

# A Star-Wheel Design of Single Crystal Sapphire Optical Fiber Promoting Single Mode Operation in the Infrared Regime

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**Abstract**—In this study, a star-wheel design of single crystal sapphire optical fiber is proposed to achieve single mode operation in the infrared regime. In the azimuthal direction the structure retains a reduced core of higher refractive index. It is connected to the outer boundary via star-wheel configuration of segments. The region of alternating symmetrical truncated cavities of lower refractive index is air. The enclosed alternating layers of sapphire and air cavities around the reduced core function as cladding. Fiber structure in the azimuthal direction is uniformly distributed in the radial direction. Finite element method is employed to analyze the modal characteristics of fundamental and higher order modes. Under strongly guided approximation, the structure can effectively eliminate the large modal interference. The proposed waveguides, at operating wavelength of  $\sim 1.55 \mu\text{m}$ , with the diameters of  $\sim 50 \mu\text{m}$ ,  $75 \mu\text{m}$ ,  $100 \mu\text{m}$ , and  $125 \mu\text{m}$  diameter, exhibit confinement loss of  $\sim 0.0314 \text{ dB/m}$ ,  $0.0072 \text{ dB/m}$ ,  $0.0023 \text{ dB/m}$ , and  $0.0009 \text{ dB/m}$ , respectively. It is anticipated that such a fiber can be a potential candidate in addressing a wide range of optical sensors and communication systems, which unable to sustain in extremely harsh environments. COMSOL multi-physics® is used to perform numerical investigations.

## 1. INTRODUCTION

Superlative material characteristics of single crystal sapphire optical fiber  $\alpha\text{-Al}_2\text{O}_3$  (SCF) offers various advantages, such as high resolution, superior rigidity, high laser power transfer, flexible strength, chemical unresponsiveness, optical spectroscopy, thermal shock resistance, and high melting point [1–4]. It is more sustainable and resistant than the ordinary silica fibers and can work under harsh environments [5–8]. An unclad SCF of a large core structure possesses large value of numerical aperture and effective refractive index, which turn the optical waveguide unrealistic in terms of reliability and compatibility. Such waveguides restrict numerous practical applications because of large modal interference, transmission losses, and contaminations. Efforts are made to design cladding for SCF by coating low refractive index surface layer, or deposition of highly reflective layer [9–11]. Such coating structures succeeded in the confinement of light propagation into core region of fiber. These fibers, when being exposed to extremely harsh environment loses thermal stability, caused by erosion of coated layer. Due to the lack of adequate cladding, SCF faces major challenges of contamination, reliability, and dopant diffusion, which hinders the performance and acceptance of such fibers in an optical industry.

Compared to silica fibers, the SCF exhibits wide operational range of temperature  $\sim 0$  to  $1800^\circ\text{C}$ , hence, it is becoming a hot topic of research for different industrial units, i.e., gas turbines, coal gasifiers, and other extreme environment catalyst processes. SCF has diversified operating wavelength

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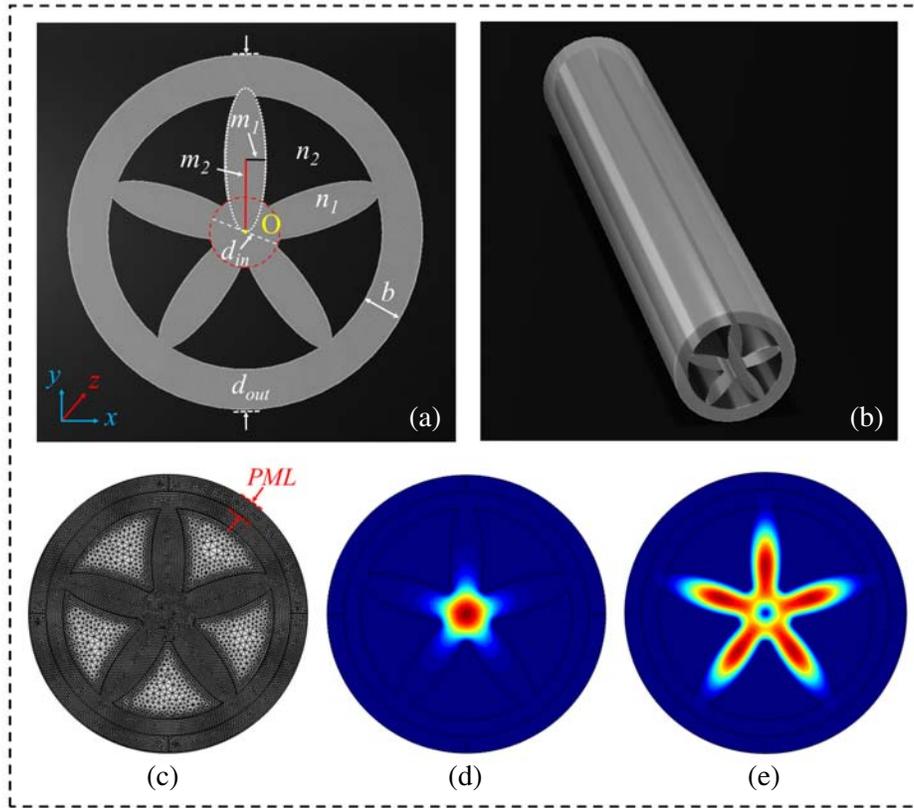
range of 0.3 to 5  $\mu\text{m}$  [12], enabling it to be used from ultra-violet (UV) to Terahertz (THz) wave-guiding. Nowadays, SCF is rapidly gaining popularity in interferometry, and numerous applications have been developed using SCF for interferometric sensing [13] and lasing [14]. SCF is multimode, and its smallest commercially available diameter is  $\sim 75 \mu\text{m}$  and supports  $\sim 23436$  modes [15], still limits the fiber performance owing to large modal interference. Katyba et al. [16, 17] presented photonic crystal waveguides of hollow cores. They achieved low loss dispersion profile of SCF in THz regime and developed a circular geometry SCF close to 300  $\mu\text{m}$  diameter for near field scanning probe microscopy. Nubling and Harrington [18] reported an SCF structure with low loss using laser-heated pedestal-growth method for the ultra violet and visible infrared wavelength regime. Hill et al. [19] presented single mode operation with a fiber diameter of 6.5  $\mu\text{m}$  in the infrared wave-guiding regime by a post-fiber-growth chemical etching process. Cheng et al. [20, 21] explored by simulating a model of windmill shape SCF, to show that the confinement of single-mode is achievable with low loss by tailoring the “windmill” parameters at 532 nm of operating wavelength. This structure addresses the fundamental mode propagation over long distance, but in extreme case the handling of fringes like windmill structure is quite challenging. The structure does not have any appropriate cover. The fiber may face splintering of fringes. It can influence transmission deterioration possibly losing functioning in harsh environments. Recently in [1], our group has reported a precise hexagonal SCF waveguide of  $\sim 35$  micron radius that exhibits 0.077 dB/m confinement loss at 200 nm. Since the hexagonal SCF has a large radius, it supports a large number of modes, where a reduction in fiber diameter would make modal reduction possible, but it has limited range of operating wavelength.

To study FM confinement in the wide range of operating wavelength, a novel and effective design of SCF geometry is proposed. It is proposed that the effective core region is reduced by alternating symmetrical air cavities rounded with the segment of star-wheel configuration, such that alternating layers of higher and lower refractive indices are constituted angularly. The structure ensures the confinement of fundamental mode (FM) over long distance with low confinement loss (CL) and minimal dispersion. Higher order modes (HOMs) incorporate higher leakage loss, thus HOMs are strip-off, and clean single mode operation in the fiber is ensured. A rigorous analysis of segmented-cladding fiber by the radial-effective-index method [22] extends in the numerical investigations. The optical analysis of waveguides is extended up to 2.0  $\mu\text{m}$ , and it is assumed that their results of optical losses, effective refractive index, and dispersion will be helpful for incorporating valuable contribution in the area of high-power fiber thulium and holmium lasers. As such, laser technology is evolving into a variety of optical applications. Accomplishment of such a fine SCF structure will also boost transmission efficiency, sensing capabilities, and thermal robustness, opening new corridors in the field of optical sensing and optics.

## 2. PROBLEM DESCRIPTION AND FORMULATION

### 2.1. Geometry of SCF

The transverse and longitudinal cross-section of proposed SCF is shown in Figs. 1(a) and (b), respectively, where transverse cross-section of SCF lies in the  $xy$ -plane; O is the origin;  $d_{out}$  is the SCF original diameter;  $d_{in}$  is the reduced diameter of effective core region;  $b$  is the width of outer boundary;  $m_1$  and  $m_2$  are the semi-minor and major-axes used to define the alternating segments of sapphire along with azimuthally distributed air cavities, as shown in Fig. 1(a). The proposed structure is uniform in radial direction, as shown in Fig. 1(b). The core and cladding refractive indices are  $n_1$  and  $n_2$ , respectively. The cladding region is taken to be alternating angular array of high and low refractive indices. Free triangular meshing is defined for the proposed geometry to employ FEM. Using the predefined function of COMSOL MESH MENU, free triangular meshing sizes of “extra fine” and “normal” are calibrated for “sapphire” and “air” region, respectively. The perfect match layer (PML) of  $\sim b/2$  is used in the simulations, as shown in Fig. 1(c). COMSOL MODE ANALYSIS is used to obtain the FM and HOM profiles of the structure, as shown in Figs. 1(d) and 1(e), respectively. In this study, four different samples are analyzed for numerical solutions, and their parameters of manufacturing are listed in Table 1. In addition, the proposed samples of SCF can be manufactured by different reported methods, such as edge-defined film-fed growth [23], laser-heated floating-zone directional solidification [24], laser-heated pedestal-growth [25], and micro pulling down [26].



**Figure 1.** (a) Transverse, (b) longitudinal cross-section of the proposed SCF, (c) free triangular meshing by FEM solution, (d) fundamental mode, and (e) higher order mode profile.

**Table 1.** Fiber parameters for manufacturing.

Fiber Type	$d_{out}$ ( $\mu\text{m}$ )	$d_{in}$ ( $\mu\text{m}$ )	$b$ ( $\mu\text{m}$ )	$m_1$ ( $\mu\text{m}$ )	$m_2$ ( $\mu\text{m}$ )	PML ( $\mu\text{m}$ )
SCF — 50 $\mu\text{m}$	50	10	6	3	20	3
SCF — 75 $\mu\text{m}$	75	15	9	4.5	30	4.5
SCF — 100 $\mu\text{m}$	100	20	12	6	40	6
SCF — 125 $\mu\text{m}$	125	25	15	7.5	50	7.5

### 2.2. Theoretical Formulation

In cylindrical coordinates system  $(r, \phi, z)$ , Maxwell's equations for electromagnetic fields in an optical waveguide of invariant index profile along the  $z$ -direction can be decomposed into transverse and longitudinal components as

$$\xi(r, \phi, z, t) = \{\xi_t(x, y) + \xi_z(x, y)\} e^{-j(\omega t - \beta z)}, \tag{1}$$

where  $\xi$  denotes the  $E$  or  $H$  field; subscripts  $t$  and  $z$  denote the transverse and longitudinal components, respectively;  $\omega$  is the angular frequency;  $\beta$  is the complex propagation constant used to solve PML function in the computational domain. When electromagnetic wave reaches the boundary, PML boundary condition absorbs the electromagnetic waves with no reflection. Thus, light propagates in an ideal optical waveguide along  $z$ -direction. Maxwell's equations for an anisotropic-type of a PML

boundary condition can be expressed as [27],

$$\nabla \times E = -jk_o\mu_r [S] H, \quad (2)$$

$$\nabla \times H = jk_o\varepsilon_r [S] E, \quad (3)$$

and

$$[S] = \begin{bmatrix} S_x/S_y & 0 & 0 \\ 0 & S_x/S_y & 0 \\ 0 & 0 & S_x S_y \end{bmatrix}, \quad (4)$$

where  $[S]$  is the PML matrix of  $3 \times 3$ ,  $k_o$  the wave number in the vacuum,  $\varepsilon_r$  the relative dielectric permittivity, and  $\mu_r$  the relative magnetic permittivity. Thereafter, FEM is employed which enables the modified eigen-mode values equation as [28, 29],

$$\nabla \times \mu_r^{-1} ([S]^{-1} \nabla \times E) - k_o^2 \left( \varepsilon_r - \frac{j\sigma}{\omega} \right) [S] E = 0, \quad (5)$$

where

$$\gamma = k_o^2 \left( \varepsilon_r - \frac{j\sigma}{\omega} \right), \quad (6)$$

$\gamma$  is the eigen-mode value,  $\sigma$  the electrical conductivity, and  $[S]^{-1}$  the inverse of matrix  $[S]$ . The time harmonic electric field propagating out of plane can be expressed as,

$$E(x, y, z) = \text{Re} \left[ \tilde{E}(x, y) e^{j\omega t - \beta z} \right], \quad (7)$$

$\tilde{E}$  is the electric field phasor, and  $z$  is the direction of propagation,

$$\beta = k_o \text{Re}(n_{eff}) + k_o \text{Im}(n_{eff}) = -\gamma, \quad (8)$$

where  $\text{Re}(n_{eff})$  and  $\text{Im}(n_{eff})$  are the real and imaginary parts of  $\beta$ . The confinement loss (CL) can be calculated as [30–32]

$$\text{CL} = 8.868 k_o \text{Im}(n_{eff}), \quad (9)$$

Further, the dispersion relation of an optical waveguide can be estimated as [32],

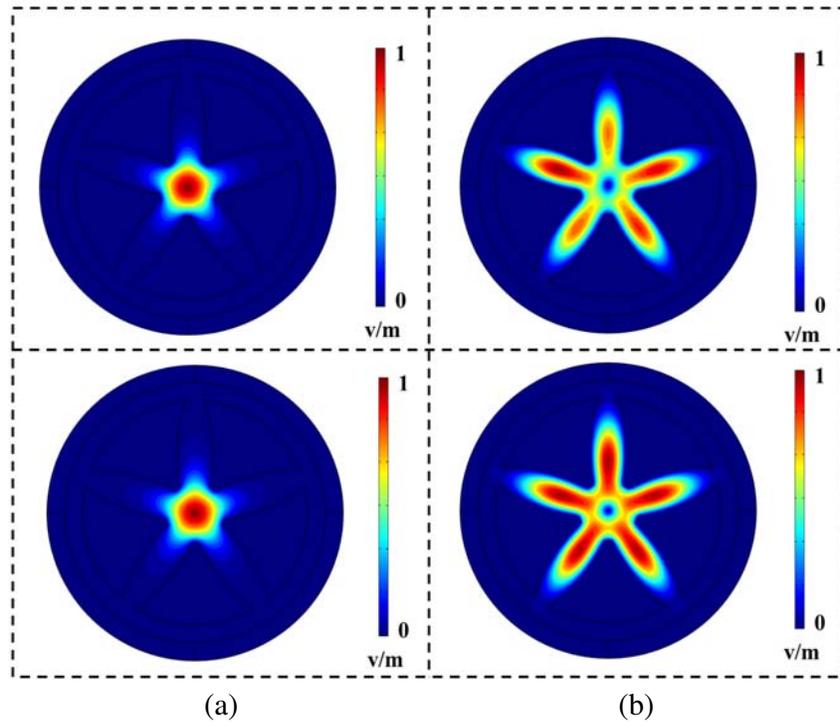
$$D = -\frac{\lambda}{c} \frac{d(\text{Re}(n_{eff}))}{d\lambda^2} \quad (10)$$

### 3. NUMERICAL RESULTS AND DISCUSSION

In order to demonstrate modal reduction, a star-wheel design of SCF structure is proposed. The star-wheel structure varies azimuthally and radially, and it is uniform. The large core of SCF can be effectively reduced by introducing the symmetrical air cavities. Alternating high and low refractive region around the reduced core can be constituted. This region is cladding region. The refractive index of the sapphire and air region used in the numerical investigation are  $n_1 = 1.7462$  and  $n_2 = 1$ , respectively. The operating wavelength of  $1.5 \mu\text{m}$  is used for simulation.

#### 3.1. Electric Field Distribution

COMSOL multi-physics<sup>®</sup> software is employed to perform the modal analysis. The spectral wavelength range of  $0.3\text{--}2.0 \mu\text{m}$  is used for modal analysis. From Eq. (6), FEM is used to obtain the modified eigen-mode value through the built-in function of free triangular meshing, as shown in Fig. 1(c). Multiple iterations are performed until the solution converges to a defined error limit. Electric field ( $E$ -field) distributions of FM and HOM for proposed geometry are obtained by employing the PML, as defined by the PML matrix  $[S]$  from Eqs. (4) and (5). The obtained  $E$ -fields at  $0.3 \mu\text{m}$  and  $1.55 \mu\text{m}$  for FM and HOM are shown in Figs. 2(a) and (b), respectively. It can be inferred from Figs. 2(a)–(b) that counter profile seems analogous but their differential ratio in the case of HOM is inconsistent at lower and higher wavelengths. The trend for the confinement of FM deemed obvious at both operating wavelengths. However, the HOM generates strong evanescent field, which may contribute to higher leakage loss.



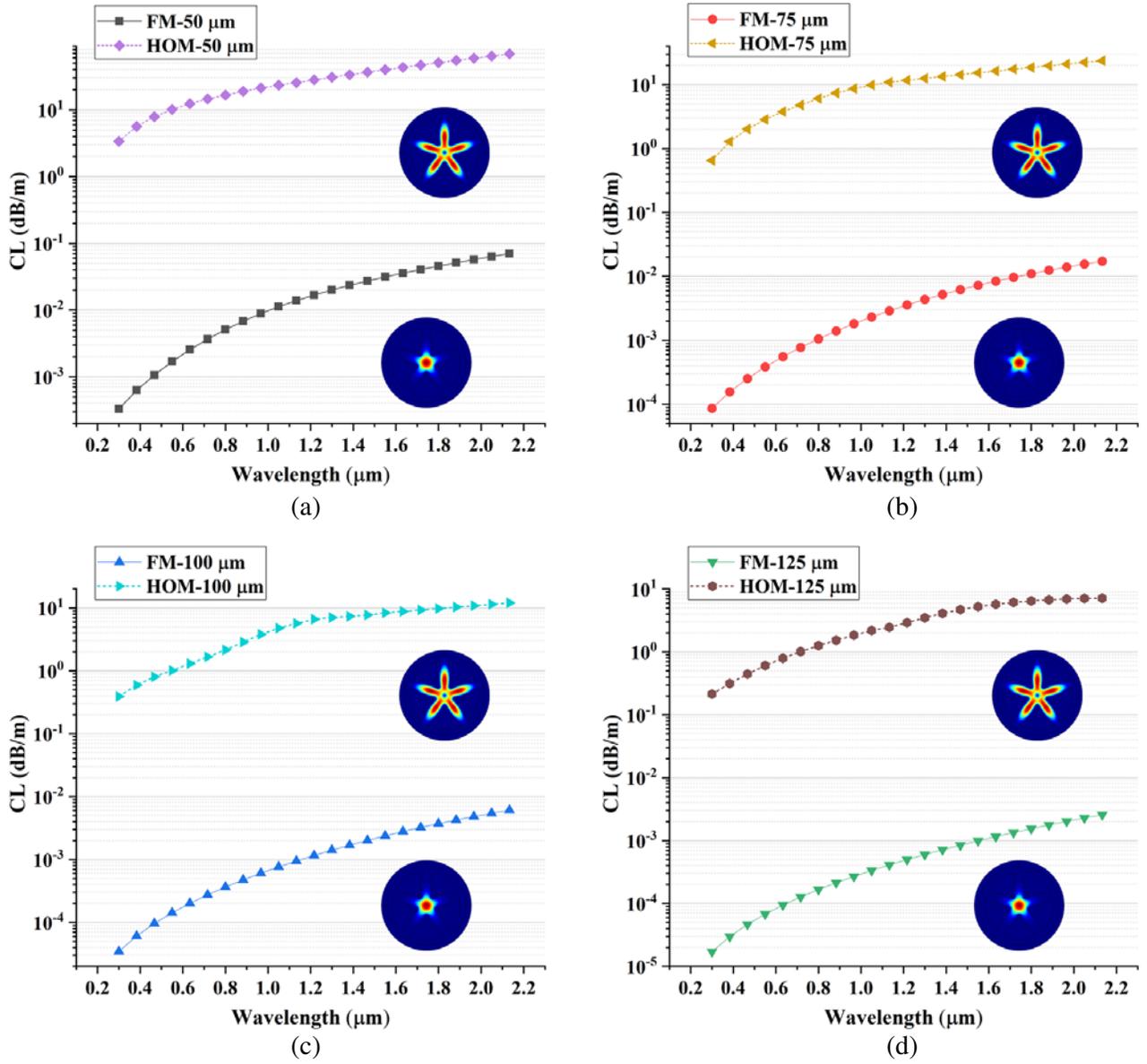
**Figure 2.** Simulated normalized E-field distribution of (a) FM (top  $\sim \lambda = 0.3 \mu\text{m}$  and bottom  $\sim \lambda = 1.5 \mu\text{m}$ ), (b) HOM (top  $\sim \lambda = 0.3 \mu\text{m}$  and bottom  $\sim \lambda = 1.5 \mu\text{m}$ ).

### 3.2. Confinement Loss and Effective Refractive Index

In order to investigate the leakage loss of FM and HOM, the CL is inspected at different wavelengths, i.e., from  $0.3 \mu\text{m}$  to  $2.0 \mu\text{m}$ . CL strongly depends on imaginary part of effective refractive index, and its values corresponding to given geometry are obtained from Eq. (9). The proposed SCF with different diameters, i.e.,  $50 \mu\text{m}$ ,  $75 \mu\text{m}$ ,  $100 \mu\text{m}$ , and  $125 \mu\text{m}$ , exhibits CL of  $0.0314 \text{ dB/m}$ ,  $0.0072 \text{ dB/m}$ ,  $0.0023 \text{ dB/m}$ , and  $0.0009 \text{ dB/m}$ , respectively, at the operating wavelength of  $1.55 \mu\text{m}$ . The absolute values of CL for

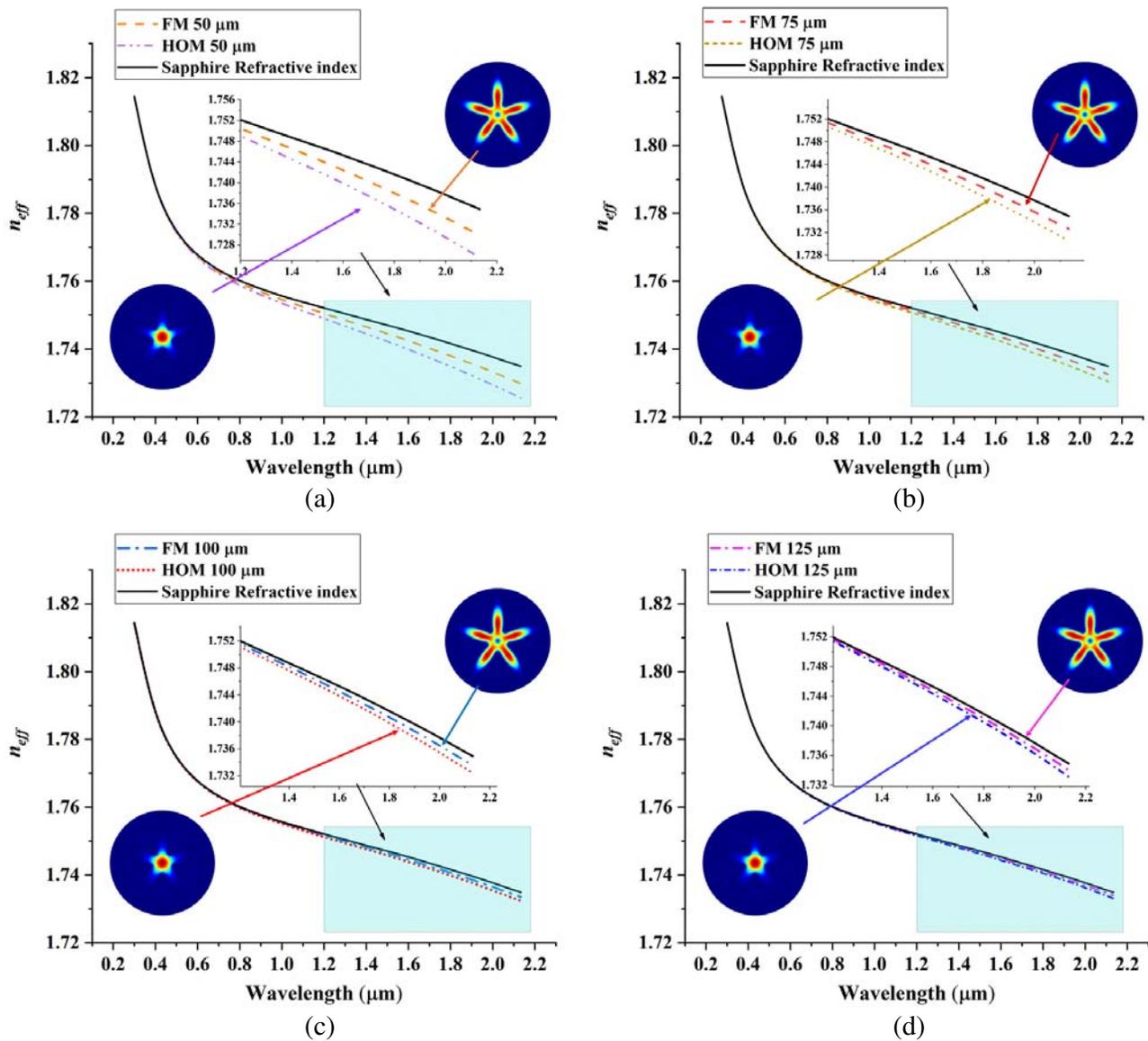
**Table 2.** Confinement loss and effective refractive index as a function of wavelength.

Wavelength ( $\mu\text{m}$ )		$\lambda = 0.3$		$\lambda = 0.8$		$\lambda = 1.55$		$\lambda = 2.0$	
CL (dB/m)	Diameter ( $\mu\text{m}$ )	FM	HOM	FM	HOM	FM	HOM	FM	HOM
	CL (dB/m)	50	$3.31 \times 10^{-4}$	2.7348	0.00509	17.103	0.03142	40.015	0.057104
75		$8.64 \times 10^{-5}$	0.85839	0.00105	8.8647	0.00728	15.337	0.013986	21.065
100		$3.45 \times 10^{-5}$	0.38455	$3.65 \times 10^{-4}$	2.4471	0.00238	8.3557	0.004823	10.917
125		$1.71 \times 10^{-5}$	0.20774	$1.66 \times 10^{-4}$	1.2618	$9.92 \times 10^{-4}$	6.4716	0.002017	6.8201
$n_{eff}$	50	1.8143	1.8142	1.7594	1.7597	1.7435	1.7411	1.7341	1.7304
	75	1.8143	1.8143	1.7598	1.7595	1.7449	1.7438	1.7364	1.7347
	100	1.8143	1.8143	1.7599	1.7598	1.7455	1.7448	1.7372	1.7362
	125	1.8143	1.8143	1.76	1.7599	1.7457	1.7453	1.7376	1.737



**Figure 3.** CL as a function of wavelength for different diameter of SCF, (a) 50  $\mu\text{m}$ , (b) 75  $\mu\text{m}$ , (c) 100  $\mu\text{m}$ , and (d) 125  $\mu\text{m}$ .

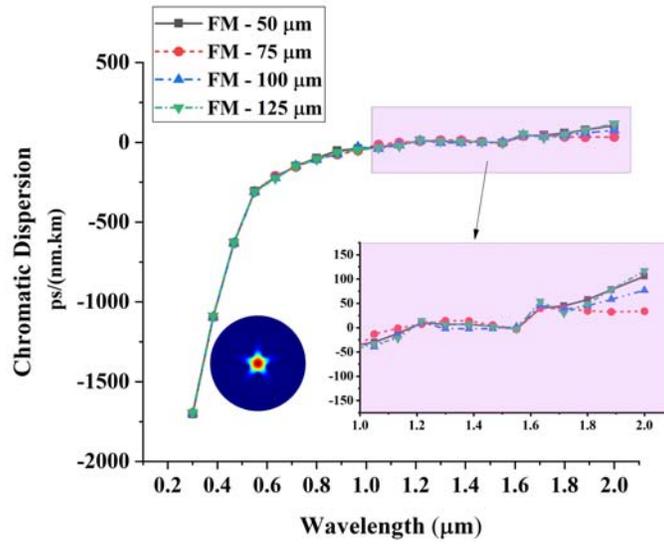
different diameters of fiber show that the proposed geometry ensures the propagation of FM with low CL. On the other hand, the HOM presents high leakage loss with differential loss factor of  $10^3$  to  $10^4$  dB/m. These modes can be easily stripped off from fiber over the shortest propagation distance, i.e., less than 1 meter. The graphical summary of CL for different proposed diameters of the SCF geometry in comparison with FM and HOM as a function of wavelength from 0.3  $\mu\text{m}$  to 2.0  $\mu\text{m}$  is given in Figs. 3(a)–(d). The effective refractive index of the proposed SCF is also numerically calculated by Sellmeier equation [1], and a comparison is made by varying the operating wavelength. From Figs. 4(a)–(d), the graphic summary elucidates the variation of  $n_{eff}$  as a function of wavelength. The insets of each figure describe the  $n_{eff}$  difference of FM and HOM with a comparison of real sapphire refractive index. The detailed numerical results of CL and  $n_{eff}$  at different wavelengths of 0.3  $\mu\text{m}$ , 0.8  $\mu\text{m}$ , 1.55  $\mu\text{m}$ , and 2.0  $\mu\text{m}$  are listed in Table 2.



**Figure 4.** The variation of effective refractive index  $n_{eff}$  of proposed SCF as a function of wavelength in comparison with Sapphire refractive index; for different diameters, (a) 50  $\mu\text{m}$ , (b) 75  $\mu\text{m}$ , (c) 100  $\mu\text{m}$  and (d) 125  $\mu\text{m}$ .

### 3.3. Chromatic Dispersion

The chromatic dispersion of proposed samples of SCF at the operating wavelengths in between 0.3  $\mu\text{m}$  and 2.0  $\mu\text{m}$  is shown in Fig. 5. It can be inferred from dispersion curves that the proposed SCF exhibits ultra-flattened, nearly zero chromatic dispersion over the observed wavelength in between 1.1 and 1.6  $\mu\text{m}$ . In the range of near and short wavelength of infrared bands, dispersion variation of 4.2 ps/(nm · km) is observed, which is given in the inset of Fig. 5. However, when the wavelength is increased from 1.6  $\mu\text{m}$  to 2.0  $\mu\text{m}$ , the fiber posed slightly dispersive from 33 to 117 ps/(nm · km). A comparison of chromatic dispersion corresponding to FM of SCF with material dispersion of sapphire is numerically evaluated from Eq. (10), and their results are listed in Table 3.



**Figure 5.** Chromatic dispersion as a function of wavelength.

**Table 3.** Chromatic dispersion as a function of wavelength.

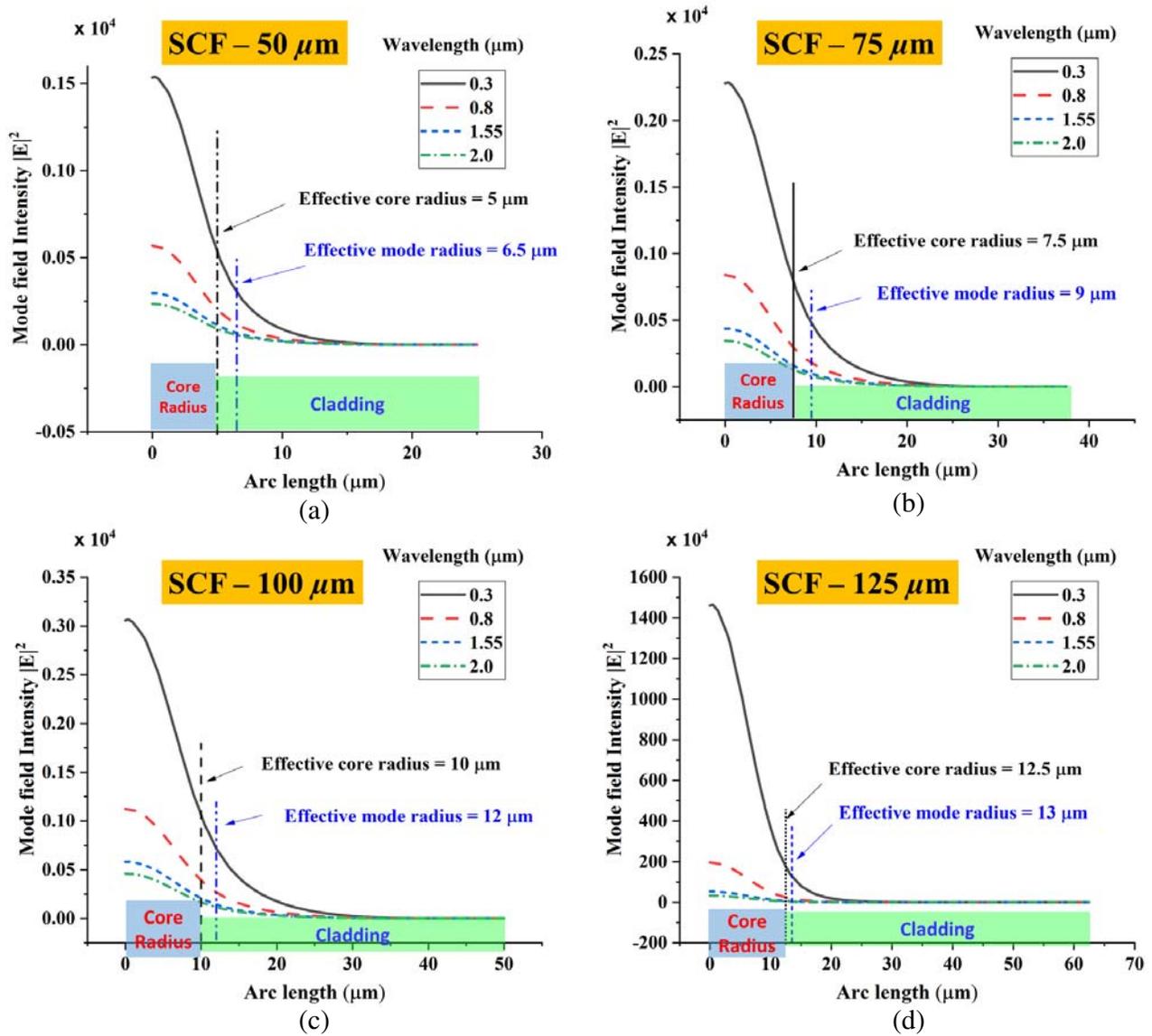
Wavelength ( $\mu\text{m}$ )		$\lambda = 0.3$	$\lambda = 0.8$	$\lambda = 1.55$	$\lambda = 2.0$
	Diameter ( $\mu\text{m}$ )	FM	FM	FM	FM
Chromatic dispersion (ps/nm · km)	50	-1703.55	-98.35	-3.04	105.76
	75	-1695.89	-103.85	-2.90	33.71
	100	-1698.41	-107.51	1.96	77.06
	125	-1692.75	-105.68	-2.60	117.05
Material dispersion in Sapphire	-	-5108.6	-170.82	25.50	57.316

### 3.4. Mode Field Radius (MFR) and Numerical Aperture (NA)

In order to analyze the optical properties of the SCF involving mode field analysis and numerical aperture (NA), FEM is utilized to solve the radial effective index that was used for analyzing any step index fibers, photonic crystal fibers, and other special structures. Since analytical solution of real and imaginary propagation constants is quite cumbersome to solve, as given in Eq. (8), numerical solution of FEM is employed. The mode field radius (MFR) and NA are numerically solved, as effective area is  $2 \times$

**Table 4.** Numerical aperture and mode field diameter of proposed fiber.

Fiber type	Numerical aperture( NA)				MFD ( $\mu\text{m}$ )
	$\lambda = 0.3$ ( $\mu\text{m}$ )	$\lambda = 0.8$ $\mu\text{m}$	$\lambda = 1.55$ $\mu\text{m}$	$\lambda = 2.0$ $\mu\text{m}$	
SCF — 50 $\mu\text{m}$	0.0190491	0.0496352	0.097068	0.1221955	13
SCF — 75 $\mu\text{m}$	0.0190491	0.0324957	0.0647259	0.0833643	18
SCF — 100 $\mu\text{m}$	0.0190491	0.026533	0.0494387	0.0645811	24
SCF — 125 $\mu\text{m}$	0.0190491	0.0187619	0.0417846	0.0527333	26



**Figure 6.** The evolution of mode field radius via intensity profile of FM, which is formulated in comparison with effective core radius for different diameters of proposed SCFs, (a) 50  $\mu\text{m}$ , (b) 75  $\mu\text{m}$ , (c) 100  $\mu\text{m}$  and (d) 125  $\mu\text{m}$ .

times of an order of MFR that is used to define mode field diameter (MFD) and determines the power field density. As we can see from the summary, Fig. 6, intensity profile of FM shows that smaller MFR would anticipate higher nonlinear effects on incidence, whereas  $NA$  of an angularly segmented cladding can be defined by replacing  $n_2$  with  $n_{eff}$  [33], thus  $NA = \sqrt{n_1^2 - n_{eff}^2}$ , and its plot as a function of wavelength is shown in Fig. 7. MFD and  $NA$  of the fiber are numerically evaluated as a function of fiber arc length and operating wavelength, respectively, and their results are listed in Table 4.

### 3.5. Guided Mode Analysis

The number of guided modes in a fiber is obtained by solving Helmholtz equation with appropriate boundary conditions. An ordinary single-mode optical fiber ensures single-mode operation under weakly guided approximations ( $n_1 \approx n_2$ ). Single-mode operation in an optical fiber is only possible if  $V < 2.405$ ,

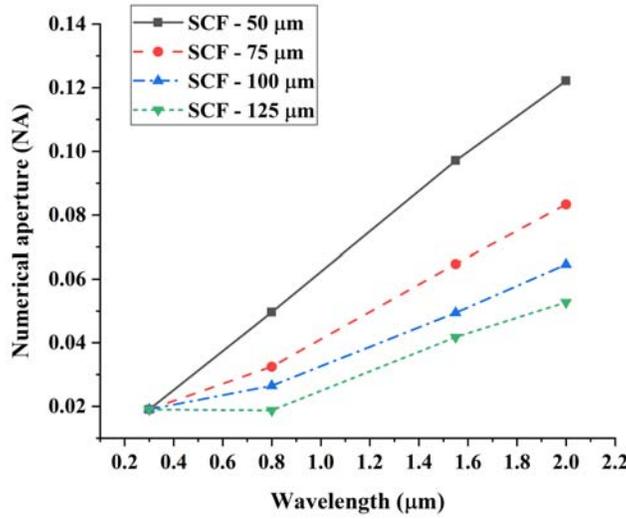


Figure 7. NA as a function of wavelength.

and the parameter  $V$  for an optical waveguide can be estimated as [34],

$$V = \pi \frac{d}{\lambda} \sqrt{n_1^2 - n_2^2} \tag{11}$$

where  $d$  is the core diameter,  $\lambda$  the operating wavelength, and the number of guided modes for a large core optical fiber can be estimated as [20]

$$M = \frac{4}{\pi^2} V^2 \tag{12}$$

The number of guided modes in a conventional SCF with reduced diameter of fiber is given by Eq. (12). The graphical analysis of  $M$  for a conventional SCF in comparison with proposed SCF is given in Fig. 8. It can be inferred from the summary that a large number of guided modes propagate in a conventional SCF. This can be decreased by the reduction of core size, but still large modal interference exists. In contrast, the use of segmented cladding (star-wheel shape) in SCF geometry has significantly

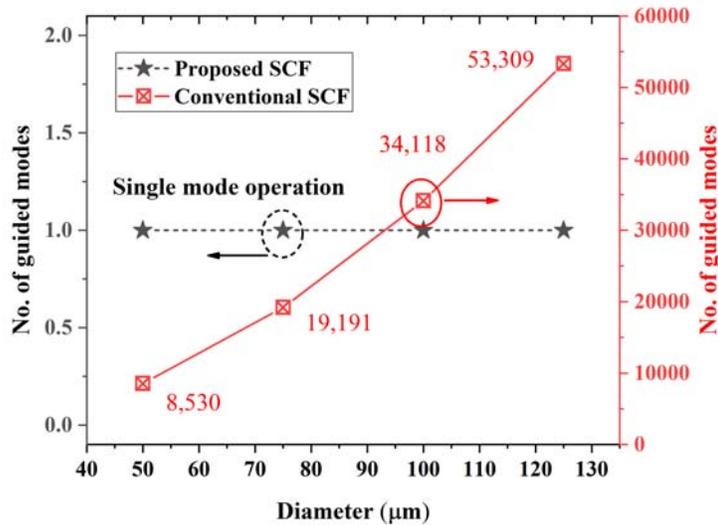


Figure 8. Comparison of number of guided mode in conventional SCF with proposed SCF.

reduced CL and chromatic dispersion, whereas HOM exhibits higher leakage loss with differential loss factor of  $10^3$  to  $10^4$  dB/m than FM. Ultra-flatten dispersion slope in the infrared regime ensures single mode operation for the proposed SCF samples of 50  $\mu\text{m}$ , 75  $\mu\text{m}$ , 100  $\mu\text{m}$ , and 125  $\mu\text{m}$ . Thus, it is fully capable of maintaining single mode operation. Compared with the CL of conventional SCF  $\sim 10^6$  dB/m [21], the proposed SCF exhibits negligible CL, which is  $\sim 10^{-3}$  to  $10^{-4}$  dB/m. Considering the simulate performance, it is proposed that the star-wheel design of SCF is reliable and sustainable candidate in the harsh and extremely high-temperature environments. Also, this structure can suppress large modal interference and gives single mode operation with low CL and minimal chromatic dispersion.

#### 4. CONCLUSION

A novel design of star-wheel shape of SCF with single mode operation in the spectrum of ultraviolet to short infrared wavelength is demonstrated. The structure retains a reduced core region surrounded by alternating segmented cladding region in the azimuthal directions, whereas radially fiber remains uniform. The effect of segmented cladding with the variation of four different fiber diameters is investigated. FEM analysis successfully demonstrates that differential loss factor of CL for HOM is  $\sim 10^4$  times greater than FM, thereafter fiber ensuring clean single mode operation. FM of the waveguides exhibits low confinement loss of  $\sim 0.0314$ , 0.0072, 0.0023, and 0.0009 dB/m and minimal chromatic dispersion of  $\sim -3.04$ ,  $-2.90$ , 1.96, and  $-2.60$  ps/(nm  $\cdot$  km), for 50  $\mu\text{m}$ , 75  $\mu\text{m}$ , 100  $\mu\text{m}$ , and 125  $\mu\text{m}$  diameter, respectively at operating wavelength of  $\sim 1.55$   $\mu\text{m}$ . Numerical results demonstrate that the proposed SCF can promote its application in wide range of interferometry and optics in extremely harsh environments.

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