the effects of the open-circuited DSPS on the performances of the proposed NGDC. When the length of the open-circuited DSPS  $L_d$  is increased from 23.6 to 24.6 mm, the NGD center frequency is decreased, and NGD absolute value and IL at the center frequency are slightly decreased.

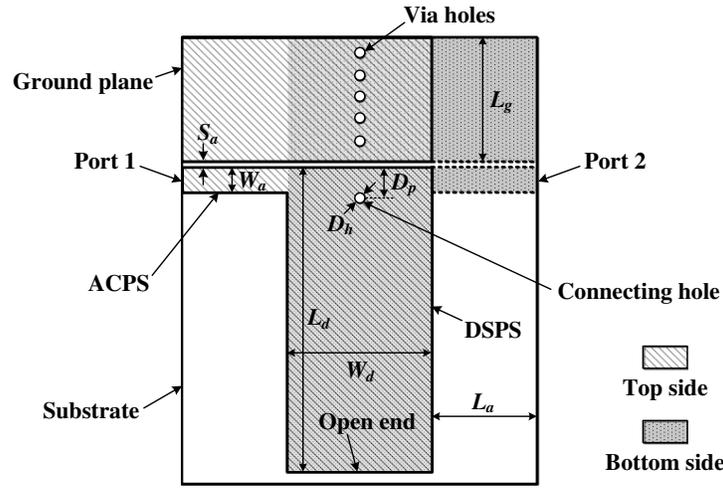


Figure 1. Configuration of the proposed NGDC.

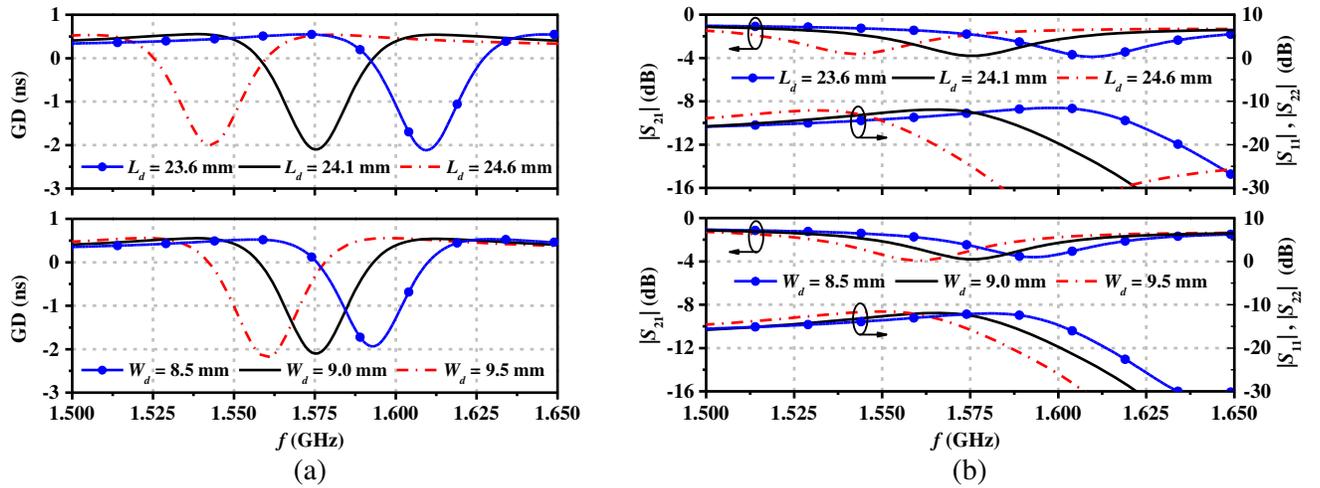


Figure 2. Effect of  $L_d$  and  $W_d$  on the performances of the proposed NGDC. (a) GD. (b)  $S$ -parameters.

Contrary to  $L_d$ , the NGD absolute value and IL at the center frequency are slightly increased by increasing the width of the open-circuited DSPS  $W_d$  from 8.5 to 9.5 mm. Also, the NGD center frequency is decreased by increasing  $W_d$ . Furthermore, the open-circuited DSPS has a slight effect on the  $|S_{11}|$  at the NGD center frequency.

Figure 3 shows the effects of the connecting hole on the performances of the proposed NGDC. When the diameter of the connecting hole  $D_h$  is increased from 0.7 to 1.3 mm, the NGD center frequency is increased. Meanwhile, NGD absolute value and IL at the center frequency are decreased. When  $D_h$  is less than 0.7 mm,  $|S_{11}|$  at the NGD center frequency will be greater than  $-10$  dB. As shown in Fig. 3, when  $D_p$  is increased from 2.5 to 3.5 mm, the NGD center frequency is increased.  $D_p$  has a negligible effect on the NGD absolute value, IL, and  $|S_{11}|$  at the center frequency.

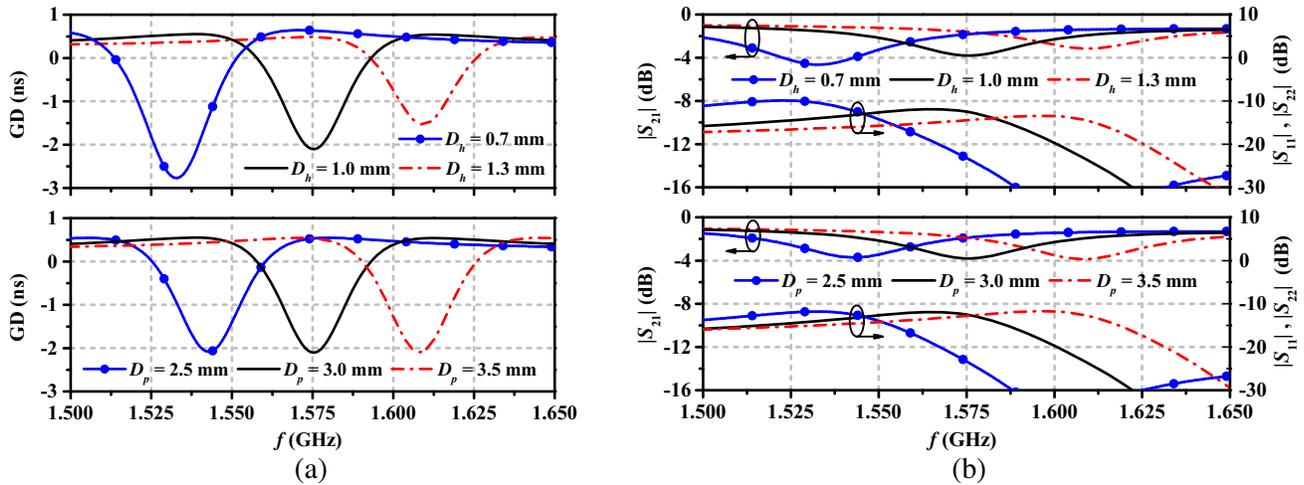


Figure 3. Effect of  $D_h$  and  $D_p$  on the performances of the proposed NGDC. (a) GD. (b)  $S$ -parameters.

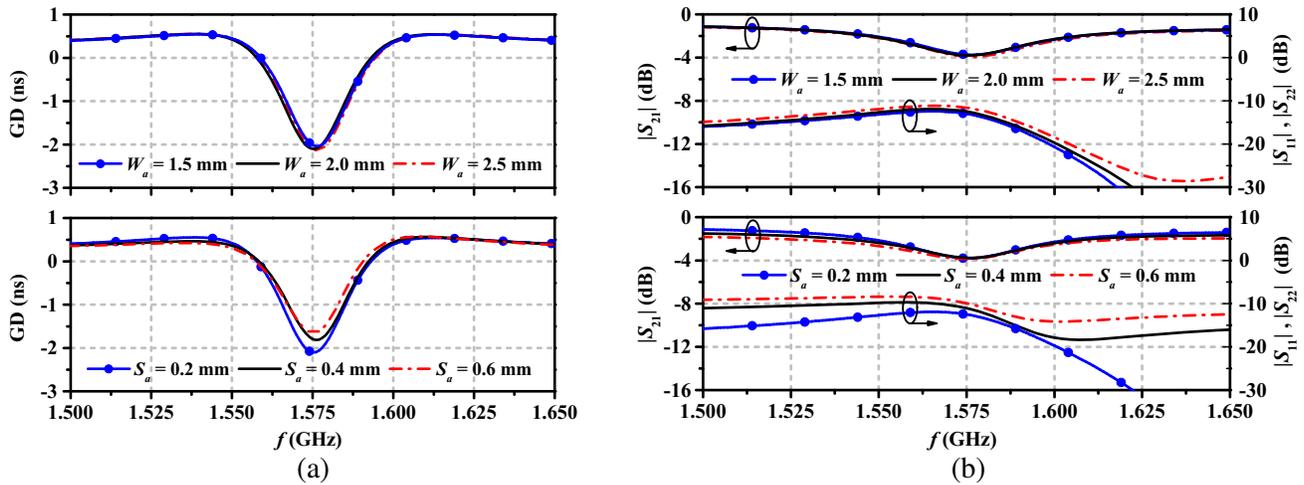


Figure 4. Effect of  $W_a$  and  $S_a$  on the performances of the proposed NGDC. (a) GD. (b)  $S$ -parameters.

Figure 4 gives the effects of ACPS on the performances of the proposed NGDC. When the strip width of the ACPS  $W_a$  is increased from 1.5 to 2.5 mm,  $|S_{11}|$  is degraded with a negligible change of GD and IL. As shown in Fig. 4, when the slot width of ACPS  $S_a$  is increased from 0.2 to 0.6 mm, the NGD absolute value at the center frequency is decreased with degradation of  $|S_{11}|$ . Thus, there is a compromise between impedance matching and fabricating difficulty.

Based on the foregoing analysis, the following procedures are suggested to design the proposed NGDC.

1) Determine the NGD time and center frequency according to the design requirements. Obtain the values of relative dielectric constant  $\epsilon_r$  and thickness  $h$  of the substrate.

2) Select a proper width of DSPS  $W_d$  referring to Fig. 2. Then calculate the length of DSPS  $L_d$  to be about  $\lambda_g/4$ , where the guided wavelength  $\lambda_g$  of DSPS is the same as that of a microstrip line with the substrate thickness  $h/2$  [16].

3) Choose a proper diameter of the connecting hole  $D_h$  based on the desired NGD time (Fig. 3).

4) Select a slot width of ACPS  $S_a$  according to the fabricating technology (Fig. 4).

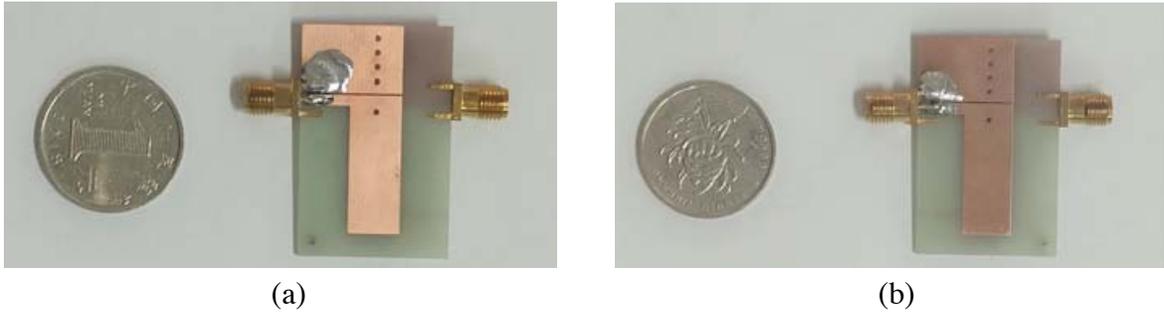
5) Adjust  $S_a$  and  $W_a$  in a full-wave electromagnetic simulator to achieve the impedance matching, referring to Fig. 4.

6) Change  $D_h$  according to Fig. 3 to obtain the desired NGD time.

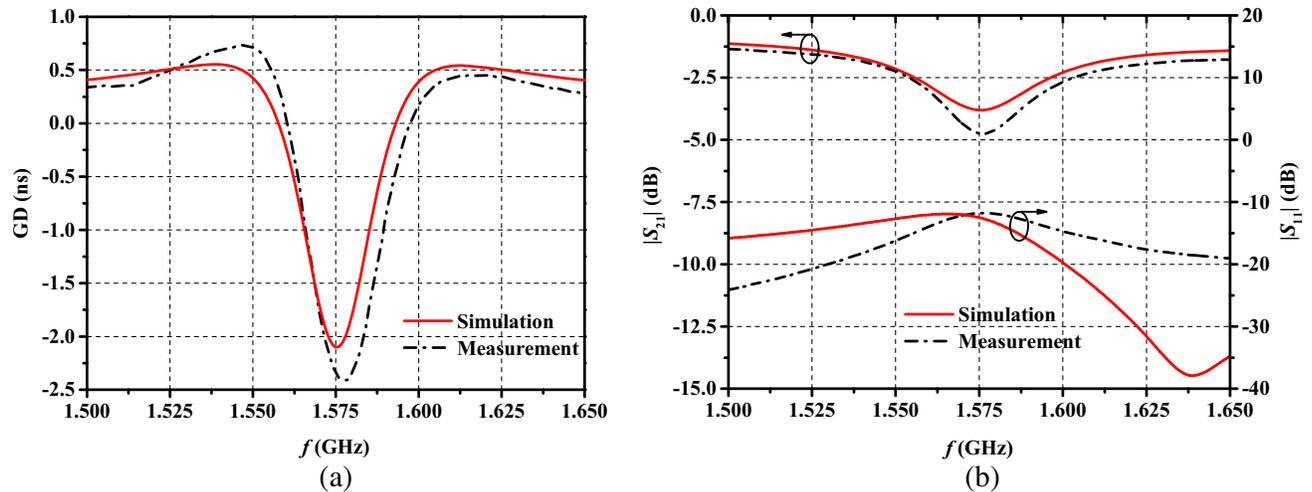
7) Tune  $D_p$  referring to Fig. 3 to achieve the needed center frequency.

### 3. IMPLEMENTATION AND PERFORMANCE

To validate the proposed topology, an NGDC prototype is designed and implemented on a 1.6 mm-thick substrate with a relative dielectric constant of 4.4 and loss tangent of 0.02. The HFSS EM software is used to obtain the optimized dimensions. The dimensions of the NGDC are found and implemented as follows:  $W_d = 9.0$  mm,  $L_d = 24.1$  mm,  $D_h = 1.0$  mm,  $D_p = 3.0$  mm,  $W_a = 2.0$  mm,  $S_a = 0.2$  mm,  $L_a = 8.5$  mm, and  $L_g = 11.8$  mm. Photographs of the fabricated NGDC are shown in Fig. 5. The circuit



**Figure 5.** Photographs of the fabricated NGDC. (a) Top view. (b) Bottom view.



**Figure 6.** Simulated and measured results of the proposed NGDC. (a) GD. (b)  $S$ -parameters.

size of the prototype is  $40 \text{ mm} \times 26 \text{ mm}$  (around  $0.38\lambda_g \times 0.25\lambda_g$ , where  $\lambda_g$  is the guided wavelength of  $50\text{-}\Omega$  transmission line at the center frequency). The fabricated NGDC is measured with an Agilent N5230A network analyzer.

Figure 6 gives the simulated and measured results of the proposed NGDC. As shown in Fig. 6(a), the measured NGD time is  $-2.42 \text{ ns}$  at the center frequency of  $1.577 \text{ GHz}$ . The fractional bandwidth (FBW) for GD less than  $0 \text{ ns}$  is  $2.28\%$  ( $1.561\text{--}1.597 \text{ GHz}$ ). In the NGD band, the measured IL and return loss (RL) are better than  $4.75 \text{ dB}$  and  $11.7 \text{ dB}$ , respectively. There are some discrepancies between the simulated and measured results, which are mainly due to inaccurate dielectric constant and loss of the used FR4 substrate in the prototype and fabrication tolerance. Table 1 shows the comparison of the proposed NGDC with previous designs. Compared with [7–15], the proposed circuit without using the coupled-lines and lumped resistors has a simple and flexible design with a moderate IL, circuit size, and figure of merit (FOM), where the FOM is defined as

$$\text{FOM} = |\text{NGD}(f_0)| \times \text{BW}_{\text{NGD}} \times |S_{21}(f_0)|. \quad (1)$$

**Table 1.** Performance comparison.

Ref.	$f_0$ (GHz)	NGD (ns)	IL (dB)	RL (dB)	NGD FBW (%)	FOM	Size ( $\lambda_g \times \lambda_g$ )	Use of resistor	Use of coupled-lines
[7]	1.016	$-2.09$	18.1	33.0	14.2	0.0375	$0.41 \times 0.41$	Y	Y
[8]	3.450	$-4.60$	20.5	33.7	3.48	0.0521	$0.33 \times 0.29$	Y	Y
[9]	1.570	$-8.75$	20.5	32.0	3.82	0.0495	$0.39 \times 0.19$	Y	Y
[10]	1.260	$-2.20$	2.40	14.0	1.59	0.0334	$0.63 \times 0.28$	N	Y
[11]	2.140	$-1.03$	3.82	12.0	2.80	0.0398	$0.74 \times 0.40$	N	Y
[12]	1.528	$-2.89$	2.91	11.9	1.57	0.0496	$0.38 \times 0.30$	N	Y
[13]	1.970	$-1.00$	2.20	14.0	1.02	0.0155	$0.31 \times 1.25$	N	Y
[14]	1.890	$-1.00$	1.70	15.0	1.06	0.0164	$1.06 \times 0.51$	N	Y
[15]	1.150	$-2.20$	1.93	13.0	1.30	0.0264	$0.44 \times 0.15$	N	Y
This work	1.579	$-2.42$	4.75	11.7	2.28	0.0504	$0.38 \times 0.25$	N	N

## 4. CONCLUSIONS

In this paper, a compact NGDC topology using ACPSs and DSPSs has been presented. Based on the parametric analysis, the NGD characteristic of the proposed circuit is mainly controlled by the open-circuited DSPS combined with the connecting hole. The proposed NGDC topology without the use of coupled lines and lumped components has a simple and flexible design. Its IL and size are small. So it can be applied to various microwave communication and GNSS systems for performance enhancement.

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