

# Ultra-Wideband Four-Way In-Phase Multilayer Power Divider with High Isolation

Long Xiao\*, Hao Peng, and Tao Yang

**Abstract**—A novel ultra-wideband four-way in-phase multilayer power divider based on the microstrip-to-slotline transition is proposed in this paper as a complementary slotline power divider with high isolation. Due to the introduction of three lumped isolation resistors, the isolations between output ports in the new structure have been improved. The design expressions have been derived by making use of odd-mode and even-mode method. Both simulated and measured results have proved that the proposed power divider has good impedance matching at all ports, high isolations between output ports, excellent amplitude and phase balance, as well as flat group delay over the wide frequency range from 3.8 GHz to 11 GHz.

## 1. INTRODUCTION

Since the ultra-wideband (UWB) spectrum was determined in 2002, a large number of devices and components have been designed [1–11]. UWB power divider, which is an indispensable passive component, plays an important role in the microwave and RF systems. To obtain an 180° out-of-phase signal division in a wide frequency range, an UWB power divider based on a T-junction consisting of a microstrip line and slotline was proposed in [4]. In [1], a compact non-conplanar power divider based on microstrip-to slotline transition was designed, which introduced two circular stubs as implemental circuit that connect to the ends of output arms to decrease the ripple in the passband. In [6], a tapered transition and a fan-shaped slot were exploited to take the place of a circular slot so that the performances of the improved power divider were better than one designed in [1, 4].

The power dividers proposed in [1–7] have low insertion losses and good return losses. However, the isolations between output ports were not satisfying. Thus, some new power dividers with high isolations based on slotline were proposed [8–11]. In [10], a slot has been processed on the ground plane which separated the ground into two parts, and a resistor bridging over the slot has been introduced to improve the isolations between output ports. Different from the power divider in [10], a via hole located on the substrate has been drilled to contain an isolation resistor that connected to the output branches in [8]. In order to expand the application of UWB power divider, a four-way out-of-phase slotline power divider was proposed in [9].

In this paper, a novel UWB four-way in-phase multilayer power divider based on microstrip-to-slotline transition is proposed, which introduces three resistors to increase the isolations between output ports. Both the simulated and measured results have proved that the new four-way power divider with high isolation has good impedance matching, excellent amplitude and phase balance as well as high isolations between output ports.

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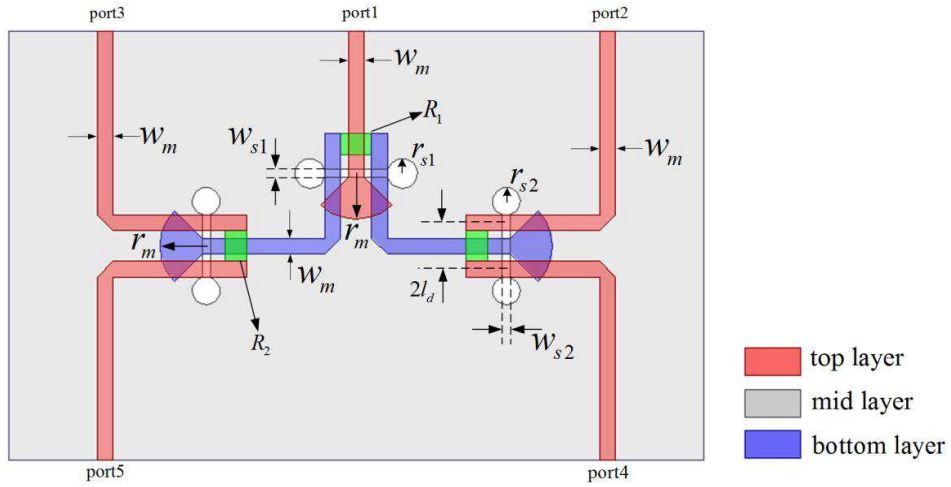
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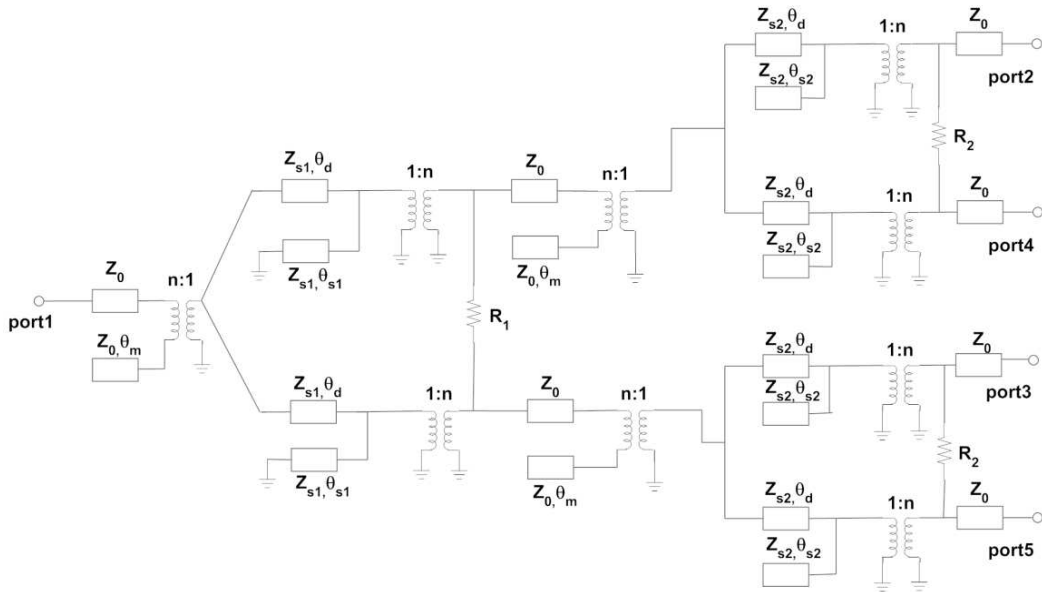
## 2. CIRCUIT DESIGN

The configuration of the proposed four-way power divider with high isolation presented in this paper is shown in Figure 1, which consists of three layers (top layer, middle layer and bottom layer). All the output ports (port 2–port 5) as well as input port (port 1) are located in the top layer. The slot is etched in the middle layer, namely ground plane. And two branches of the first-order power divider are located in the bottom layer.

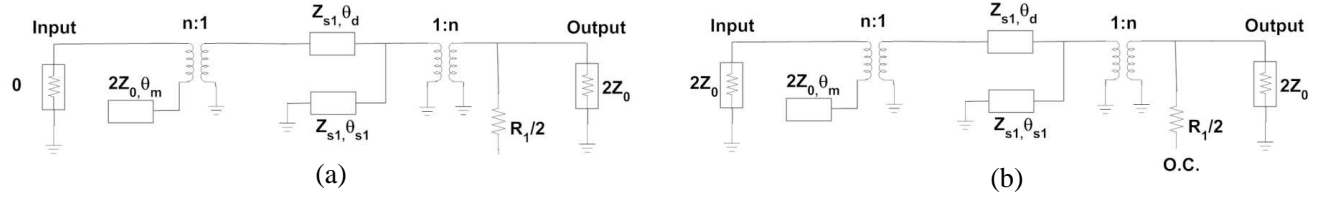
This new power divider employs microstrip-to-slotline transition to realize the goal of distributing power equally. Three resistors are employed to improve the isolations between output ports. Moreover, three radial stubs are placed at the ends of microstrip lines, and six circular stubs are placed at the ends of slotlines. No matter the radial stubs or the circular stubs, all of them act as compensating circuits. Their equivalent lengths are a quarter of  $\lambda_m$  and  $\lambda_{s1}$  (or  $\lambda_{s2}$ ).  $\lambda_m$  and  $\lambda_{s1}$  (or  $\lambda_{s2}$ ) stand for the guided



**Figure 1.** Configuration of the proposed UWB four-way in-phase multiplayer power divider with high isolation.



**Figure 2.** Equivalent circuit of the proposed UWB four-way in-phase multiplayer power divider with high isolation.



**Figure 3.** The first order power dividing. (a) Odd-mode circuit model. (b) Even-mode circuit model.

wavelength of microstrip line and guided wavelength of slotline at the center frequency, respectively.

Because of the symmetrical structure, the power divider proposed in this paper can employ odd-mode and even-mode analysis method. Its equivalent circuit is shown in Figure 2, where  $\theta_m$ ,  $\theta_{s1}$ ,  $\theta_{s2}$  and  $\theta_d$  represent the equivalent electrical length  $\lambda_m/4$ ,  $\lambda_{s1}/4$ ,  $\lambda_{s2}/4$  and  $l_d$ , respectively. Figure 3 shows the equivalent circuits of the first-order power divider (including port 1). Figure 3(a) exhibits the odd-mode equivalent circuit. In order to obtain good impedance matching and excellent isolations between output ports locating on both sides of the input port (port 1) like port 2 and port 3, the following expression must be satisfied.

$$\frac{1}{R_1} = \frac{n^4 Z_{s1}^2 \tan \theta_{s1} \tan \theta_d - j2n^2 Z_{s1} Z_0 \tan \theta_d - j2n^2 Z_{s1} Z_0 \tan \theta_{s1}}{4n^2 Z_{s1} Z_0 \tan \theta_{s1} (n^2 Z_{s1} \tan \theta_d - 2Z_0 \cot \theta_m)} + \frac{-j4Z_0^2 \tan \theta_{s1} \tan \theta_d \cot \theta_m - 2n^2 Z_{s1} Z_0 \tan \theta_{s1} \cot \theta_m + j4Z_0^2 \cot \theta_m}{4n^2 Z_{s1} Z_0 \tan \theta_{s1} (n^2 Z_{s1} \tan \theta_d - 2Z_0 \cot \theta_m)} \quad (1)$$

Because  $\theta_m = 90^\circ$ ,  $\theta_{s1} = 90^\circ$ , and the value of  $\theta_d$  is small, namely  $\cot \theta_m = 0$  and  $\tan \theta_{s1} \gg \tan \theta_d$ , equivalent (1) can be simplified as:

$$\frac{1}{R_1} \approx \frac{n^2 Z_{s1} \tan \theta_d - j2Z_0}{4n^2 Z_{s1} Z_0 \tan \theta_d}$$

Considering that resistor is a real number, the value of  $R_1$  is selected as:

$$R_1 \approx 4Z_0 \quad (2)$$

Here, the transformer turn ratio  $n$  stands for the coupling coefficient between slotline and microstrip line, which can be derived according to [12] as following:

$$n = \frac{J_0(k_{es} W_m/2) J_0(k_{em} W_s/2)}{k_{es}^2 + k_{em}^2} \cdot \left( \frac{k_{es}^2 k_1}{k_1 \cos k_1 h + k_2 \sin k_1 h} + \frac{k_{em}^2 k_2 \epsilon_r}{k_2 \epsilon_r \cos k_1 h - k_1 \sin k_1 h} \right) \quad (3)$$

where  $J_0(\cdot)$  is the zeroth-order Bessel function and

$$\begin{aligned} k_1 &= \sqrt{|k_0^2 \epsilon_r - k_{es}^2 - k_{em}^2|} = k_0 \sqrt{|\epsilon_r - \epsilon_{res} - \epsilon_{rem}|}; \\ k_2 &= k_0 \sqrt{|\epsilon_{res} + \epsilon_{rem} - 1|}; \\ k_{es} &= k_0 \sqrt{\epsilon_{res}}; \quad k_{em} = k_0 \sqrt{\epsilon_{rem}}; \end{aligned}$$

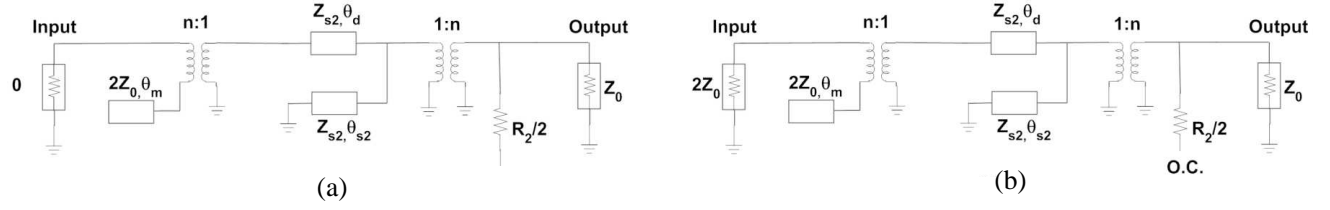
$\epsilon_{rem}$  and  $\epsilon_{res}$ , which are confined according to [12], represent the effective dielectric constants of microstrip line and slotline, respectively.

Figure 3(b) exhibits the even-mode equivalent circuit of the first-order power divider. In order to obtain good even-mode impedance matching, the characteristic impedance of slotline  $Z_{s1}$  must satisfy the following expression.

$$2Z_0 = \frac{n^2 Z_{s1} (jn^2 Z_{s1} \tan \theta_{s1} \tan \theta_d + 2Z_0 \tan \theta_{s1} + 2Z_0 \tan \theta_d)}{j2Z_0 \tan \theta_{s1} \tan \theta_d + n^2 Z_{s1} \tan \theta_{s1} - j2Z_0} \quad (4)$$

Since  $\theta_{s1}$  approximates  $90^\circ$ , and  $\theta_d$  is a small value, namely  $\tan \theta_{s1} \gg \tan \theta_d$ , the above equivalent can be simplified as:

$$2Z_0 \approx \frac{n^2 Z_{s1} (jn^2 Z_{s1} \tan \theta_d + 2Z_0)}{j2Z_0 \tan \theta_d + n^2 Z_{s1}}$$



**Figure 4.** The second order power dividing. (a) Odd-mode circuit model. (b) Even-mode circuit model.

Namely,

$$Z_{s1} \approx \frac{2Z_0}{n^2} \quad (5)$$

The odd-mode equivalent circuit of the second-order power divider is exhibited in Figure 4(a). Similar to the analysis of the first-order power divider, the resistor  $R_2$  must be confined by the following equation.

$$\begin{aligned} \frac{1}{R_2} = & \frac{n^4 Z_{s2}^2 \tan \theta_{s2} \tan \theta_d - j n^2 Z_{s2} Z_0 \tan \theta_d - j n^2 Z_{s2} Z_0 \tan \theta_{s2}}{2 n^2 Z_{s2} Z_0 \tan \theta_{s2} (n^2 Z_{s2} \tan \theta_d - 2 Z_0 \cot \theta_m)} \\ & + \frac{-j 2 Z_0^2 \tan \theta_{s2} \tan \theta_d \cot \theta_m - 2 n^2 Z_{s2} Z_0 \tan \theta_{s2} \cot \theta_m + j 2 Z_0^2 \cot \theta_m}{2 n^2 Z_{s2} Z_0 \tan \theta_{s2} (n^2 Z_{s2} \tan \theta_d - 2 Z_0 \cot \theta_m)} \end{aligned} \quad (6)$$

Because  $\theta_m = 90^\circ$ ,  $\theta_{s2} = 90^\circ$ , and the value of  $\theta_d$  is small, namely  $\cot \theta_m = 0$  and  $\tan \theta_{s2} \gg \tan \theta_d$ , equivalent (6) can be simplified as:

$$\frac{1}{R_2} \approx \frac{n^2 Z_{s2} \tan \theta_d - j Z_0}{2 n^2 Z_{s2} Z_0 \tan \theta_d}$$

Considering that resistor is a real number, the value of  $R_2$  is selected as:

$$R_2 \approx 2Z_0 \quad (7)$$

Through the analysis of Figure 4(b), expression (8) about  $Z_{s2}$  can be derived.

$$Z_0 \approx \frac{n^2 Z_{s2} (j n^2 Z_{s2} \tan \theta_d + Z_0) \tan \theta_{s2}}{n^2 Z_{s2} \tan \theta_d + j 2 Z_0 \tan \theta_d \tan \theta_{s2} + n^2 Z_{s2} \tan \theta_{s2} - j 2 Z_0} \quad (8)$$

Since  $\theta_{s2} = 90^\circ$  and  $\theta_d$  is a small value, namely  $\tan \theta_{s2} \gg \tan \theta_d$ , the above equivalent can be simplified as:

$$Z_0 \approx \frac{n^2 Z_{s2} (j n^2 Z_{s2} \tan \theta_d + Z_0)}{j 2 Z_0 \tan \theta_d + n^2 Z_{s2}}$$

Then,

$$Z_{s2} \approx \frac{\sqrt{2} Z_0}{n^2} \quad (9)$$

Equations (2) and (7) provide a simple guideline to determine the values of isolation resistors  $R_1$  and  $R_2$  so that high isolations between output ports can be obtained. In addition, the dimensions of the four-way in-phase multilayer power divider can also be confined by the above expressions.

### 3. EXPERIMENTAL RESULTS

The presented UWB four-way in-phase multilayer power divider with high isolation is designed and fabricated on a Rogers 4003C substrate with dielectric constant of 3.38, thickness of 0.508 mm, and loss tangent of 0.0023. The characteristic impedance of microstrip line is  $50 \Omega$ . Through optimization by EM simulator HFSS, the final dimensions of the presented four-way power divider with high isolation are listed as following:  $w_m = 1.14$  mm,  $r_m = 3.6$  mm,  $r_{s1} = 1.08$  mm,  $w_{s1} = 0.6$  mm,  $l_d = 1.68$  mm,

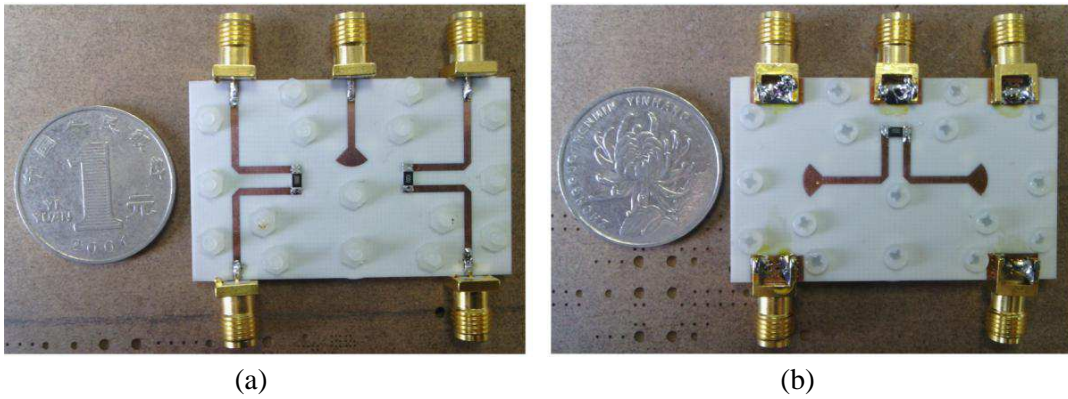


Figure 5. Photograph of the four-way in-phase power divider. (a) Top view. (b) Bottom view.

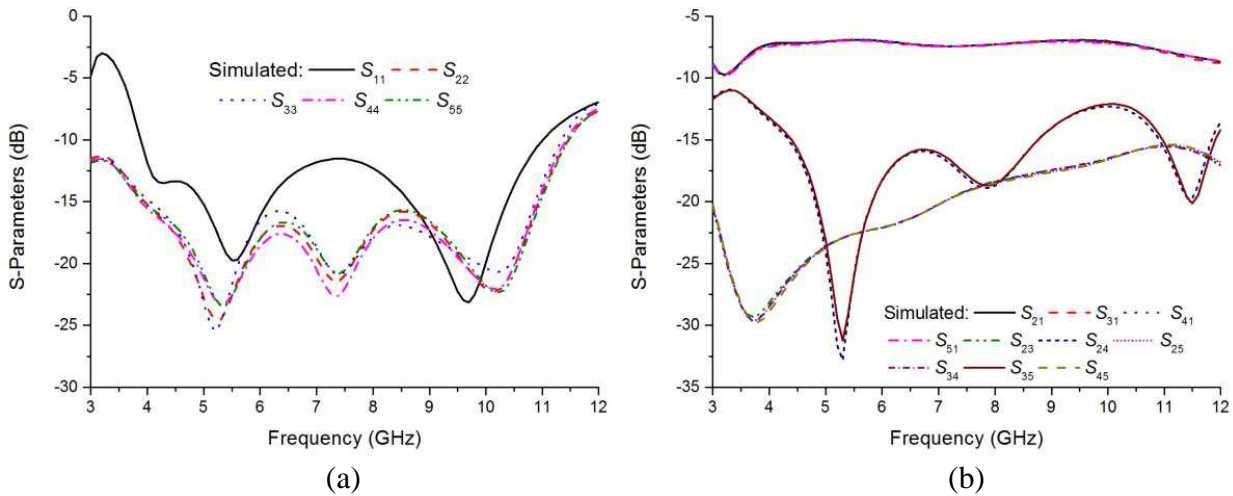
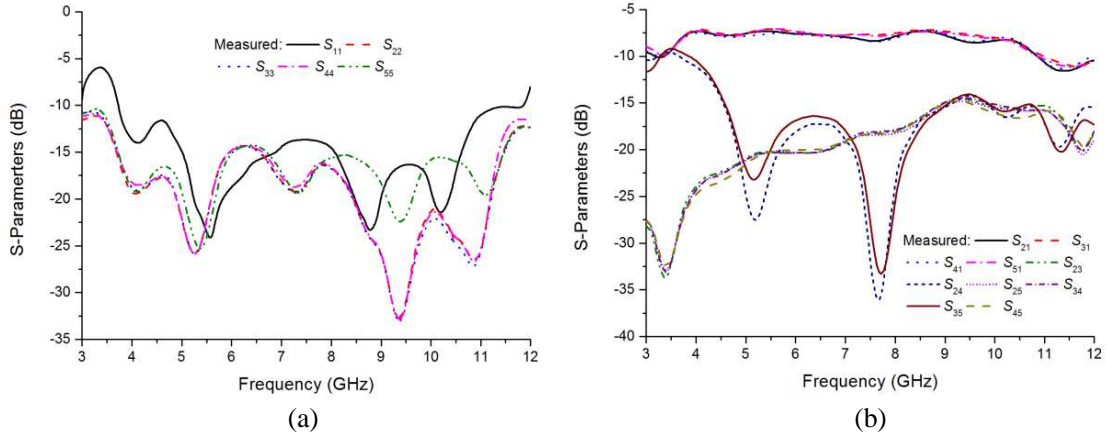


Figure 6. Simulated results. (a) Return loss. (b) Insertion loss.

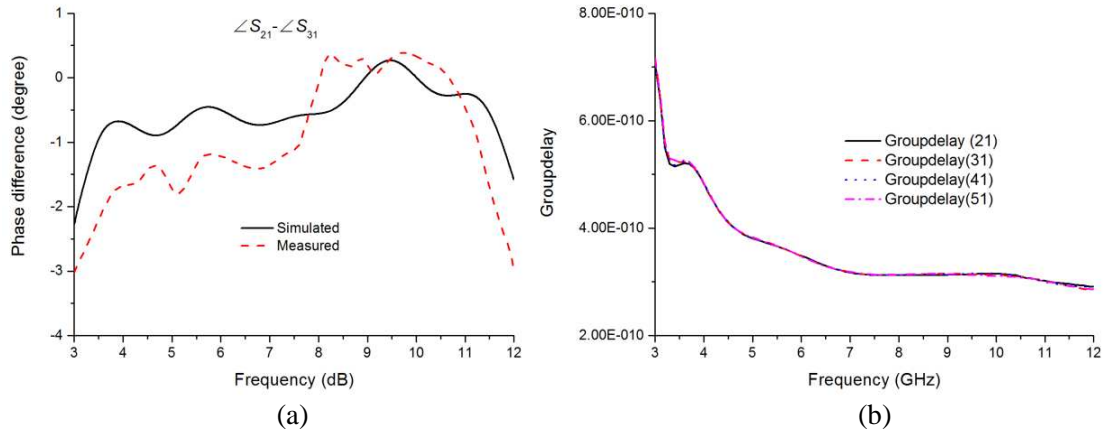
$R_1 = 200 \Omega$ ,  $R_2 = 100 \Omega$ ,  $r_{s2} = 1.0 \text{ mm}$ ,  $w_{s2} = 0.6 \text{ mm}$ . Figure 5 shows a photograph of the fabricated four-way in-phase multiplayer power divider with high isolation. The whole size of the power divider is  $30 \text{ mm} \times 50 \text{ mm}$ .

The simulated and measured results of the proposed four-way power divider with high isolation are exhibited in Figure 6, Figure 7 and Figure 8. It is obvious that the measured results show a good agreement with the simulated ones in the wide working frequency range. The simulated and measured 10 dB return loss bandwidths of input port, namely  $S_{11}$ , are about 7.2 GHz (from 3.8 GHz to 11 GHz) and 7.5 GHz (from 3.7 GHz to 11.2 GHz), respectively. The measured return losses of outputs ports  $S_{22}$ ,  $S_{33}$ ,  $S_{44}$  and  $S_{55}$  are better than 12 dB in the frequency range from 4 GHz to 11 GHz, while the simulated ones are better than 15 dB in the same frequency band, which are shown in Figure 6(a) and Figure 7(a).

Figure 6(b) and Figure 7(b) exhibit the simulated and measured insertion losses of all the input and output ports and the isolations between output ports. The simulated insertion losses  $S_{21}$ ,  $S_{31}$ ,  $S_{41}$  and  $S_{51}$  are within  $7.2 \pm 0.3 \text{ dB}$  in a wide frequency range from 4 GHz to 10 GHz, while the measured insertion losses are within  $7.5 \pm 0.5 \text{ dB}$ . The measured isolations  $S_{24}$  and  $S_{35}$  are better than 10 dB in the range from 4 GHz to 12 GHz, while the simulated ones are better than 12 dB. In addition, the other simulated and measured isolations  $S_{23}$ ,  $S_{25}$ ,  $S_{34}$  and  $S_{45}$  are better than 15 dB and 14 dB over frequency range 3 GHz–12 GHz, respectively.



**Figure 7.** Measured results. (a) Return loss. (b) Insertion loss.



**Figure 8.** (a) Simulated and measured phase difference. (b) Measured group delay.

Figure 8(a) exhibits the phase difference between output port 2 and port 3, which represents the phase balance of the power divider. The measured result is within  $0^\circ \pm 1^\circ$  from 4 GHz to 11 GHz, which shows good agreement with simulated one. Moreover, it is easy to find that the group delay is very flat as shown in Figure 8(b).

#### 4. CONCLUSION

A new ultra-wideband four-way in-phase multiplayer power divider with high isolation has been proposed. Three isolation resistors have been introduced to increase the isolations between output ports. Equivalent circuits have also been constructed to determine the dimensions of the power divider. The simulated and measured results exhibit a good agreement. The results also indicate that the presented four-way power divider shows good input and output impedance matching, high isolations between output ports, as well as excellent amplitude and phase balance at output ports in a wide frequency range.

#### ACKNOWLEDGMENT

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