

## Compact EBG Structures for Reduction of Mutual Coupling in Patch Antenna MIMO Arrays

Mohammad Naser-Moghadasi<sup>1</sup>, Rahele Ahmadian<sup>2</sup>, Zahra Mansouri<sup>3, \*</sup>,  
Ferdows B. Zarrabi<sup>4</sup>, and Maryam Rahimi<sup>2</sup>

**Abstract**—Electromagnetic band gap (EBG) structures are usually realized by periodic arrangement of dielectric materials. These periodic structures can help in the reduction of mutual coupling in array antennas. In this paper a new arrangement of EBG structures is presented for reducing mutual coupling between patch antenna MIMO arrays. The patch antennas operate at 5.35 GHz which is defined for wireless application. Here  $2 \times 5$  EBG structures are used to reduce mutual coupling more than 20 dB. The total size of the antenna is  $36 \text{ mm} \times 68 \text{ mm} \times 1.6 \text{ mm}$ . So it is more compact in than pervious research. Experimental results of return loss and antenna pattern have been presented for 5.4 GHz and compared with HFSS simulation results. Also the EBG structures have been designed with numerical modeling and dispersion diagram. New EBG model is compared with conventional EBG model, and equivalent circuit model is given for new structure.

### 1. INTRODUCTION

Recently, in next-generation wireless communication systems, there is high demand for high data transfer rate and fast access with best quality for cellular connection by MIMO (multi-input-multi-output) communication [1]. In the last two decades, different protocols have been defined by IEEE to improve wireless access for voice communication in cellular phone such as GSM 900 or GSM 1800, WLAN for high rate data communication in narrow band, UWB system such as IEEE 802.11a for 5.15–5.825 GHz and FCC in 3.1–10.6 GHz UWB range [2]. Microstrip antenna is a popular type of antenna for its good features such as planar structure, low cost, easy fabrication, ability to use in integrated circuits and compact devices. Microstrip antennas are appropriate for array form antenna and MIMO systems, and it has been noticed because of easy feed [3]. In some applications, size reduction of microstrip antenna is needed, and some methods are introduced for this aim [3]. One way is to use metamaterial structures such as CRLH and EBG to reduce the size of the microstrip antenna [2–4]. Metamaterials have some unusual properties such as anti-parallel phase, group velocities, and negative reflection index. Metamaterials are known as artificial structures and do not exist in natural situation [5].

In metamaterial structures, electric field, magnetic field and wave vector follow left-hand rule, so they are called left-handed materials (LHM). They have negative permittivity and permeability, so they are also called double negative (DNG). Thus, in some structures only one of them is negative. Metamaterials make it possible to design a miniaturized, multi-band antenna, filter or other microwave devices [5].

EBG structures are defined as a kind of artificial magnetic conductor (AMC) that prevent/assist the propagation of electromagnetic waves in a specified band of frequency for all incident angles and

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*Received 16 August 2014, Accepted 15 September 2014, Scheduled 22 September 2014*

\* Corresponding author: Zahra Mansouri (zm.mansouri@gmail.com).

<sup>1</sup> Department of Electrical and Computer Engineering, Sciences and Research Branch, Islamic Azad University, Tehran, Iran. <sup>2</sup> Young Researchers and Elite Club, South Tehran Branch, Islamic Azad University, Tehran, Iran. <sup>3</sup> Department of Electrical Engineering, Khodabandeh Branch, Islamic Azad University, Khodabandeh, Iran. <sup>4</sup> Faculty of Electrical and Computer Engineering, University of Tabriz, Tabriz, Iran.

all polarization states [6, 7]. Coupling reduction in antennas and specially in array antennas is very important in MIMO system that has been considered by EMI. For this aim, absorbers and other common EBG structures can be used to reduce coupling. Metamaterials are used in ideal absorber structures and electromagnetic shields to prevent electromagnetic waves propagation [8–10]. Many different shapes and arrangements of metamaterials such as DGS [11], spiral electromagnetic band-gap (SEBG) [12], slotted-complementary split-ring resonators [13] and crossed-meander-line slit [14] have been suggested to improve coupling and shielding factor. Also, many studies in application of metamaterials in different forms have been noticed to reduce mutual coupling between antennas. EBG structures are also used to reduce mutual coupling between planar microstrip patch antennas. Among the various attempts, the mutual coupling is reduced by 18 dB, and radiated power is decreased 60% using metamaterial structure in ground plane by Salehi and Tavakoli [15].

Coupling between the microstrip antenna arrays is the essential problem that always exists. To solve the problem, metamaterial development is used in a rectangular patch antenna array substrate in order to reduce coupling between array antennas [16–18]. EBG structure is the most popular element, which consists of metal or dielectric periodic structures, and shows characteristics of band-pass or band-stop [19] and makes isolation between components [20]. They can be used in other applications such as to reduce coupling between two parallel plate waveguides up to 20 dB and suppression of surface wave between other structures, and it has been noticed by Mohajer-Iravani et al. to reduce coupling of patch and aperture [21]. Various forms of planar EBGs, such as mushrooms and fractal shapes, are introduced to expand the bandwidth, phase characteristics and improvement of gain. Also studies on equivalent circuits have been performed to modify bandwidth [22–24]. As described in [22] because the surface wave propagate along the  $E$ -plane direction, EBG structure has strong effect in reducing the surface wave in  $E$ -plane condition, and through it, the coupling between antennas will be reduced. On the other hand, for  $H$ -plane state EBG cells have a weak role in reducing mutual coupling.

Coupling coefficient is calculated by the following equation [25]:

$$|C|^2 = \frac{|S_{21}|^2}{(1 - |S_{11}|^2) \times (1 - |S_{22}|^2)} \quad (1)$$

In this paper, a novel effective EBG structure is suggested to reduce mutual coupling between patch antenna arrays. The patch antennas operate at 5.35 GHz which is attractive frequency for wireless applications. We have used  $2 \times 5$  EBG structures to reduce mutual coupling more than 20 dB. Here cells in a row are joint to improve the mutual coupling. ZOR dispersion diagram is used for conventional EBG, and then the effect of the slots is studied. The  $E$ -plane and  $H$ -plane patch coupling is studied with prototype EBG and surface current distribution with and without EBG structure emphasizes the effect of the EBG on mutual coupling.

## 2. EBG MODELING AND NUMERICAL METHOD

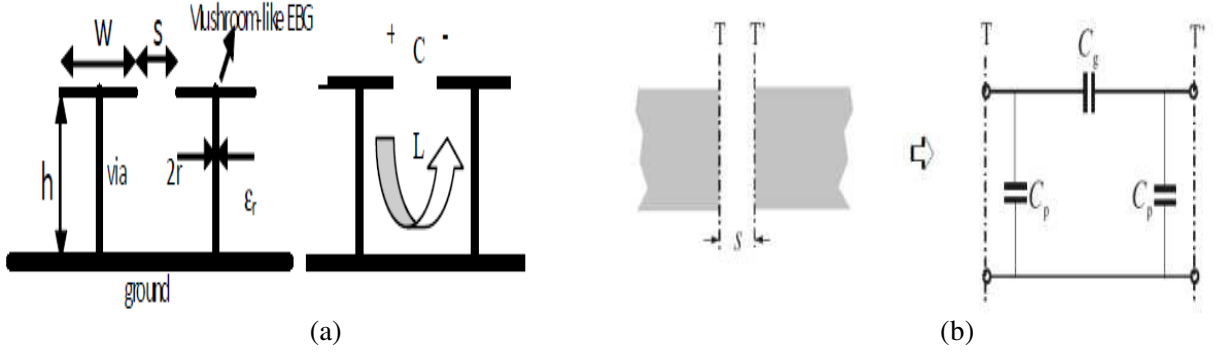
Figure 1(a) shows how inductance ( $L$ ) and capacitance ( $C$ ) are determined by conventional EBG structure. Resonant behavior is used to explain the features of the EBG band gap structure. This model is not very accurate because of simple approximation of  $C$  and  $L$  [26]. Parameters of the EBG structure in Fig. 1(a) are patch width  $W$ , gap width  $S$ , substrate thickness  $h$ , via radius  $r$  and dielectric constant  $\epsilon_r$ . When the periodic length of structure ( $W + S$ ) is small compared to the wavelength, the mechanism of EBG structure can be explained by a model of the compact LC elements. As shown in Fig. 1, equivalent capacitor is obtained by the gap between the patches and current through the adjacent patches [26]. Fig. 1(b) demonstrates microstrip gap structure that includes a coupling series and parallel capacitor between the patch and the ground plane, respectively. The value of this capacitor can be calculated by [28–29].

Impedance and resonant frequency of a parallel  $LC$  circuit can be obtained as follows:

$$Z = \frac{j\omega L}{1 - \omega^2 LC} \quad \omega_0 = \frac{1}{\sqrt{LC}} \quad (2)$$

For a simple patch, the edge capacity of a narrow gap is calculated as [27]:

$$C = \frac{W\epsilon_0(1 + \epsilon_r)}{\pi} \cosh^{-1} \left( \frac{W + S}{S} \right) \quad (3)$$



**Figure 1.** EBG structure and gap. (a) Model for the compact  $LC$ . (b) Microstrip gap structure and its equivalent circuit.

$$L = \mu h \quad (4)$$

According to the following equations, the parameters that affect the value of the series capacitors are length ( $s$ ) and gap width ( $w$ ). The series capacitor gets larger with smaller gap length.

$$C_p = 0.5C_e \quad (5)$$

$$C_p = 0.5C_e \quad (6)$$

$$C_g = 0.5C_o - 0.25C_e \quad (7)$$

$$\frac{C_o}{W} (\text{pF/m}) = \left(\frac{\epsilon_r}{9.6}\right)^{0.8} \left(\frac{s}{W}\right)^{m_o} \exp(K_o) \quad (8)$$

$$\frac{C_e}{W} \left(\frac{\text{pF}}{m}\right) = 12 \left(\frac{\epsilon_r}{9.6}\right)^{0.9} \left(\frac{s}{W}\right)^{m_e} \exp \exp(K_e) \quad (9)$$

$$\begin{cases} m_o = \frac{W}{h} \left[ 0.619 \log \log \left(\frac{W}{h}\right) - 0.3853 \right] \\ K_o = 4.26 - 1.453 \log \left(\frac{W}{h}\right) \end{cases} \quad \text{for } 0.1 \leq s/W \leq 1.0 \quad (10)$$

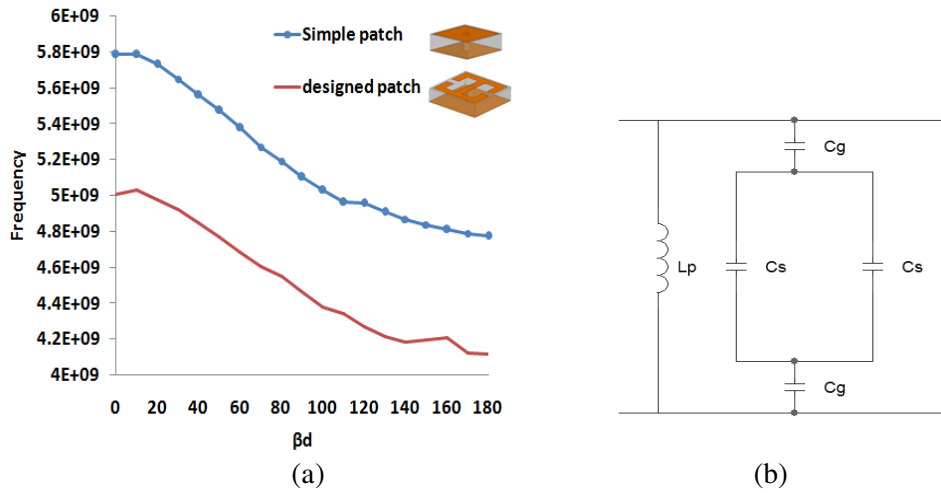
$$\begin{cases} m_e = 0.8675, K_e = 2.043 \left(\frac{W}{h}\right)^{0.12} \\ m_e = \frac{1.565}{(W/h)^{0.16}} - 1, K_e = 1.97 - \frac{0.03}{W/h} \end{cases} \quad \text{for } 0.1 \leq s/W \leq 0.3 \quad (11)$$

Figure 2(a) shows the comparison of the dispersion diagram between the simple patch and designed structure by using the full wave simulation. In a simple patch structure, the zero order resonance (ZOR) occurs at 5.8 GHz. With numerical calculations the inductance is  $2 \mu\text{H}$ , and capacitance is  $0.34 \text{ pF}$ , so the resonance is achieved at 5.98 GHz. In modified structure, the ZOR frequency is decreased to 5 GHz. In the second model, the inductance is  $2 \mu\text{H}$ , and series capacitance is increased by gap structure to  $0.5 \text{ pF}$ , so the calculated resonance is at 5.02 GHz.

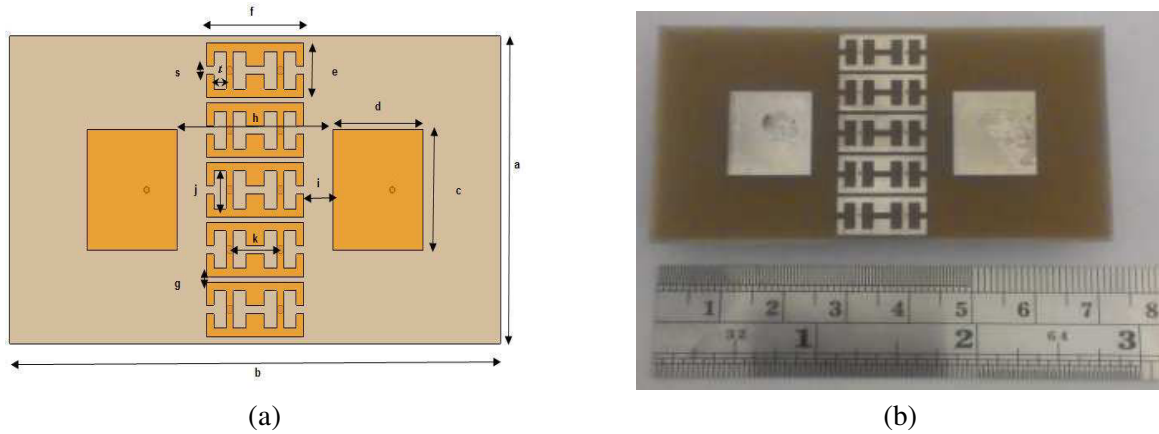
Figure 2(b) shows the final prototype EBG equivalent circuit. Some equivalent circuit parameters have been neglected here.  $L_p$  and  $C_g$  are calculated by Equations (4) and (3), respectively. With this calculation the value of  $C_g$  is  $0.17 \text{ Pf}$ . For calculation of  $C_s$  Equations (5) to (11) have been used, and  $C_s$  is obtained, about  $0.46 \text{ Pf}$ . So total capacitance is about  $0.57 \text{ Pf}$ .

### 3. SIMULATION AND EXPERIMENTAL RESULT

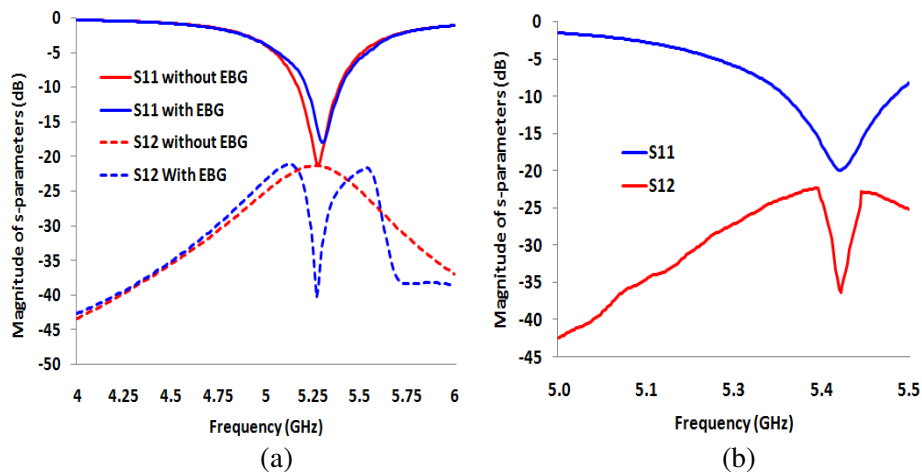
In this paper, the simulation of prototype antenna with HFSS 11 is presented. Two microstrip patch antennas are designed for resonance at 5.28 GHz. The size of each antenna is  $14.4 \times 12.6 \text{ mm}$ , and the



**Figure 2.** Unit cells modeling. (a) Dispersion diagram of conventional EBG and new designed unit cell. (b) Equivalent circuit model for new designed EBG unit cell.



**Figure 3.** Patches array antenna with EBG structure. (a) Simulation and dimensions. (b) Fabricated antenna.



**Figure 4.** S parameters. (a) Simulation in presence and absence of EBG. (b) Experimental result with EBG.

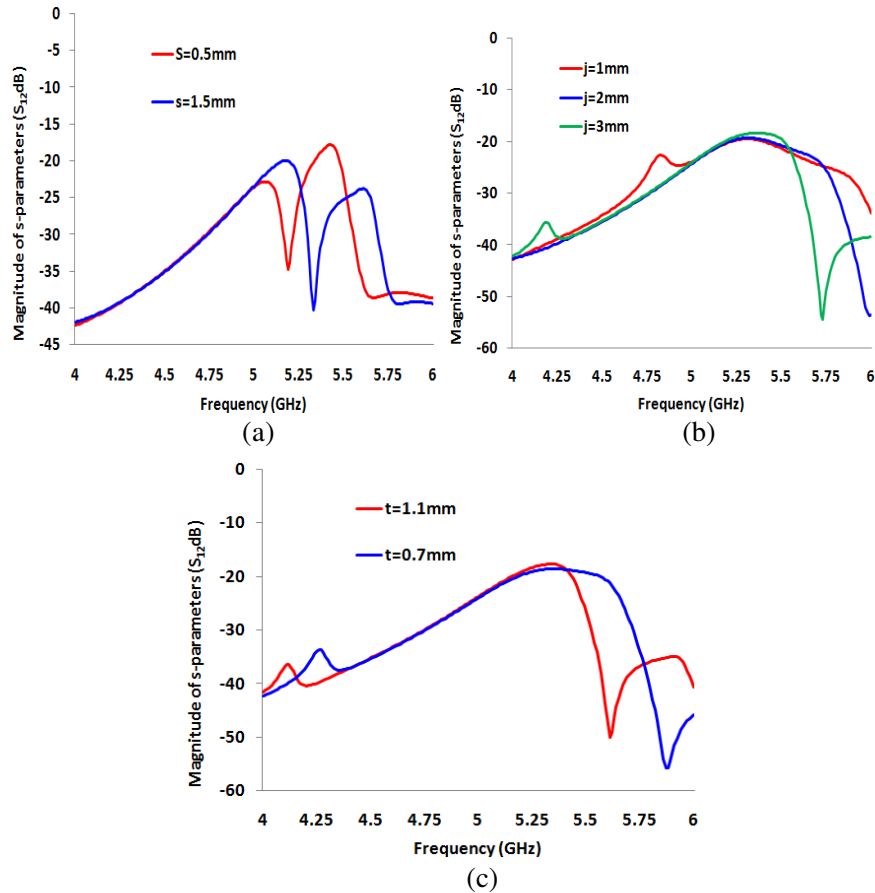
distance between them is 34 mm. The designed antenna is fabricated on a low cost FR-4 substrate where the permittivity is 4.4, and dielectric loss tangent is 0.02. It is fed by 50 Ω coaxial probe, and the bandwidth of antenna is 3%. Fig. 3 shows patches array antenna with a EBG structures. The antennas are in *E*-plane coupling state. The cell size of periodic structure is 6.4 mm × 6.4 mm, and Vias radius is 0.5 mm. The total size of antenna is 36 mm × 68 mm × 1.6 mm. All dimensions are presented in Table 1 with details.

First resonance frequency of modified EBG cell is about 5 GHz, which is coincided with resonance of the patch. Fig. 4(a) shows the simulation results of *S* parameters of array antenna with and without EBG structure. Mutual coupling level is about -22 dB for a simple array and -43 dB for the array with EBG structure. Obviously, *S*<sub>21</sub> is reduced more than 20 dB, by using the EBG structure. Fig. 4(b) shows experimental results for prototype arrangement with HP8722ES network analyzer. The prototype antenna has been modified for 5.35 GHz. In experimental result, *S*<sub>21</sub> is reduced to -36.3 dB. The effect of *s*, *j* and *t* on *S*<sub>12</sub> in parametric form is studied as shown in Fig. 5.

Figure 5(a) shows the effect of change in *s* to 0.5 mm and 1.5 mm. For lower *s*, *S*<sub>12</sub> is reduced, and when it is increased, the frequency is shifted to higher frequency, but these changes are not effective, and less than 100 MHz shift is visible.

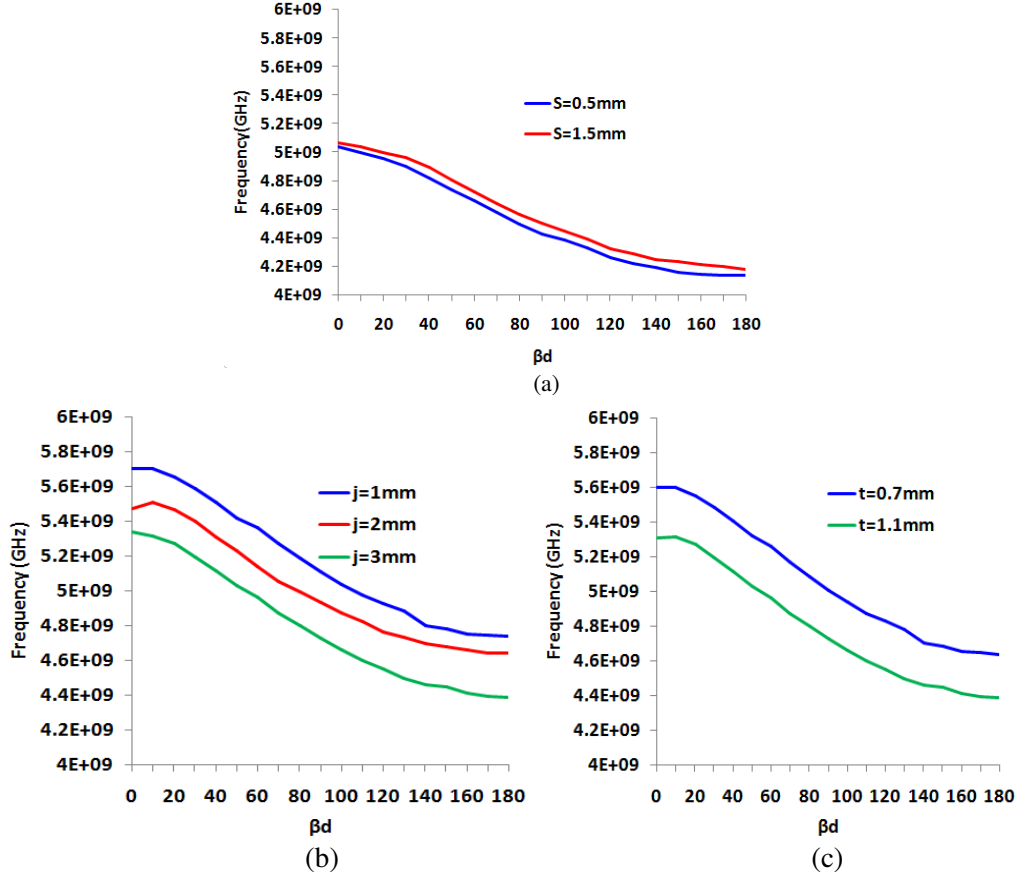
Figure 5(b) shows the effect of change in *j* for 1 mm, 2 mm and 3 mm. By increasing this gap the frequency is reduced. Fig. 5(c) shows the effect of change in *t* for 0.7 mm and 1.1 mm. By increasing this gap, the frequency is reduced. So *t* and *j* are most important parameters which will affect EBG characteristic.

The dispersion diagram of EBG unit cell shows that the frequency changes have similar behavior to that in *S*<sub>12</sub> of the antenna, but a little shift is visible in Fig. 2 and Fig. 6 dispersion diagrams in



**Figure 5.** *S*<sub>12</sub> parameters. (a) The effect of change in *s*. (b) The effect of change in *j*. (c) *S* parameters simulation for the effect of change in *t*.

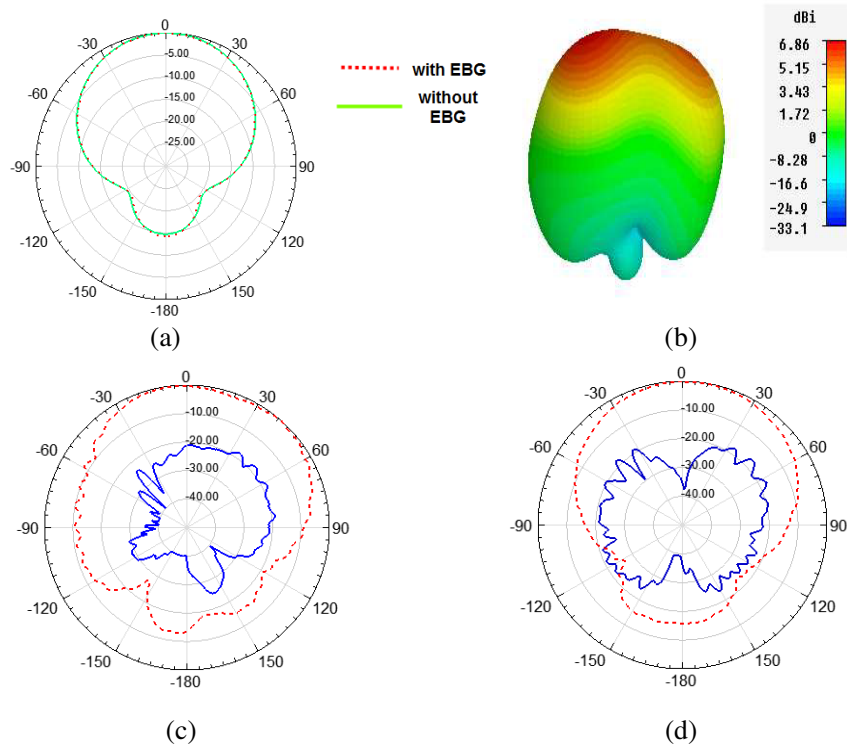
comparison to antenna  $S_{12}$ . This shift is happened because metal loss is master slave simulation and fringed capacitance at edge of gaps, which is effective in this simulation method. Fig. 6 shows the dispersion diagram for each change in EBG gaps.



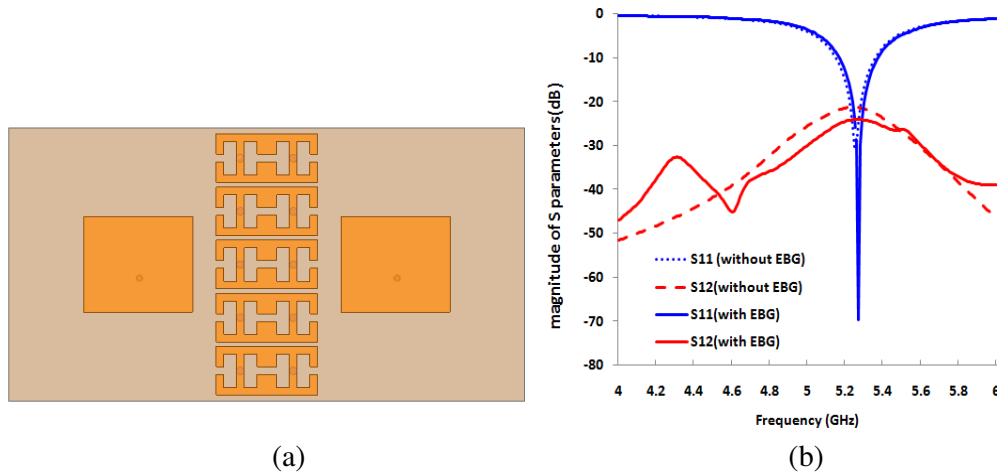
**Figure 6.** Dispersion diagram. (a) Change in  $s$ . (b) Change in  $j$ . (c) Change in  $t$ .

**Table 1.** Geometry dimensions of antenna and EBG.

parameter	mm
$a$	36
$b$	78
$c$	14.4
$d$	12.6
$e$	6.4
$f$	13.4
$g$	0.6
$h$	21.4
$i$	4
$j$	4.4
$k$	7
$s$	1
$t$	1.7



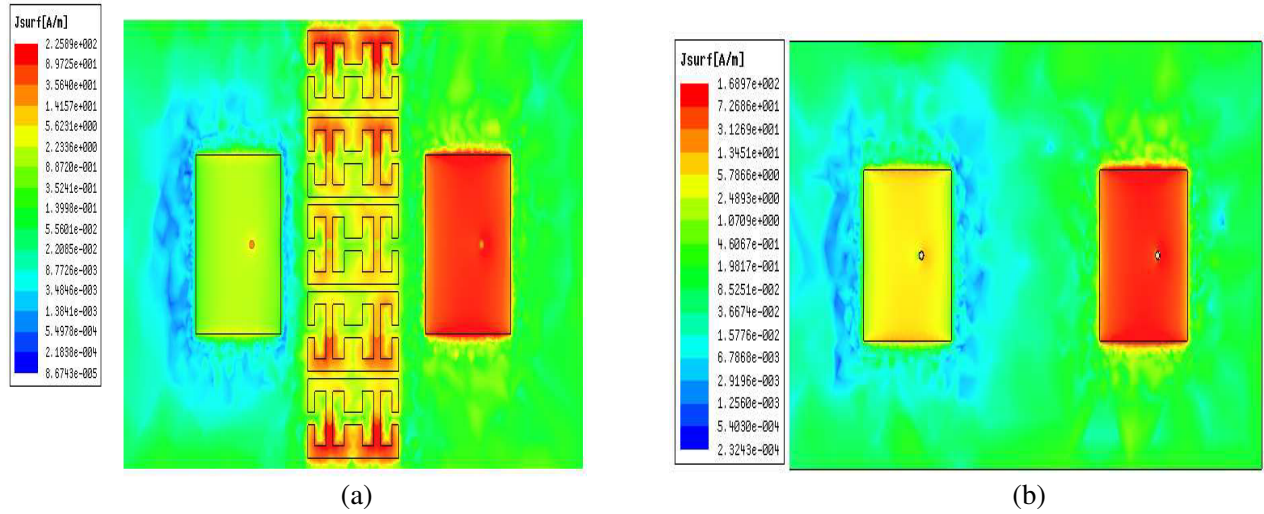
**Figure 7.** The pattern of antenna with and without EBG (a) simulation of the *E*-plane in presence and absence of EBG. (b) Gain and 3D pattern of antenna in 5.3 GHz. (c) The experimental result for *E*-plane. (d) The experimental result for *H*-plane (co-polarization is shown with dashes).



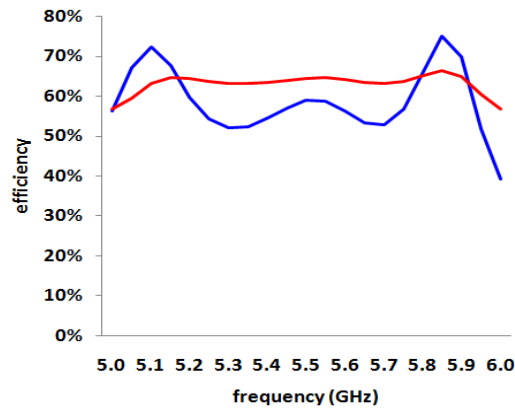
**Figure 8.** (a) The antenna structure in *H*-plane coupling. (b) *s* parameters of antenna with and without EBG.

The *E*-plane patterns of the antenna with absence and presence of EBG are demonstrated in Fig. 7(a) at 5.3 GHz. Here the comparison between prototype structure for conventional arrangement and that by applying EBG structure is presented, and as shown in Fig. 7(a) the EBG structure does not affect antenna pattern. Fig. 7(b) shows 3D pattern of the antenna at 5.3 GHz, antenna gain and simulation result around 6.86 dBi. Fig. 7(c) and Fig. 8(d) show the final structure's (*E*-plane and *H*-plane) experimental result for Co-polarization and cross-polarization for 5.3 GHz, respectively.

Figure 8 shows the comparison of mutual coupling for *H*-plane in presence and absence of EBG cell.



**Figure 9.** Surface current distribution with and without EBG structure. (a) Patch array with EBG. (b) Patch array without EBG.



**Figure 10.** Antenna efficiency in presence and absence of EBG Cells.

**Table 2.** Comparison between presented design and previous researches.

	Frequency range	Mutual coupling	Size
<b>Our design</b>	5.4 GHz	20 dB	$68 \times 36 \times 1.6$
<b>Ref. [10]</b>	5.9 GHz	18.28 dB	$80 \times 60 \times 1.35$
<b>Ref. [11]</b>	5 GHz	19 dB	Not given
<b>Ref. [12]</b>	5.85 GHz	25.3 dB	$100 \times 50 \times 2$
<b>Ref. [13]</b>	5.75 GHz	14 dB	$78 \times 78 \times 2.54$

It is obvious that in  $H$ -plane coupling, EBG structure has no effect on reducing mutual coupling for this structure. Fig. 9 shows surface current distribution with and without EBG structure. Obviously, our EBG absorber has limited the current distribution on the antenna surface and mutual coupling of antenna at the resonant frequency. The EBG has restricted the surface field in array structure. The antenna current is reduced from 8.5 A/m to around 3.9 A/m in the presence of EBG, so the coupling current is reduced more than 50%.

Figure 10 shows the antenna efficiencies in presence and absence of EBG cells. Without EBG



cells the antenna efficiency is around 65% at 5.3 to 5.4 GHz, and when EBG cells are placed between antennas, antenna efficiency is reduced to 53% at 5.3–5.4 GHz.

Previously, different models of EBG have been used to decrease the mutual coupling between patch antennas in WLAN frequency at around 5 GHz. Table 2 represents the comparison between current structure and some previous designs. The prototype structure's size has been reduced about 20–40% in comparison to similar previous researches.

#### 4. CONCLUSIONS

In this paper, a novel effective EBG structure is suggested to reduce mutual coupling between patch antenna arrays. The patch antennas operate at 5.35 GHz which is attractive frequency for wireless applications. We have used  $2 \times 5$  EBG structures to reduce mutual coupling more than 20 dB. The EBG cells capacitance and inductance have been calculated by numerical methods.  $S_{12}$  parameters are compared with dispersion diagram results. In addition, the simulation results are compared with experimental ones. Return loss and surface current in presence and absence of EBG cells have been compared by full wave simulations. The coupling current is reduced more than 50%, and the prototype structure size has been reduced around 20–40% in comparison to previous researches.

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