### A MINIATURIZED TRIPLE-BAND BRANCH-LINE COU-PLER BASED ON SIMPLIFIED DUAL-COMPOSITE RIGHT/LEFT-HANDED TRANSMISSION LINE

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Abstract—A miniaturized triple-band branch-line coupler based on the simplified dual-composite right/left-handed transmission line (S-D-CRLH-TL) is proposed in this paper. The electromagnetic characteristics of S-D-CRLH-TL are analyzed by the simulator and equivalent circuit model, and the results prove that there are three frequency points with phase of -90-degree in the passbands; this characteristic can be used to design triple-band quadrature microwave The proposed branch-line coupler is fabricated and components. measured, the measured and simulated results are in good agreement with each other, showing that the triple-band operating at 3.06 GHz, 4.00 GHz and 5.54 GHz, the useful bandwidths are 2.97 GHz–3.16 GHz, 3.82 GHz-4.12 GHz and 5.48 GHz-5.67 GHz. In addition, compared with the conventional branch-line coupler, the whole size of the proposed one is  $17 \text{ mm} \times 14.4 \text{ mm} (0.173\lambda \times 0.147\lambda)$  ( $\lambda$  is the wavelength in low frequency), it realizes a 73% size reduction. Moreover, compared with the triple-band branch-line coupler based on the double-Lorentz transmission line metamaterial, the proposed branch-line coupler is more effective in the situation, which is sensitive to phase-changing, as the sign of phase difference in the two outputs at the three frequency points keeps the same.

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### 1. INTRODUCTION

Recently, with the fast development of microwave wireless communication technology, the miniaturization and multiple bands of microwave components are becoming more and more important [1-25]. As an important microwave component, there are many methods applied to realize the miniaturization and multiple bands of branch-line coupler. In paper [2, 3], dual-band branch-line couplers are realized by adding the cross couple-lines to the parallel-lines and third branch-line in the coupler, but the size of these branch-line coupler is very large. In paper [4], the author applies the composite right/left-handed transmission lines (CRLH-TLs) based on complementary split ring resonator (CSRR) to design dual-band branch-line coupler, the dual-band and small size are realized. In paper [5], the structure of CRLH-TLs based on new technology of MIM (metal-insulator-metal) is used to design BLC, the small size is also realized, but the coupler based on CRLH-TLs cannot be used in the situation which is sensitive to phase-changing. In paper [6], a triple-band branch-line coupler is realized by using T-type and additional port impedance transformers, but it does not realize miniaturization. Paper [7] proposes a triple-band branch-line coupler by substituting the  $\lambda/4$  transmission lines in the conventional branchline coupler, however its complex structure is the biggest problem, in paper [16], the double-Lorentz transmission line metamaterial also can be used to design triple-band branch-line coupler, but the sign of phase difference in the two outputs at the triple-band do not keeps the same. and the designed branch-line coupler can not be used in the situation, which is sensitive to phase-changing.

In this paper, a novel simplified dual-composite right/left-handed transmission line (S-D-CRLH-TL) is proposed firstly. Then its electromagnetic characteristics are analysed by the simulator, and the equivalent circuit model is also provided. The results of the simulator and the equivalent circuit model are in good agreement, which prove that the equivalent circuit model is right. In the simulated results, there are three frequency points with phase of -90degree in the passbands, and this characteristic has been applied in designing the triple-band branch-line coupler in this paper. Then, the proposed triple-band branch-line coupler is fabricated and measured. the measured and simulated results are in good agreement with each other, showing that the triple-band centre at 3.06 GHz, 4.00 GHz and 5.54 GHz, the useful bandwidths are 2.97 GHz-3.16 GHz, 3.82 GHz-4.12 GHz and 5.48 GHz–5.67 GHz. As the sign of phase difference in the two outputs at the triple-band keeps the same, the proposed branchline coupler is more effective in the situation, which is sensitive to phase-changing. In addition, the whole size of the proposed branchline coupler is  $17 \text{ mm} \times 14.4 \text{ mm} (0.173\lambda \times 0.147\lambda)$  ( $\lambda$  is the wavelength in low frequency), it realizes a 73% size reduction in comparison with the conventional one.

#### 2. ANALYSIS OF THE S-D-CRLH-TL

Figure 1 is the geometry structure and equivalent circuit model of the S-D-CRLH-TL proposed in this paper, The unit structure is designed on a substrate with relative dielectric constant 2.65 and thickness 0.8 mm. In the circuit model, where the  $L_1$  is models the main transmission line inductance, the  $L_R$  is realized by the narrow microstrip lines paralleled with the structure of spiral inter-digital, the  $L_L$  models the left-handed inductance realized by the stub line, the  $C_L$ represents the coupling of the structures of spiral inter-digital and the  $C_1$  and  $L_2$  are realized by the self-coupling of the structures of spiral inter-digital.



**Figure 1.** Geometry structure and equivalent circuit model of S-D-CRLH-TL. (a) Geometry structure. (b) Equivalent circuit model.

Compared with the conventional D-CRLH-TL, the proposed S-D-CRLH-TL does not have the right-handed capacitance  $(C_R)$ , so the stopband between the first right-handed passband and the left-handed passband of the conventional D-CRLH-TL is destroyed, a passband between the two transmission zeros is engendered, and because of this, the dispersion diagram will change as shown in Figure 2.

In Figure 2, we can see that a new passband is engendered, and the electromagnetic characteristics of the S-D-CRLH-TL in other frequency keep the same with the D-CRLH-TL.

In order to obtain good performances such as low insertion losses in the bandwidth of interest and sharpened rejection out of band, the physical dimensions of the S-D-CRLH-TL are optimized and the detailed dimensions are:  $l_1 = 10 \text{ mm}$ ,  $l_2 = 7 \text{ mm}$ ,  $l_3 = 3 \text{ mm}$ ,  $w_1 = 2.2 \text{ mm}$ ,  $w_2 = 1.8 \text{ mm}$ ,  $w_3 = 1.2 \text{ mm}$ ,  $w_4 = 0.2 \text{ mm}$ ,  $w_5 = 0.2 \text{ mm}$ . The simulated results are shown in Figure 3. We can see that there are three frequency points with phase of -90-degree, and all these three frequency points are in the passband.

Figure 1(b) is the equivalent circuit model of the proposed S-D-CRLH-TL. When  $L_1 = 0.19 \text{ nH}$ ,  $L_2 = 0.45 \text{ nH}$ ,  $L_R = 12.22 \text{ nH}$ ,  $C_1 = 2.32 \text{ pF}$ ,  $C_L = 5.28 \text{ pF}$ , the results of the equivalent circuit model are shown in Figure 4.

From Figures 3 and 4, we can see that the results of the simulator and the equivalent circuit model are in good agreement with each other, proving that the circuit model is right.



Figure 2. The dispersion diagrams of D-CRLH and S-D-CRLH-TL.



**Figure 4.** *S*-parameters and phase of S-D-CRLH-TL by equivalent circuit model.



**Figure 3.** *S*-parameters and phase of S-D-CRLH-TL by simulator.



Figure 5. The conventional structure of branch-line coupler.

## 3. DESIGN OF THE TRIPLE-BAND BRANCH-LINE COUPLER

## 3.1. Unit Cells of S-D-CRLH-TL with Different Physical Dimensions

Figure 5 is the structure of conventional branch-line coupler, which is consisted of two parallel-lines and two branch-lines. According to the designing method proposed in paper [8], the electrical length of branch-line and parallel-line is 90-degree,  $Z_1 = 50 \Omega$ ,  $Z_2 = 35 \Omega$ , so the width of branch-line is 2.2 mm, and parallel-line is 3.5 mm.

In order to make sure the electromagnetic characteristics of the S-D-CRLH-TL unit cells with different width keep the same, other physical dimensions of this structure should be change. It is known that the three frequency points with -90-degree phase shift of the 50  $\Omega$  transmission line are 3.08 GHz, 4.02 GHz and 5.50 GHz, then, the required 35  $\Omega$  transmission line is designed through similar procedures. The geometrical parameters of the 50  $\Omega$  and 35  $\Omega$  transmission lines are shown in Table 1. The comparison results of these two unit cells are shown in Figure 6.

In Figure 6, the results indicate that there are three frequency points with phase of -90-degree in the passbands. The proposed prototype can be treated as the 50  $\Omega$  and 35  $\Omega$  transmission lines with

Table 1. The physical dimensions of two unit compared	ls (mm).
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	$l_1$	$l_2$	$l_3$	$w_1$	$w_2$	$w_3$	$w_4$	$w_5$
unit1	10	7	3	2.2	1.8	1.2	0.2	0.2
unit2	10	7	3	3.5	2.7	1.2	0.3	0.3



**Figure 6.** Comparison of two unit cells with different width. (a) S-parameters. (b) Phase of  $S_{21}$ .

90-degree phase shift, and based on the above two transmission lines, the branch-line coupler is convenient to synthesize. Besides, compared with the double-Lorentz transmission line proposed in paper [16], the phase of the three frequency points of S-D-CRLH-TL keep the same, and it is more suitable in designing the microwave components, which are sensitive to phase-changing.

## **3.2.** Design of the Proposed Triple-band Branch-line Coupler

Figure 7 shows the structure of the proposed triple-band branch-line coupler. The unit cells of S-D-CRLH-TL are embedded into the branch-lines and parallel-lines. By using the optimization in Ansoft HFSS, when W = L = 10 mm, the performances of this proposed branch-line coupler are the best.



Figure 7. Structure of the proposed branch-line coupler.



Figure 8. The photograph of the fabricated triple-band branch-line coupler.

### 4. MEASURED RESULTS AND DISCUSSIONS

Figure 8 is a photograph of the fabricated triple-band branch-line coupler. The measured and simulated results are shown in Figure 9.

Figure 9 shows that the measured and simulated results are in good agreement with each other, the triple-band operating at 3.06 GHz, 4.00 GHz and 5.54 GHz, as shown in Table 2, the first operating frequency is 3.06 GHz, the useful bandwidth is 2.97 GHz-3.16 GHz, the relative is 6.2%, in this band, the return loss is less than -12 dB, the phase difference is from 80-degree to 94-degree, the performance is very good; the second frequency is 4.00 GHz, the bandwidth is 0.3 GHz, it also has a good performance; the third frequency is 5.54 GHz, it has a very narrow bandwidth, the relative is only 3.4%. The isolation



**Figure 9.** Measured and simulated results. (a) Simulated Sparameters. (b) Measured S-parameters. (c) Phase difference of  $S_{21}$ and  $S_{31}$ .

**Table 2.** The performances of the three bands  $(\Delta S_{21} = ||S_{21}| - 3 \,\mathrm{dB}|, \Delta S_{31} = ||S_{31}| - 3 \,\mathrm{dB}|, \Delta \varphi = ||\varphi(S_{21}) - \varphi(S_{31})| - 90^{\circ}|).$ 

$f/{ m GHz}$	$S_{11} < -10  \mathrm{dB}$	$\Delta S_{21} < 1 \mathrm{dB} \& \Delta S_{31} < 1 \mathrm{dB}$
$3.06\mathrm{GHz}$	$2.81\mathrm{GHz}{-}3.21\mathrm{GHz}$	$2.96\mathrm{GHz}{-}3.16\mathrm{GHz}$
$4.00\mathrm{GHz}$	$3.73\mathrm{GHz}{-4.13\mathrm{GHz}}$	$3.82\mathrm{GHz}{-}4.12\mathrm{GHz}$
$5.54\mathrm{GHz}$	$5.35\mathrm{GHz}{-}5.67\mathrm{GHz}$	$5.48\mathrm{GHz}{-}5.89\mathrm{GHz}$
$f/{ m GHz}$	$\Delta \varphi < 10^\circ$	useable
$3.06\mathrm{GHz}$	$2.97\mathrm{GHz}{-}3.26\mathrm{GHz}$	$2.97\mathrm{GHz}{-}3.16\mathrm{GHz}$
$4.00\mathrm{GHz}$	$3.51\mathrm{GHz}{-4.31\mathrm{GHz}}$	$3.82\mathrm{GHz}{-}4.12\mathrm{GHz}$
$5.54\mathrm{GHz}$	$5.38\mathrm{GHz}{-}5.68\mathrm{GHz}$	$5.48\mathrm{GHz}{-}5.67\mathrm{GHz}$

of this designed branch-line coupler is also great, it is less than  $-12.5 \,\mathrm{dB}$ , especially in the first and second operating band, it reaches to  $-20 \,\mathrm{dB}$ . This proposed branch-line coupler not only has good triple-

band performances, but also is more effective in the situation which is sensitive to phase-changing, as the sign of phase difference in the two outputs at the three frequencies keeps the same. In addition, the whole size of this triple-band branch-line coupler is  $17 \text{ mm} \times 14.4 \text{ mm}$  $(0.173\lambda \times 0.147\lambda)$  ( $\lambda$  is the wavelength in low frequency), it realizes a 73% size reduction in comparison with the conventional branch-line coupler.

### 5. CONCLUSION

A novel miniaturized triple-band branch-line coupler based on S-D-CRLH-TL is proposed in this paper. The electromagnetic characteristics of S-D-CRLH-TL are analyzed by the simulator and equivalent circuit model, and the characteristic of three frequencies with phase of  $-90^{\circ}$  is proved. Then, the proposed branch-line coupler is designed, fabricated and measured. The measured and simulated results are in good agreement, showing that the triple-band operating at 3.06 GHz, 4.00 GHz and 5.54 GHz, the useful bandwidths are 2.97 GHz–3.16 GHz, 3.82 GHz–4.12 GHz and 5.48 GHz–5.67 GHz, this designed coupler has good triple-band performances. In addition, this coupler not only is effective in the situation, which is sensitive to phase-changing, but also can realize a 73% size reduction in comparison with the conventional one.

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