

# A Dual-Layer Microstrip Patch Antenna with Stub Designed by Simulated Annealing Algorithm for Circular Polarization

Li Guo\* and Zhiqiang Yao

**Abstract**—In this paper, a design method that employs simulated annealing (SA) algorithm to create stub structure of a dual-layer microstrip patch antenna for circular polarization is presented. Firstly, based on established controls of SA algorithm, a series of stub structures have been created automatically on the stacked parasitic element — (Split Ring Resonator) SRR of antenna. The desired stub structure is chosen according to the generation of orthogonal modes that produce circular polarization through the electromagnetic coupling to the driven patch with an SRR-shaped slot. Then, a dual-layer microstrip patch antenna with a Z-shaped stub and left-hand circularly polarized (LHCP) characteristic is obtained by employing the assisted design. The designed antenna is simulated, optimized, fabricated, and measured. The results show that the microstrip patch antenna with Z-shaped stub has a simulated minimum axial ratio of 1.64 dB at 2.4 GHz, and the measured peak gain can be up to 5.87 dBi.

## 1. INTRODUCTION

Circularly polarized (CP) antennas are used widely in modern wireless communication systems, since they can aid in reduction of multipath effects and making the orientation between transmitting and receiving antennas flexible. However, sometimes the design process of CP antennas is arduous due to multi-objective solutions with the need of meeting desired or high requirements. Using optimization/evolutionary algorithms for the design of circular polarization can lighten the design process and has received much attention [1, 2]. Amongst CP antennas, single-feed multilayer microstrip patch antennas are much preferred due to their simple feeding structures [3]. In addition, by stacking parasitic or multilayer structures and employing electromagnetic coupling, high CP performances can be realized [4]. For such antennas, generally, perturbation structures need to be applied and are vital for CP radiation. Thus, to reduce design complexity, one can use optimization algorithms to only design the perturbation structure of these antennas for circular polarization. The applications behind these CP antennas include mobile communications [5], satellite communications, wireless sensor networks [6], amongst others.

As for designing single-feed CP multilayer microstrip patch antennas, the excitation of two orthogonal modes with equal amplitude and  $90^\circ$  phase difference is challenging in limited antenna geometry. Different from this, another approach needs two separate orthogonal feeds to achieve circular polarization. The radiation patch for generating circular polarization can have various shapes, such as rectangular, triangular, circular, and square-ring shapes. Generally, the patches need to be truncated, slotted or load stubs to introduce perturbations. Also, circular polarization can be realized by stacking structures [7], asymmetrical feeding, etc. When loading stubs, the functions for stubs are to introduce or excite a loaded mode and to tune the phase difference of orthogonal modes to be  $90^\circ$  [8]. However, majority of stubs are loaded on the driven patch or feeding layer, and little research work focuses on loading a stub on the stacked structure for generating orthogonal modes through electromagnetic

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\* Corresponding author: Li Guo (guoli\_31@163.com).

The authors are with the College of Information Engineering of Xiangtan University, Xiangtan, China.

coupling [9]. In addition, the loading location and shape of stubs are difficultly determined, or they are obtained with the need of amounts of human operations. Using optimization/evolutionary algorithms to design the stub structure for circular polarization can reduce heavy workloads. The possible employed algorithms may include: genetic, particle swarm, and simulated annealing algorithms, which function by generally simulating the behaviours existing in nature [10,11]. Apart from the designs mentioned above, these algorithms have been successfully applied to the optimization of various antennas, such as wire, single-layer patch [12], and array antennas [13]. However, it is usually difficult to create/place structures using optimization/evolutionary algorithms for attaining desired performances [14]. Generally, algorithms are applied combining certain antenna characteristics for these designs [15]. In particular, stub structures on the stacked element can be designed by using algorithms and can be loaded to excite the orthogonal modes of circular polarization by employing or enhancing electromagnetic coupling. Amongst available algorithms, simulated annealing algorithm (SA) is a simple tool and has advantages in finding the hidden global minimum. It has been utilized in several antenna designs to solve multiobjective and global antenna optimization problems [16].

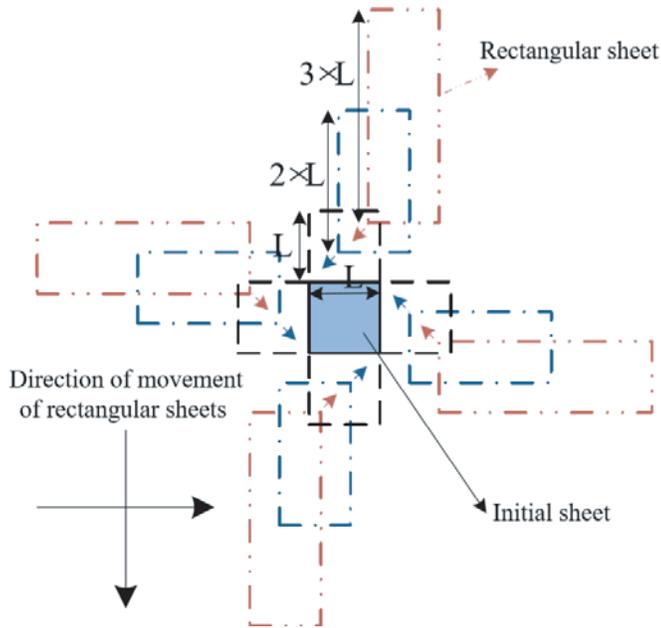
In this paper, a dual-layer microstrip patch antenna with a Z-shaped stub structure has been designed by employing SA algorithm which is dedicated to the creation of stub structures on a stacked SRR for circular polarization. In this regard, HFSS and MATLAB software package are used for co-simulation to create the design, for which firstly, the stub structures are generated in terms of placement of a set of discrete small rectangular sheets. Then, they are united with the stacked SRR in further optimization process. By integrating these innovations in the design, a dual-layer microstrip patch antenna with a Z-shaped stub is produced with CP property. The Z-shaped stub is used to generate orthogonal modes which result in CP radiation. The remaining parts of this paper are arranged as follows. Section 2 presents the procedure for antenna design combining the SA and resulting stub structures. Section 3 illustrates an optimized CP microstrip patch antenna and its corresponding characteristics. The conclusion is presented in Section 4.

## 2. ANTENNA DESIGN PROCESS

### 2.1. Design Methodology Combining SA

In the design process, an initial dual-layer microstrip patch antenna is first constructed following the utilization of algorithm for further design, and SA control is an important consideration for the final antenna geometry, which is dedicated to creating stub structures. Despite the general deployment of distinction optimization algorithms for optimizing antenna structures, this paper presents solutions for constructing structures on a stacked parasitic element of a microstrip patch antenna. This design is based on an original dual-layer microstrip patch antenna with co-simulation of HFSS and MATLAB. For positively exploiting the electromagnetic coupling between stacked layers of the microstrip patch antenna, two layers of substrate are employed for the designed antenna and are then spaced by an air gap layer. Furthermore, the stub structure is built on the parasitic element of the upper layer to achieve a desired impact on the driven patch and the entire antenna. A square driven patch is placed on the lower substrate, and an SRR-shaped slot is etched into it. In addition, a stacked SRR (SSRR) is placed on top of the upper substrate with its split direction facing opposite to the split of the lower SRR-shaped slot. To achieve broadband and different polarizations, the desirable stub structures are generated in a step-by-step process along the split of the SSRR. These are composed of a sequence of small rectangular conducting sheets which are selectively placed, under the control of SA. The operation steps involved are elaborated as follows.

First, the initial placement location (the location is at the split gap of the SSRR) and initial small square sheet with a width of 1 mm are specified, along with determination of initial antenna size and SA parameters. Second, the arm width of SRR-shaped slot and the feeding position are set at the beginning initially in order to establish the required parameters for the antenna addressed in the following step. Third, based on the initially placed sheet, a set of small rectangular sheets with widths of 1 mm are placed in an adding-and-deleting manner along all edges of the initial sheet throughout four directions — front, back, left, and right, with three lengths, 1 mm, 2 mm, and 3 mm, which are changed at each direction. The placement process for small rectangular sheets is illustrated in Figure 1. The reflection coefficient  $|S_{11}|$  of the resulting antenna is calculated in HFSS. The  $|S_{11}|$  at three frequencies:



**Figure 1.** Diagram of the placement process of the small rectangular sheets.

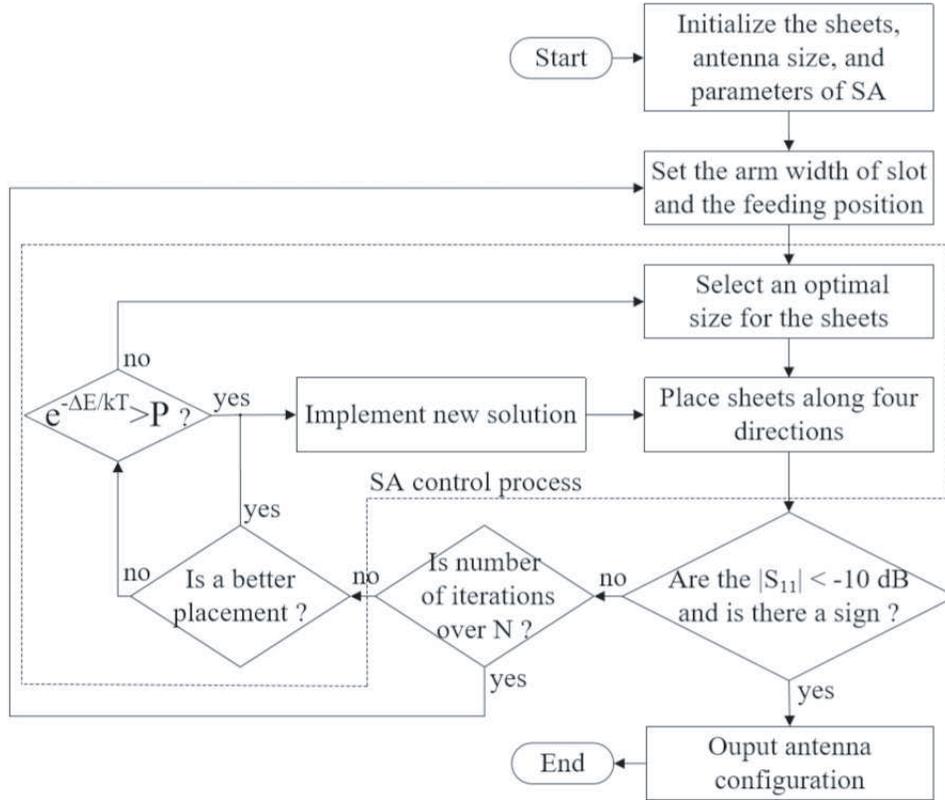
first and second resonance frequency, and frequency corresponding to the peak  $|S_{11}|$  that lies in the previous two frequencies, are recorded to determine an optimal size for the placed small rectangular sheets. In addition, if three resonance frequencies appear in the placement process, then it gives a message to represent three possible resonant modes produced with the sheets placed in the near area. Per the criterion for optimal size, at the middle frequency,  $|S_{11}|$  is the lowest among the stored values of the middle frequency. Fourth, a set of small rectangular sheets with optimum size are placed in an adding-and-deleting manner along all four edges of the sheet selectively before determining the following optimal sheet placement. Note that for every placement,  $|S_{11}|$  is calculated. Fifth, if the recorded value of  $|S_{11}|$  at the three frequencies is below  $-10$  dB, and a message representing three resonant modes appears, then the desired stub structure is generated, marking the end of the design process. However, if the number of iterations exceeds the value of  $N$ , then arm widths of the SRR-shaped slot and feeding position are reset. If the number of iterations is not  $N$ , then an annealing process is carried out involving probability judgment and a possible redoing of size selection for sheets which is done in step three, as required. Subsequently, SA controls the main convergence process. In addition, it is critical to set the arm width of SRR-shaped slot and feeding position as it is imperative to the overall design — if done properly, only a few iterations are needed to achieve the desired antenna design. A complete flowchart for these steps is shown in Figure 2.

In optimization process, the design is directed by calculating the  $|S_{11}|$  only at the first and second resonance frequencies and at the peak point between the former two frequencies but not for the third one. The reason behind this is to firstly reduce program complexity, and, secondly, for matching the impedance of third resonance with the former two ones since it has a low mutual coupling and can be adjusted through further optimization. Another point worth mentioning is to place the small rectangular sheets to obtain the desired stub structures while using the random search algorithm, as it is highly difficult to converge it to target state even if it undergoes a number of dimension adjustments.

A critical part of the SA algorithm is the annealing process, which guides the convergence, as the current temperature  $T_n$  is decreased step by step. The geometric annealing process can be represented as [10, 13]:

$$T_n = \alpha T_0 \tag{1}$$

where  $T_0$  is the initial temperature, and  $\alpha$  is the scale factor. For the parameters initialized in the program,  $T_0 = 50$ ,  $\alpha = 0.75$ .



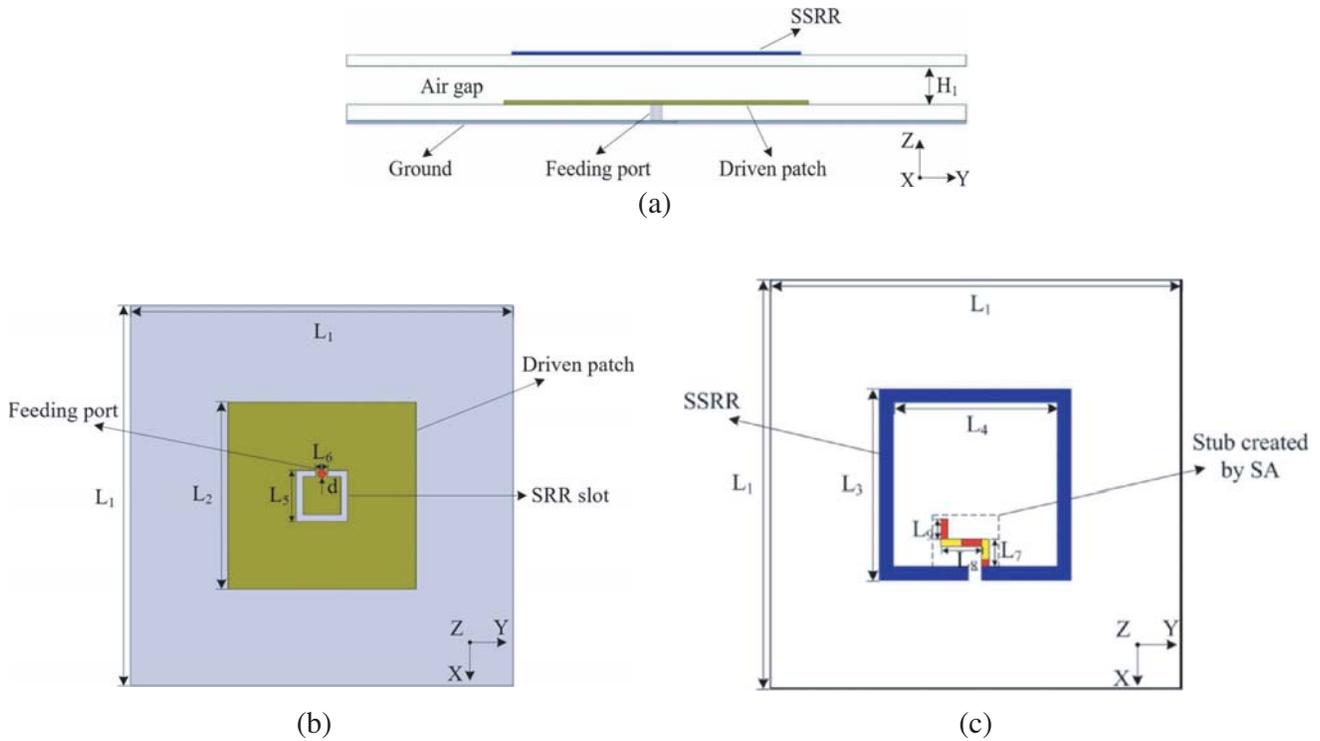
**Figure 2.** Flowchart of design procedure. In the formula:  $\Delta E$  represents the energy change related to the calculated  $|S_{11}|$ ,  $T$  is the current temperature,  $k$  is the Boltzman's constant, and  $P$  is a random probability.

## 2.2. Antenna and Stub Structures

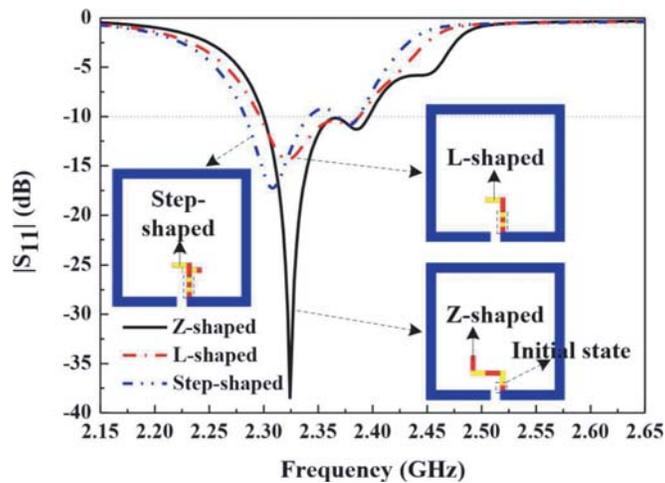
Initial antenna geometry comprising stub created by SA is presented in Figure 3. In this design, the stub consists of a set of discretely-placed, small rectangular sheets. The substrates used employ Rogers 4350B material ( $\epsilon_r = 4.38$ ,  $\tan \delta = 0.0037$ , at the frequency of 10 GHz). The thicknesses for lower and upper substrates are 1.5 mm and 1 mm, respectively. The whole dimension of the antenna is  $0.48\lambda_0 \times 0.48\lambda_0 \times 0.056\lambda_0$ , where  $\lambda_0$  is the free-space wavelength at the center frequency. A set of discretely-placed small rectangular sheets constitute a stub with a certain shape, such as a Z-shaped stub, which works on positively obtaining desired antenna performances.

After a series of trial-and-correction steps, three stub structures are created, namely Z-, L-, and step-shaped stubs, as shown in Figure 4.  $|S_{11}|$  versus frequency curves corresponding to these stubs have also been provided. The Z-shaped stub is created in terms of one initial placed sheet, while the L- and step-shaped stubs are created in terms of four. In addition, the step-shaped stub is obtained for the  $|S_{11}|$  value  $-10 \text{ dB} < |S_{11}| < -9 \text{ dB}$  in the fifth step of the design procedure. As evident from Figure 4, there are three combined resonant peaks that form a wide 10-dB ( $|S_{11}| < -10 \text{ dB}$ ) impedance bandwidth. The rectangular patch, SRR-shaped slot, and SSRR induce three resonances. The creation and use of stubs makes it possible to combine the resonances in a low mutual coupling state. Note that there is a slight difference in size for the lower patch and feeding position of the three resulting antennas because of size resetting that occurs in the design procedure.

Co-simulation is run on a desktop computer with a CPU Intel(R) Core (TM) i7-4770 with a main frequency of 3.4 GHz. The results obtained for simulation experiments show that most run-times of the co-simulation are taken on HFSS due to the need for massive electromagnetic parameter calculation. When final optimized programs are accomplished, the dual-layer microstrip patch antenna with a Z-



**Figure 3.** Geometry of the designed dual-layer microstrip patch antenna: (a) lateral view; (b) lower layer; (c) upper layer. The labelled dimensions are listed as follows:  $L_1 = 60$  mm,  $L_2 = 29.5$  mm,  $L_3 = 28$  mm,  $L_4 = 24$  mm,  $L_5 = 8$  mm,  $L_6 = 2$  mm,  $L_7 = 4$  mm,  $L_8 = 6$  mm,  $L_9 = 3$  mm,  $d = 3.5$  mm, and  $H_1 = 4.5$  mm.



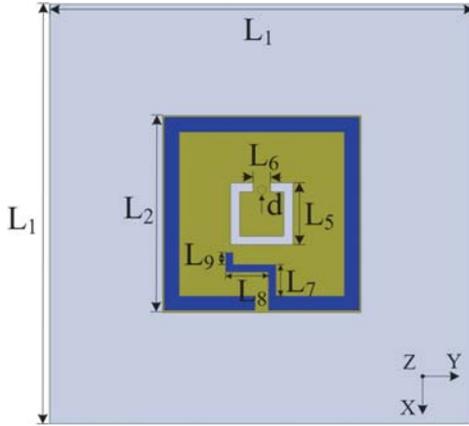
**Figure 4.** Reflection coefficients of the three designed dual-layer microstrip patch antennas with Z-, L-, and step-shaped discrete stub, respectively, along with the corresponding stub structures.

shaped stub experiences 25 iterations; the antenna with an L-shaped stub experiences 19 iterations; the antenna with a step-shaped stub experiences 64 iterations due to a more complicated structure. The stub structures are generated in a step-by-step process in consideration of their sensitivity to impedance match and adjustment of resonance, which can be reflected throughout  $|S_{11}|$  parameters calculated in the search procedure. In addition, all resulting antennas possess similar geometries, differing only in stub structure, which leads to approximate gain and impedance bandwidth.

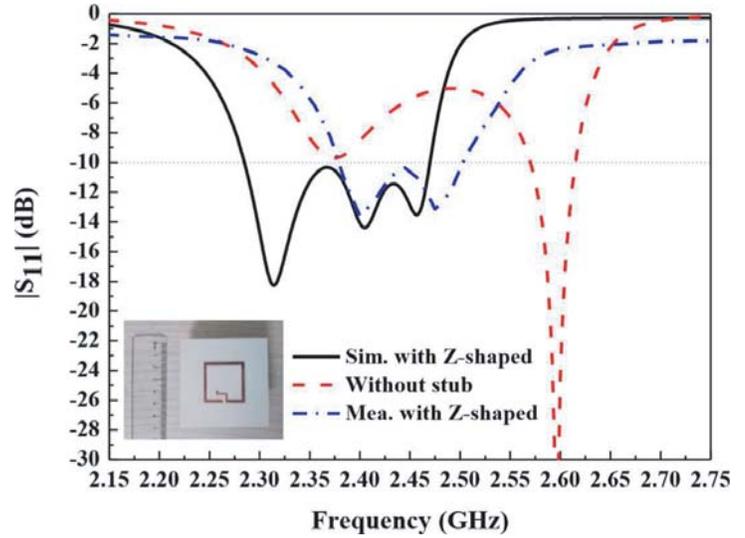
### 3. CP ANTENNA AND CHARACTERISTICS

#### 3.1. Optimized Antenna and Reflection Coefficients

In terms of the original antennas previously created using different discrete stub structures, further optimizations are conducted by combining all the discrete sheets and by slightly adjusting SSRR and antenna dimensions for CP performance. Considering the two dual-layer microstrip patch antennas with step- and L-shaped stubs, respectively, to have similar performances, both are linearly polarized antennas with comparable impedance bandwidth and radiation pattern, and they are not discussed here for the sake of brevity. The dual-layer microstrip patch antenna with Z-shaped stub exhibits CP performance, thus, further analysis for it is taken into account, and its optimized configuration is shown in Figure 5. Sizes of its parts are correspondingly listed. Its CP characteristics will be validated in the following sections.

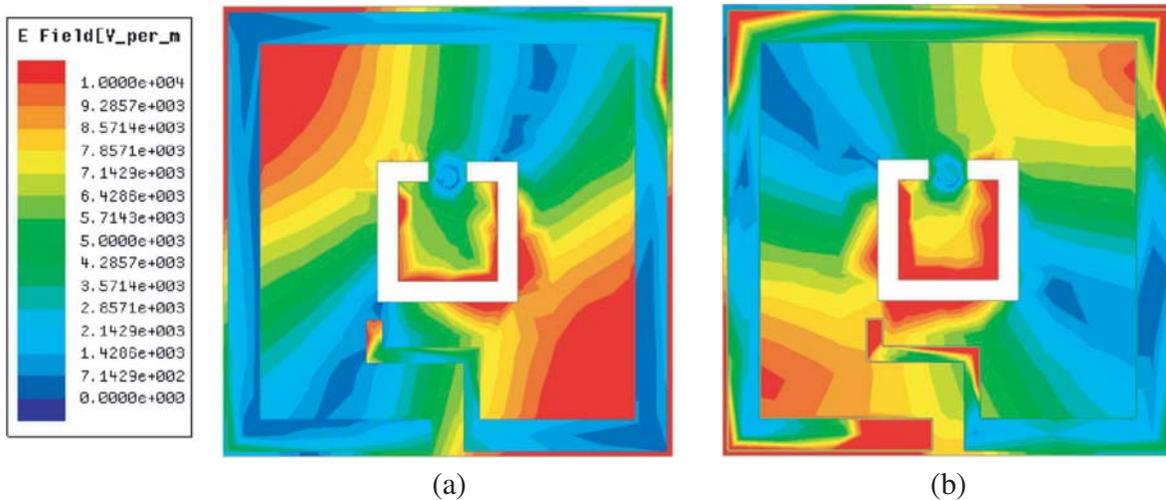


**Figure 5.** Optimized geometry of the proposed microstrip patch antenna. Partial sizes of antenna are listed as follows (unit: mm):  $L_1 = 60$ ,  $L_2 = 28.1$ ,  $L_5 = 8.8$ ,  $L_6 = 2.4$ ,  $L_7 = 4.5$ ,  $L_8 = 6.1$ ,  $L_9 = 1.7$ ,  $d = 3.4$ , and the thickness of the air gap is  $H_1 = 4.6$ .



**Figure 6.** Reflection coefficients of the proposed microstrip patch antenna with Z-shaped stub and the reference antenna without stub.

Figure 6 shows the simulated and measured  $|S_{11}|$  for the proposed microstrip patch antenna with a Z-shaped stub (the measurement is conducted by an Agilent E5063A vector network analyzer), along with its prototype photograph. For result of simulated dual-layer microstrip patch antenna with a Z-shaped stub, it can be observed that three resonant peaks are merged to form a fractional impedance bandwidth ( $|S_{11}| < -10$  dB) of 7.78% (2.285–2.47 GHz). The three resonances centered at 2.314, 2.4, and 2.456 GHz are, respectively, associated with the rectangular driven patch, SRR-shaped slot, and stacked SRR. For measured result, the fractional impedance bandwidth is 4.3% (2.385–2.49 GHz), which is formed by the merging of two resonant peaks. The narrower bandwidth and the other differences between the measured and simulated results are mainly due to fabrication error. In addition, certain values of simulated and measured  $|S_{11}|$  are high due to the weak electromagnetic coupling of thin SSRR for the impedance matching. For comparison, simulated  $|S_{11}|$  of the proposed microstrip patch antenna without the presence of the stub is provided, which has double bands centered at 2.374 and 2.596 GHz. However, there actually exist three resonances in the case of unloading Z-shaped stub; the frequency band corresponding to the SRR-shaped slot is merged into the first frequency band.



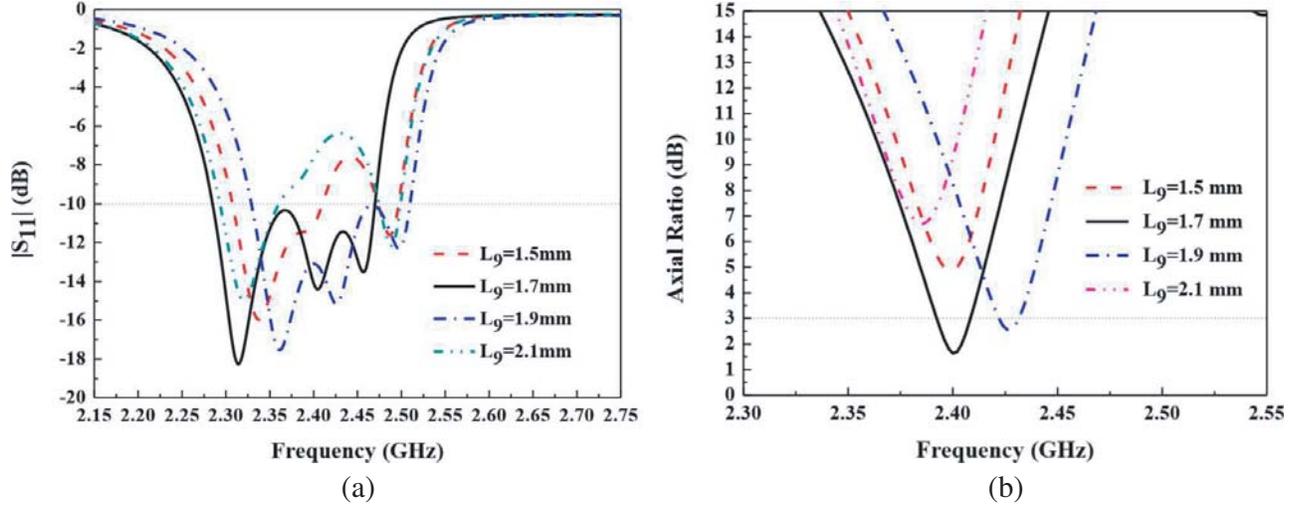
**Figure 7.** Simulated  $E$ -field distributions of the proposed microstrip patch antenna at the second and third resonance frequencies: (a) at 2.4 GHz, (b) at 2.456 GHz.

### 3.2. Operating Principle of CP Antenna

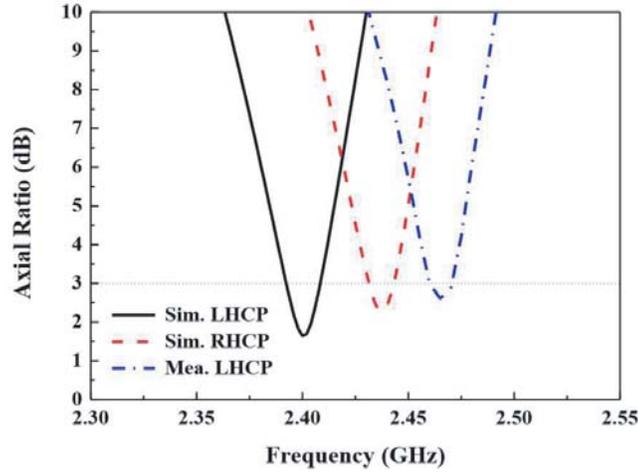
Figure 7 shows simulated  $E$ -field distributions of the proposed microstrip patch antenna at the second and third resonance frequencies: 2.4 and 2.456 GHz. As shown from Figures 7(a) and (b), the maximum  $E$ -fields of the two distributions are on the diagonal lines of the patches and orthogonal to each other. Based on this characteristic, when the corresponding two resonant modes are generated with equal amplitude and  $90^\circ$  phase difference, a CP microstrip patch antenna will be produced. It should be mentioned that when the designed CP antenna unloads the Z-shaped stub, the maximum  $E$ -fields are not orthogonal. This demonstrates that the Z-shaped stub can be used to introduce orthogonal modes; also, by tuning the amplitude and phase of the orthogonal modes, a circular polarization can be achieved. Because the resonance frequency of the  $45^\circ$ -polarized  $E$ -field is lower than the resonance frequency of the  $135^\circ$ -polarized  $E$ -field, and the phase of the  $45^\circ$ -polarized  $E$ -field is faster than the phase of the  $135^\circ$ -polarized  $E$ -field by  $90^\circ$ , the proposed microstrip patch antenna exhibits left-handed CP (LHCP) [7].

### 3.3. AR

Further investigation into CP performance of the proposed microstrip patch antenna is focused on its AR parameter. Figure 8 shows the impact of varied “ $L_9$ ” on the AR and  $|S_{11}|$ , and optimum value of 1.7 mm is chosen. It suggests that by tuning the Z-shaped stub to make the electromagnetic fields coupling to the lower driven patch properly, the antenna can obtain CP performance while maintaining impedance matching. Simulated and measured ARs of the proposed microstrip patch antenna are presented in Figure 9. For simulation, the proposed microstrip patch antenna has an AR (AR < 3 dB) bandwidth of 0.58% (2.393–2.407 GHz) with the minimum AR value of 1.64 dB at 2.4 GHz. For measurement, the AR bandwidth is 0.48% (2.46–2.472 GHz) with the minimum AR value of 2.6 dB at 2.465 GHz. It can be seen that the measured AR curve is shifted right and upwards relative to the simulated one. This difference can be attributed to the discrepancies between simulation and fabrication, such as material discrepancy. It is worth mentioning that when reversing the Z-shaped stub and connecting it to the other end of the split of SSRR, a right-hand circularly polarized (RHCP) antenna can be produced. The AR curve of the RHCP antenna is also shown in Figure 9, which demonstrates an AR bandwidth of 0.49% (2.431–2.443 GHz) with the minimum AR value of 2.25 dB at 2.438 GHz. The AR bandwidth is narrow, which is mainly attributed to the probe-feeding structure. It should be mentioned that the dimensions of the CP antenna can be adjusted to suitable values to make the AR frequency band of the antenna adapt to other applications, such as global positioning systems (GPS).



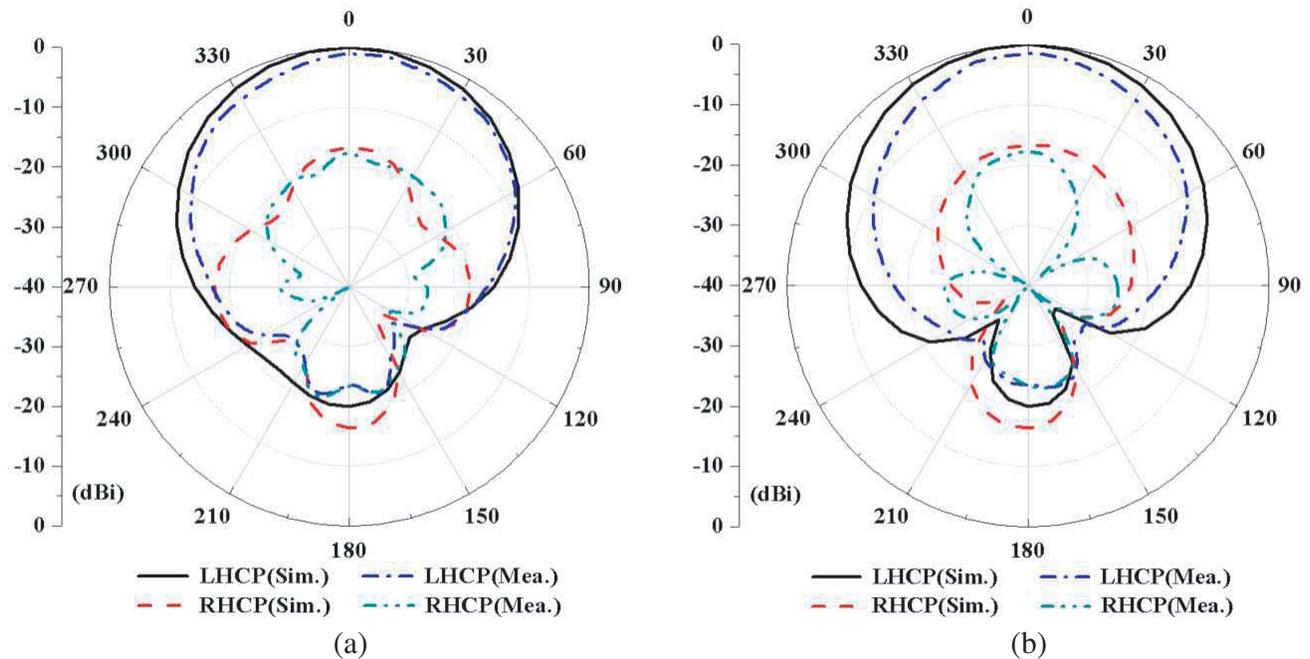
**Figure 8.** Impacts of different lengths of the terminal strip of the Z-shaped stub on the reflection coefficient ( $|S_{11}|$ ) and axial ratio (AR) of the proposed microstrip patch antenna. (a)  $|S_{11}|$ , (b) AR.



**Figure 9.** Measured AR curve of the proposed (LHCP) microstrip patch antenna and simulated ones of the LHCP and RHCP antenna (the RHCP antenna considered here is that the Z-shaped stub is reversed and connected to the other split end of the SSRR).

### 3.4. Radiation Patterns

The normalized simulated and measured two-dimensional radiation patterns of the proposed (LHCP) microstrip patch antennas are shown in Figure 10 (the measurement is conducted in a multi-probe spherical near-field test anechoic chamber). The observed frequency is at 2.4 and 2.465 GHz for simulation and measurement, respectively, which corresponds to the minimum AR value. The simulated results show that the LHCP microstrip patch antenna has a peak realized gain up to 6.98 dBi with cross-polarization  $-13.5$  dBi, and half-power beamwidth near  $75^\circ$ . Measurement shows a peak gain up to 5.87 dBi with cross-polarization of  $-10.9$  dBi, and half-power beamwidth near  $75^\circ$ . The differences between measurement and simulation can be attributed to fabrication and measurement tolerance, such as welding error at the feeding port. Additionally, the simulated gain of the proposed microstrip patch antenna is over 6.9 dBi within its operational frequency band, while the measured gain is over 4.6 dBi across its operational frequency band. The simulated radiation efficiency of the proposed antenna is over 90% throughout its operational frequency band.



**Figure 10.** Simulated and measured two-dimensional radiation patterns of the proposed (LHCP) microstrip patch antenna. The observed frequencies of simulation and measurement are at 2.4 and 2.465 GHz, respectively. (a)  $xz$  plane, (b)  $yz$  plane.

#### 4. CONCLUSION

A dual-layer microstrip patch antenna with a Z-shaped stub is designed by employing SA which aims to create stub structure for circular polarization. The design process based on SA is effectively implemented by the co-simulation of HFSS and MATLAB. The Z-shaped stub is generated on the SSRR of the antenna and results in two orthogonal modes through the electromagnetic coupling to the driven patch to achieve circular polarization. The resulting dual-layer microstrip patch antenna with a Z-shaped stub is LHCP with a narrow AR bandwidth. Simulated and measured results validate the feasibility of the CP design.

#### ACKNOWLEDGMENT

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