## Mode Splitting Based on the Coupling between Modes of Two Nanodisks Cavities and a Plasmonic Waveguide

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Abstract—A metal-insulator-metal (MIM) plasmonic waveguide coupled with two nanodisks as a resonator has been examined and numerically simulated with the finite-difference time-domain (FDTD) and analytically by the Temporal Coupling Mode Theory (CMT). Based on the three-level system, the strong destructive interference between the two resonators leads to the distinct mode splitting response. The characteristics of mode splitting show that there is anomalous dispersion with the novel fast-light feature at the resonance. Meanwhile, the slow light characteristic can also be achieved in the system at wavelengths of the split modes. The relationship between the transmission characteristics and the geometric parameters is examined. The results show that the modulation depth of the mode splitting transmission spectrum of 80% with 0.175 ps fast-light effect of resonance can be achieved, while for the two modes these values are around 30% with -0.18 ps slow light-effect. There is a good agreement between the FDTD simulated transmission features and CMT. The characteristics of the system indicate critical potential applications in integrated optical circuits such as slow-light and fast-light devices, optical monitoring, an optical filter, and optical storage.

### 1. INTRODUCTION

Plasmonics; The Promise of Highly Integrated Optical Devices play an important role in routing, switching and controlling of light in a large number of fields of modern optical communication and networks [1, 2]. In the plasmonic waveguides there is a coupling between the transferred electromagnetic waves and the surface collective oscillations of free electrons in a metal; therefore, it is known by Surface Plasmon Polaritons (SPPs). The SPP waves are bound to and propagate along the metal-dielectricmetal interfaces [2]. The light confinement below the diffraction limit is the competitive advantage of plasmonic waveguide compared to other types of optical waveguides such as photonic crystals, optical fibers, etc. Furthermore, the introduction of deep-submicron technologies in electronic engineering leads to a revolution in optoelectronic circuits [3] and membrane technology [31]. A Huge number of structures are introduced by transporting SPPs such as grooves and wedges [4, 5], Domino plasmon waveguide [6, 7], Metal-Insulator-Metal waveguides (MIM) [8], and thenano-particle plasmon waveguides [9]. In addition to the high degree of SPP confinement, compact size and fabrication simplicity have made MIM geometry the most used structure among other nano-scale waveguides [10]. Different types of plasmonic filters such as tooth-shaped subwavelength and add-drop topologies are introduced and analyzed by numerical methods such as Finite-Difference Time-Domain (FDTD) and finite element method (FEM) [11, 12]. It has been shown that the transmission spectra of these structures can generate a narrow bandpass filter [12]. Moreover, ring resonator filters generate opposite phase standing waves using optical cavities, for use in the suppression of some specific wavelengths in the transmission spectrum [13]. Depending on the position of cavities relative to the main MIM guiding structure, it is possible to achieve bandpass (two parallel MIM waveguides coupled to each other by a circular ring resonator) or band-stop filters (two

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MIM waveguides at the same line separated by a circular ring resonator) [14]. One of the most important applications of MIM waveguides that have been the subject of many recent papers is the construction of integrated plasmonic optical filters by cavity waveguide coupling [14, 15]. Coupled Mode Theory (CMT) [16] and numerical methods [17, 18] are used for the analysis of such structures. Optical filters, as the most important building block of integrated optical circuits, are recently introduced in different geometries such as bidirectional splitter in different angles of incident light [19], plasmonic mode splitter based on the MIM waveguide with periodic grooves [20] and wavelength de-multiplexer based on MIM plasmonic nano-capillary resonators [21]. However, there are some limits in these structures such as huge dimensions to splitting functionality, low transmittance, power leakage, and maximum fanout of two for splitter channels [19–21].

Mode splitting of surface plasmon resonance has a great significance in many applications especially in integrated optics. Different structures are proposed to achieve mode splitting such as mode splitting in a super-period metal nanohole array grating [22]. But the transmission values of the split modes are much different. This paper introduces a novel nanoscale plasmonic mode splitting while its functionality is verified by CMT and FDTD in different configurations. This paper is organized as follows. Section 2 introduces the CMT Design of two nanodisks coupled with the plasmonic waveguide. Section 3 describes the FDTD modeling of proposed structure and introduces the numerical results. The transmission characteristics with varying geometric parameters are introduced in Section 4. Finally, Section 5 summarizes our concluded remark.

# 2. CMT DESIGN OF TWO NANODISKS COUPLED WITH PLASMONIC WAVEGUIDE

The MIM plasmonic waveguide coupled with a nanodisk resonator shown in Fig. 1 is a well-known structure, and the nanodisk is to satisfy the theoretical resonant equation given by [23]

$$k_{d}\left(H_{n}^{(1)'}(k_{m}R) \middle/ H_{n}^{(1)}(k_{m}R)\right) = k_{m}\left(J_{n}^{(1)'}(k_{d}R) \middle/ J_{n}^{(1)}(k_{d}R)\right)$$

$$k_{d,m} = k\sqrt{\varepsilon_{d,m}}$$
(1)

where k is the wave number, and it includes a relatively small negative imaginary part which stands for the loss.  $k_{d,m}$  are the wave vectors in the metal and the dielectric nanodisk, respectively.  $\varepsilon_d$  is the relative dielectric constant of the dielectric and  $\varepsilon_m$  the relative dielectric constant of the metal, which can be obtained from the Drude model. R represents the radius of the nanodisk cavity.  $H_n$  and  $H'_n$ are the first kind Hankel function with order n and its derivation, and  $J_n$  and  $J'_n$  are the first kind Bessel function with order n and its derivation, respectively. The first and second orders of Bessel and Hankel functions correspond to the first- and second-order modes that resonate inside the nanodisk. It is obvious from Eq. (1) that the resonance wavelength  $\lambda_0$  depends on radius R and the refractive index. The width of the bus waveguide is set at  $d = 0.05 \,\mu\text{m}$  which is small enough compared to the wavelength of the incident light. Therefore, only the fundamental mode of the waveguide is taken into consideration [24]. As the signal passes through the system, the wavelength which satisfies the resonant condition of the nanodisk, Eq. (1), will be confined in the nanodisk and coupled back into the waveguide output. So, the obvious stop-pass filtering effect should be observed in the waveguide-resonator system, as shown in Fig. 2. As expected, the light can be confined in the resonator when the wavelength of  $\lambda$ is equal to 1.084 µm, and the corresponding transmission dip of 30% can be achieved.



Figure 1. A schematic diagram of the single nanodisk coupled to plasmonic waveguide.



**Figure 2.** (a) Transmission spectrum of the proposed structure in Figure 1 with R = 276 nm,  $g_1 = 11$  nm, (b)–(d) contour map of the magnitude of the magnetic field distribution for the structure.

To make this phenomenon more clear, the magnitudes of the magnetic field distributions at wavelengths  $\lambda = 1.038, 1.158$ , and  $1.084 \,\mu\text{m}$  are displayed in Figs. 2(b), (c) & (d). It is obvious from these figures that the energy is highly coupled into the nanodisk at the resonance wavelength result in the weak magnetic distributions in the bus waveguide (see Fig. 2(d)).

#### 2.1. Mode Splitting Based on the Plasmonic Waveguide Coupled with Two Nanodisks

The proposed schematic illustration of the new system is shown in Fig. 3. Compared with Fig. 1, the only difference is that we add a new nanodisk on the top of nano resonator. The radius of this new nanodisk is assumed to be equal to the radius of the first one. The material of the bus waveguide and the two nanodisks are assumed to be air. The background metal is silver, and its dispersive permittivity can be denoted by the Drude model [24]

$$\varepsilon\left(\omega\right) = \varepsilon_{\infty} - \omega_{p}^{2} / \left(\omega^{2} + i\omega\gamma\right) \tag{2}$$

where  $\omega$  is the angular frequency of the incident light,  $\varepsilon_{\infty}$  the dielectric constant at an infinite angular frequency and equals 3.7,  $\omega_p$  the bulk plasma frequency and equals 9.1 eV, and  $\gamma$  the electron collision frequency equals 0.018 eV. The surface plasmon polaritons (SPPs) is excited at the metallic surface and confined in the plasmonic waveguide when a TM light is entered into the waveguide [25]. When the SPPs waves go through the waveguide, the energy can be coupled directly into the first nanodisk and then coupled between the first and second nanodisks.



Figure 3. A schematic diagram of double nanodisks coupled to plasmonic waveguide.

In CMT, an overall system is described in terms of a set of weakly coupled components which can be analyzed using general principles [22]. A cavity, for example, is treated as an oscillator in the time. For the SW cavity (such as a nanodisk) coupled to a waveguide, its cavity mode decays equally into the forward and backward propagating waveguide modes, while for a TW cavity (such as a ring), the cavity mode decays in only one direction due to momentum matching [26]. For characterizing a nanodisk, we define the following parameters:  $\omega_0(\lambda_0)$  is the resonant frequency (wavelength);  $A_1\&A_2$  are the mode amplitudes of first and second nanodisks, respectively;  $S_{1,in}, S_{2,out}, S_{1,out}$  are the incident/transmitted/reflected waveguide mode amplitudes, which are normalized such that their squared values correspond to the incident/transmitted/reflected/dropped power;  $1/\tau_{i1}$ ,  $1/\tau_{i2} \& 1/\tau_w$  are decay rates due to intrinsic loss for the two nanodisks and waveguide coupling loss, respectively;  $Q_{i1}, Q_{i2} \& Q_w$  are cavity quality factors related to intrinsic loss at the nanodisks and the waveguide coupling loss, respectively;  $Q_t$  is total quality factor  $(1/Q_t = 1/Q_{i1} + 1/Q_{i1} + 1/Q_w)$ . Here,  $Q_w$  denotes the nanodisk-waveguide coupling and is referred to as "waveguide coupling quality factor", whereas  $Q_c$ represents the nanodisk-nanodisk coupling and is referred to as "disk coupling quality factor". The decay rates relate to the cavity quality factors by  $Q_{ie} = \omega_0 \tau_{ie}/2$ ; (e = stands for 1 or 2) and  $Q_w = \omega_0 \tau_w/2$ . And the coupling coefficient between the two cavity modes is denoted by  $\tau_c$  which relates to disk coupling quality factor by  $Q_c = \omega_0 \tau_c/2$ .  $\delta$  is used to normalize the frequency  $\omega$ , which is defined by  $\delta = (\omega - \omega_0)/\omega_0$ , and  $t = S_{2,out}/S_{1,in}\&r = S_{1,out}/S_{1,in}$  to denote transfer functions for the transmitted port and the reflected port, respectively. The transmission T, effective phase shift  $\theta$  and group delay  $\tau$  can be calculated as  $T = abs(t^2), \theta = \arg(t)$  and  $\tau = d\theta(\omega)/d\omega$ , respectively. The CMT equations are given as follows:

$$\frac{dA_1}{dt} = \left(j\omega_0 - \frac{1}{\tau_{i1}} - \frac{1}{\tau_w}\right)A_1 + \sqrt{\frac{1}{\tau_w}S_{1,in} - j\mu A_2}$$
(3)

$$\frac{dA_2}{dt} = \left(j\omega_0 - \frac{1}{\tau_{i2}}\right)A_2 - j\mu A_1 \tag{4}$$

Due to energy conservation, the relationship of the incoming and outgoing lights in the bus waveguide can be denoted as

$$S_{1,out} = S_{2,in} + j\sqrt{\alpha}A_1 \tag{5}$$

$$S_{2,out} = S_{1,in} + j\sqrt{\alpha}A_1 \tag{6}$$

If a sinusoidal harmonic oscillation,  $e^{-i\omega t}$ , is assumed, then  $dA/dt = -i\omega A$ . Plugging this and  $S_{2,in} = 0$  into Equations (3) and (4), the transfer function  $t = S_{2,out}/S_{1,in}$  can be obtained as follows:

$$t = 1 - \frac{j\delta\omega_0\tau_w + \tau_w/\tau_{i2}}{\left(\frac{2}{\tau_c}\right)^2 + \left(j2\delta\omega_0 + \frac{1}{\tau_{i1}} + \frac{1}{\tau_{i2}} + \frac{1}{\tau_w}\right)^2 - \left(\frac{1}{\tau_{i1}} - \frac{1}{\tau_{i2}} + \frac{1}{\tau_w}\right)^2}$$
(7)

It is useful to write this transfer function in terms of quality factors Q instead of  $\tau$ 

$$t = 1 - \frac{\left(j2\delta + 1/Q_{i2}\right)/Q_w}{\left(\frac{1}{Q_c}\right)^2 + \left(j2\delta + \frac{0.5}{Q_{i1}} + \frac{0.5}{Q_{i2}} + \frac{0.5}{Q_w}\right)^2 - \left(\frac{0.5}{Q_{i1}} - \frac{0.5}{Q_{i2}} + \frac{0.5}{Q_w}\right)^2}$$
(8)

For simplicity, let  $\tau_{i2} = 0$  or  $Q_{i2} = \infty$ . From Eq. (8) and the definition of transmission T, we can obtain an expression of T as

$$T = 1 - \frac{\delta^2 \left( 2/Q_{i1}Q_w + 1/Q_w^2 \right)}{\delta^2 \left( 1/Q_{i1} + 1/Q_w \right)^2 + 4 \left( \delta^2 - 1 / \left( 2Q_c^2 \right)^2 \right)^2}$$
(9)

Two conclusions can be drawn from Eq. (9): (1)  $T(\omega_0) = 1$ , meaning that complete transparency can be obtained in the transmission spectrum; (2) T achieves minimum at  $\delta = 1/2Q_c$ .

Figure 4 plots the transmission, phase shift and group delay for this system extracted from Eqs. (8) & (9). It can be seen from this figure that when there is no direct coupling,  $Q_c \gg$ , the dispersion is abnormal, and fast-light occurs at resonance. As the direct coupling increases, the mode splitting



**Figure 4.** Illustration of the transmission, phase shift and group delay of cavities for the structure of Figure 3.

becomes obvious, and the dispersion changes to normal around the resonance. It can also be seen that the delay is quite large at the resonance, which is obviously demonstrated in Fig. 4(c) when  $Q_c = 39.3$ . Note that no complete transparency is achieved because we consider the values of  $Q_{i2}$  and  $Q_{i1}$  which represent the loss of mode  $A_1$  and  $A_2$ , not high enough.

#### 3. FDTD MODELING AND NUMERICAL RESULTS

In this section, we investigate the mode splitting properties of the nanocavities resonators in a twodimensional (2D) plasmonic waveguide with Ag-air-Ag interfaces using a finite-difference-time-domain (FDTD) method [17] and perfectly matched-layer (PML) as an absorbing boundary condition (ABC). In our numerical calculations with FDTD, the nanocavities resonators are described by a spatial discretization grid. A spatial grid size of  $\Delta x = \Delta y = 2$  nm in the FDTD algorithm is found sufficient for convergence of the numerical results. Calculations in FDTD are performed according to the steps listed in Fig. 5 [27].





Our system is made up of a 2D box (along the x- & y-axes) with propagation along the x-axis. UPML boundary conditions are applied at both boundaries in y and x of the box in order to eliminate the reflection of outgoing waves [27]. 200 nm width for the PML is found to be thick enough to fully absorb outgoing waves. The structure is supposed to be infinite along the z-direction. The equations of motion are solved with a time integration step  $\Delta t = (\Delta x/4c) = 1.7 \times 10^{-3}$  fs to avoid the problems of numerical dispersion and stability. The number of time steps is equal to  $2^{16}$ , which is the necessary tested time for good convergence of the numerical calculations.

The first group of simulated results is presented in Fig. 2. The transmission spectrum of MIM waveguide coupled with the first nanodisk whin  $g_2 = 50 \text{ nm}$  is plotted. By this value of  $g_2$ , there is no

coupling between the two nanodisks,  $Q_c \gg$ . Therefore, this case represents only one nanodisk coupled to the plasmonic waveguide. Fig. 2 shows the contour map of the magnitude of Hz at three different wavelengths: 1.038, 1.158, and 1.084 µm.

What is shown in this figure can be explained as follows. As the optical signal passes through the waveguide, the wavelength of the incident light, which satisfies the resonant condition of the nanodisk, can be confined in the nanodisk and coupled back into the waveguide output. So, the obvious notch filtering effect should be observed in the waveguide-resonator system as shown in Fig. 2(a). As expected, the light is confined in the resonator when the wavelength equals  $1.084 \,\mu\text{m}$ , and the corresponding transmission dip of 0.3 can be achieved. This phenomenon can be clarified by the magnetic field distribution of the mode at wavelengths: 1.038, 1.158, and  $1.084 \,\mu\text{m}$  in Figs. 2(b), (c), (d). It is obvious from Figs. 2(b), (c) that the energy is highly coupled into the bus waveguide resulting in the weak magnetic distributions in the nanodisk. On the other hand, for Fig. 2(d) which represents the resonance of the nanodisk, the energy is highly coupled into the nanodisk resulting in weak magnetic distributions in the waveguide.

The second group of simulated results is presented in Fig. 6. The transmission spectrum of MIM plasmonic waveguide coupled with the two nanodisks is shown in Fig. 6(a). One can find that the transmission value at the resonance is very high compared to its counterpart results shown in Fig. 2(a). Simultaneously, two new transmission dips with wavelengths of 1.056 and 1.113 µm are formed. The corresponding transmission dip of the splitmode transmission spectrum is near 0.4. In addition, the corresponding magnetic field distribution of several key wavelengths is shown in Figs. 6(b)–(d). The reason that the transmission is low at  $\lambda = 1.056$  and 1.113 µm is the destructive interference at waveguide between the electromagnetic energy coming from the first nanodisk which acts as a pump signal [28] and the electromagnetic energy propagating in the waveguide, as shown in Figs. 4(b), (c). By the same interpretation, for  $\lambda = 1.084 \,\mu$ m which is also the resonance wavelength of the second nanodisk the destructive interference occur here at the first nanodisk between electromagnetic energy coupled from the second nanodisk which acts as a pump signal [28] and the electromagnetic energy coupled from the second nanodisk which acts as a pump signal [28] and the electromagnetic energy coupled from the second nanodisk which acts as a pump signal [28] and the electromagnetic energy coupled from the second nanodisk which acts as a pump signal [28] and the electromagnetic energy coupled from the waveguide result in approximately no coupling between the waveguide and the two nanodisks.



Figure 6. (a) Transmission spectrum of the proposed structure in Figure 3 with R = 276 nm,  $g_1 = 11$  nm,  $g_2 = 15$  nm, (b)–(d) contour map of the magnitude of the magnetic field distribution for the structure.

The above results and interpretations permit the use of the concept of three-level energy diagram system [28, 29] to unravel the physical origin of the mode splitting behavior. To do this, recall from [28, 29] the electromagnetically induced transparency EIT equation

$$T_{ab} = 1 - \Omega_1^2 \Gamma \Delta^2 / \left[ \left( \Gamma \Delta \right)^2 + 4 \left( \Delta^2 - \Omega_2^2 / 4 \right)^2 \right]$$
(10)

where  $\Omega_1$  and  $\Omega_2$  are respective Rabi frequencies of probe field and pump field;  $\Gamma$  is decay rate;  $\Delta$  is the detuning of the probe field from atomic resonance. It can be seen that Eq. (9) is identical to the

#### Progress In Electromagnetics Research M, Vol. 55, 2017

EIT equation if we regard  $\omega_0 \delta \to \Delta$ ,  $\omega_0(1/Q_{i1} + 1/Q_w) \to \Gamma$ , and  $\omega_0/Q_c \to \Omega_2$ . Therefore, as shown in Fig. 7, the incident waveguide is considered as the ground state  $|1\rangle$ . The first nanodisk coupled directly to the waveguide acts as a bright resonator with the radiative plasmonic state  $|2\rangle$ . The second nanodisk cannot be excited directly by the incident light and behaves as a dark resonator with the dark plasmonic state  $|3\rangle$ . The state  $|2\rangle$  is coupled to the ground state  $|1\rangle$  by a bright dipole-allowed transition with resonance frequency  $\omega_0$ . At the same time, it is coupled to a dark state  $|3\rangle$ , which might be detuned by a shift  $\delta$ . The direct path  $|1\rangle - |3\rangle$  is forbidden. The second nanodisk is excited only by near-field coupling with the first nanodisk corresponding to  $|2\rangle - |3\rangle$  path. However, the coupling of the levels  $|2\rangle$ and  $|3\rangle$  allows for a population of state  $|3\rangle$ , which will cause a back action and an excitation of level  $|2\rangle$ . According to the distributions of the magnetic field  $H_y$  shown in Fig. 6(d), the realization of the mode splitting response results from the strong destructive interference between two propagation pathways: the direct transition  $|1\rangle - |2\rangle$  and the indirect one  $|1\rangle - |2\rangle - |3\rangle - |2\rangle$ .



Figure 7. Three-level model scheme of the plasmonic system.

As shown in Fig. 6(d), the filed in the nanodisk is extraordinarily suppressed due to the strong destructive interference. This destructive interference lets the first nanodisk act as a null with respect to the waveguide, and hence the SPP power is passed to the waveguide output, which is a direct evidence of the outstanding transmission window at the resonance wavelength. For the new transmission nulls, however, the first nanodisk is directly excited by the incident SPPs. For the second nanodisk excited from the first one, the coupling is enhanced at one null (in-phase coupling) and degrades at the other null (out-phase coupling). The in-phase coupling resonance occurs between the two nanodisks at  $\lambda = 1.056 \, upmum$  (see Fig. 6(b)) whereas the out-phase coupling forms at  $\lambda = 1.113 \, \mu m$  (see Fig. 6(c)). The incident SPP power can be coupled back into the waveguide by the first nanodisk, resulting in the newly appearing transmission nulls. Therefore, the presence of the second nanodisk can prevent the confinement and absorption of the SPP power which is absorbed previously by the first nanodisk resonance, thereby, achieve the novel mode splitting response.

# 4. THE TRANSMISSION CHARACTERISTICS WITH VARYING GEOMETRIC PARAMETERS

In order to study the relationship between the two transmission nulls and the geometric parameters, we investigate the transmission properties with the parameters of different R and  $g_2$ , respectively. Fig. 8 shows the transmission spectra of the proposed structure with different R when  $g_1 = 11$  nm and  $g_2 = 15$  nm. It can be seen that the transmission dips 1 and 2 shift to long wavelength when R increases; meanwhile, the depth transmissivity of dip 1 increases and that of dip 2 decreases. The full-width at half maximum (FWHM) of dip 1 is also decreased when R increases; meanwhile, the FWHM of dip 2 increases, as shown in Fig. 8. This can be explained as follows, by increasing R, the out-phase coupling which controls the first dip degrades hence less capable of making the destructive interference. As a result, the depth of dip 1 will decrease. On the other hand, the in-phase coupling which controls the second dip increases then more capable of making the destructive interference. As a result, the depth of dip 1 will decrease. On the other hand, the in-phase coupling which controls the second dip increases. Also, the enhancement in coupling will cover a shorter band of wavelengths resulting in a decrease in FWHM, and vise verse for the degradation in the coupling. The results show that one can control the modulation depth and FWHM by adjusting R. Moreover, the opposite



Figure 8. Transmission spectrum of the proposed structure with different R when  $g_1 = 11$  nm,  $g_2 = 15$  nm.



**Figure 9.** Transmission spectrum of the proposed structure with different  $g_2$  when R = 276 nm,  $g_1 = 11$  nm.



Figure 10. (a) Simulated transmission phase shift, (b) optical delay time and (c) group indices with  $R = 276 \text{ nm}, g_1 = 11 \text{ nm}, g_2 = 15 \text{ nm}.$ 

variation characteristics of dip 1 and dip 2 with R indicates that this structure can be used in many different applications such as monitoring applications.

Figure 9 shows the transmission spectra of the proposed structure with different  $g_2$  when R = 276 nm,  $g_1 = 11$  nm. As we can see, the transmission dip 1 shifts to the long wavelengths; meanwhile, dips 2 shifts to short wavelengths when  $g_2$  increases. The results of this figure can be easily interpreted as follows: the transmission spectrum tends to form one dip from the two dips with the increase of  $g_2$ ; the coupling between the two nanodisks decreases

The above system can not only work as a high-performance notch filter and ultra-high-performance mode splitting effect but also support the slow and fast group velocities. Slow- and fast-light effects are

#### Progress In Electromagnetics Research M, Vol. 55, 2017

an important index, and it can be described by the group index  $n_q$  [30]

$$n_g = \frac{c}{v_q} = \frac{c}{H} \tau_g = \frac{c}{H} \frac{d\theta\left(\omega\right)}{d\omega} \tag{11}$$

where,  $v_g$  and  $\tau_g$  stand for the group velocity and the optical delay time in the selected structure, respectively. c represents the speed of light.  $\theta(\omega)$  is the transmission phase shift and H the length from the light source to the detector. By means of detecting the transmission phase shift and a serial of calculations based on the above definitions of the group delay, we numerically investigate, with  $g_1 = 11 \text{ nm}$ , R = 276 nm,  $g_2 = 15 \text{ nm}$ , the optical group delay. Fig. 1 shows the transmitted phase shift ( $\theta(\omega)$ ) between the waveguide input and output, group delay time ( $\tau_g$ ), and group index. It is clear from Fig. 10(a) that the phase slope is negative and steepest around the resonance wavelengths of different modes. It can be seen from Fig. 10(b) that the optical delay is negative at resonance and positive at wavelengths of the split modes; fast-light occurs at resonance and slow light at wavelengths of the splitted modes.

### 5. CONCLUSION

In summary, a plasmonic coupling system consisting of MIM bus waveguide and two nanodisks as resonators is investigated both numerically and theoretically. The novel mode splitting effects with fast-light feature at resonance and slow-light feature at the splitting modes are realized respectively in the new structure. Such novel fast- and slow-light characteristics originate from the extreme destructive interference between the two nanodisks resonators. In this paper, the simulated results are verified by the CMT. This structure will open up a new opportunity to develop slow- and fast-light techniques and play a vital role in the integrated optical devices such as optical switching, monitoring, and optical storage.

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